MODELLING HYDROGEN INDUCED STRESS CORROSION CRACKING IN AUSTENITIC STAINLESS STEEL

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ABSTRACT

A model has been developed which simulates the deformation of single crystal austenitic stainless steels and captures the effects of hydrogen on stress corrosion cracking. The model is based on the crystal plasticity theory which relates critical resolved shear stress to plastic strain and the strength of the crystal. We propose an analytical representation of hydrogen interactions with the material microstructure during deformation and simulate the effects hydrogen will have on void growth prior to fracture. Changes in the mechanical properties of the crystal prior to fracture are governed by the interaction of hydrogen atoms and ensembles of dislocations as the crystal plastically deforms and is based on the hydrogen enhanced localised plasticity (HELP) mechanism. The effects of hydrogen on void growth are considered by analysing the effect of hydrogen on the mechanical property of material bounding an embedded void. The model presented has been implemented numerically using the User Material (UMAT) subroutine in the finite element software (ABAQUS) and has been validated by comparing simulated results with experimental data. Influencing parameters have been varied to understand their effect and test sensitivities.

Keywords: Plastic deformation; hydrogen embrittlement; void growth; stress corrosion cracking.

1. INTRODUCTION

Austenitic Stainless Steels such as AISI 304, 310 and 316 have widespread application in the nuclear, automobile, chemical, oil and gas production, refining and medical industries showing a superior strength range, ductility and corrosion resistance when compared to other types of steel [1, 2]. Austenitic Stainless Steels are however vulnerable to Stress Corrosion Cracking (SCC) in specific environmental conditions including when exposed to hydrogen. When steel is embrittled and fails by cracking due to exposure to hydrogen in the presence of stress, the failure mechanism is known as Hydrogen Induced Stress Corrosion Cracking (HISCC) [3]. Hydrogen Enhanced Localised Plasticity (HELP) is a commonly cited failure mechanism used to explain this phenomenon [4-6]. HELP suggests that hydrogen in solid solution reduces barriers to dislocation motion and increases localised deformation [7]. A manifestation of HELP in metals with low hydrogen diffusivity is strain aging and this occurs when dislocation ensembles are "pinned" by hydrogen atoms [8]. It is believed that hydrogen influences dislocation mobility by two competing mechanisms; pinning of dislocation or enhancement of dislocation mobility [6]. Robertson [6] provided evidence of increased dislocation velocity and reduced flow stress due to hydrogen. Stress-strain relationship for homogeneous solid solutions of austenitic stainless steel was studied at different temperatures and strain rates. Yield and flow stresses were observed to increase with hydrogen concentration. Yagodzinskyy and his colleagues [10] observed an increase in crystal strength and flow stress in the hydrogen charged single crystals. Their work provided experimental evidence of dislocation motion restriction due to hydrogen in single crystal austenitic stainless steel. Schebler [11] formulated a model that simulates the deformation of a single crystal face centred cubic (FCC) metal using a crystal plasticity based finite element model (FEM) and similar results to Yagodzinskyy et al [10] were obtained. The facilitation of HISCC via fracture processes of void nucleation, growth and coalescence is well established and there is experimental and theoretical evidence to support this phenomenon. S.P Lynch [12] provided a concise review of the various theories and the reader is referred to this work for more information. We use the Hydrogen Enhanced Strain Induced Vacancy (HESIV) mechanism to explain how hydrogen affects void nucleation and growth during plastic deformation [13]. HESIV proposes that hydrogen promotes strain localisation and increases vacancy formation, agglomeration to form voids, void growth and coalescence [8]. The HESIV mechanism proffers that hydrogen promotes the formation and accelerates the aggregation of vacancies introduced by plastic flow. Voids have also been observed to nucleate and grow due to intense interaction between dislocations in regions of high strain localisation [8]. Martin et al [14, 15] have previously demonstrated that the formation and extension of voids occurred along slip bands and were facilitated by the presence of hydrogen. Bullen et al [16]

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introduced hydrogen into interstitial sites and observed that hydrogen increased void density, but void size was reduced. Matsumoto et al [13, 17] have shown that hydrogen promotes the formation and decreases the removal of vacancies in steel during plastic deformation. Ductile fracture by vacancy condensation is considered a viable and common mechanism for transgranular failure of FCC materials including austenitic stainless steels [18] and will form the basis of modelling in this work. We extend on the above theories and model the response of a single crystal austenitic steel to applied deformation and observe the effect hydrogen has on material mechanical properties and void growth.

2. CRYSTAL PLASTICITY THEORY

Crystal plasticity theory is extended to account for the effects of hydrogen on plastic deformation and fracture of austenitic stainless steel. We assume that the elastoplastic deformation of the crystal is driven primarily by crystalline slip across well-defined planes and dislocation motion. The kinematics of the single crystal constitutive theory is derived from multiplicatively decomposition of the deformation gradient based on the finite strain theory [19].



Figure 1: Representation of the multiplicative decomposition of the deformation gradient

Consider a body deformed as illustrated in Figure 1, we use vectors \mathbf{x}^1 , \mathbf{x}^2 , \mathbf{x}^3 and \mathbf{x}^4 to express a set of particle positions in the configurations B_o , \overline{B} , \widehat{B} and B respectively. B_o represents the original configuration and B represents the final deformed state at time t. Unloading elastically from B gives a configuration \widehat{B} that still has the permanent plastic deformation and the dilatational distortion induced by hydrogen. Excluding the distortional effect of hydrogen gives a second intermediate configuration, \overline{B} . For finite strain theory, the deformation gradient matrix can be used to capture deformation histories so that F^e , F^h and F^p are the elastic, hydrogen and plastic parts of the deformation gradient respectively. These can be expressed as follow

$$F = \frac{\partial x_i^4}{\partial x_j^1} ; \ F^e = \frac{\partial x_i^4}{\partial x_j^3} ; \ F^h = \frac{\partial x_i^3}{\partial x_j^2}; \ F^p = \frac{\partial x_i^2}{\partial x_j^1}$$
(1)

Applying the chain rule for partial differential equations gives;

$$\frac{\partial x_i^4}{\partial x_j^1} = \frac{\partial x_i^4}{\partial x_j^3} \frac{\partial x_i^3}{\partial x_j^2} \frac{\partial x_i^2}{\partial x_j^1} \tag{2}$$

or

$$F = F^e F^h F^p \tag{3}$$

The elastoplastic formulations defined by Marin [20] are modified to include the dilatational effects of hydrogen as illustrated in figure 1;

$$F = V_e F^*, \quad F^* = R^e F^h F^p \tag{4}$$

F represents the deformation gradient in the final deformed configuration B from an original configuration B_o . V_e is the elastic stretching of the crystal. R^e is the rigid crystal body rotation, F^p represents plastic slip and is deformation gradient for the first intermediate configuration designated \overline{B} . F^h represents the dilatational effect of hydrogen and is deformation gradient for the second intermediate configuration designated \hat{B} . The third intermediate configuration \tilde{B} is obtained hypothetically by unloading elastic stretch from the final configuration B through V^{e-1} without excluding rotation and is represented by the deformation gradient F^* .

The velocity gradient in the final deformed configuration B can be expressed as;

$$l = FF^{-1} \tag{5}$$

and in the intermediate configuration \tilde{B} as

$$\tilde{L} = V^{e^{-1}} l V^e = V^{e^{-1}} V^e + \tilde{L}^*$$
(6)

By using equations (4), (5) and (6), and simplifying:

$$\tilde{\boldsymbol{L}}^* = \dot{\boldsymbol{R}}^e \boldsymbol{R}^{e^T} + \boldsymbol{R}^e \hat{\boldsymbol{L}}^h \boldsymbol{R}^{e^T} + \boldsymbol{R}^e \boldsymbol{F}^h \bar{\boldsymbol{L}}^p \boldsymbol{F}^{h^{-1}} \boldsymbol{R}^{e^T}$$
(7)

 \tilde{L}^* describes plastic flow due to crystallographic slip, the dilatational effect of hydrogen and rotation of the lattice in the \tilde{B} configuration. Velocity gradient due to dilatational effect of hydrogen, \hat{L}^h , is expressed as per the Sofronis relationship [7] as follows:

$$\boldsymbol{L}^{h} = \dot{\boldsymbol{F}}^{h} \cdot \boldsymbol{F}^{h^{-1}} = \frac{d}{dt} \left(1 + \frac{(c-c_{0})\lambda}{3} \right) \boldsymbol{I} \cdot \left[\left(1 + \frac{(c-c_{0})\lambda}{3} \right) \right]^{-1} \boldsymbol{I} = \frac{1}{3} \Lambda(c) \dot{c} \boldsymbol{I}, \quad \Lambda(c) = \frac{3\lambda}{3+(c-c_{0})}$$
(8)

Here c and c_o are current and initial (stress-free) concentrations of hydrogen at the material point (expressed in hydrogen atoms per lattice atom). λ is equal to $\frac{\Delta V}{V_m}$, ΔV is the volume change per atom of hydrogen introduced into solid solution and V_m is the mean atomic volume of the host metal atom.

For austenitic stainless steels, bulk diffusion of hydrogen is relatively slow due to the low diffusivity of hydrogen in FCC material when compared with body centered cubic (BCC) material [9]. A comparison of hydrogen diffusivity for FCC material and experimental observation supporting constant hydrogen concentration has been discussed by Schebler [11]. Based on this, the term " $c - c_0$ " tends to zero and L^h is reduced to an identity matrix. The plastic deformation characteristics of the material is however altered by the presence of atomic hydrogen and a discussion of these effects will be covered in section 3.

The plastic part of velocity gradient, \bar{L}^p , can be defined as:

$$\bar{L}^{p} = \sum_{\alpha=1}^{N} \dot{\gamma}^{\alpha} \, \bar{s}^{\alpha} \otimes \bar{m}^{\alpha} \tag{9}$$

where $\dot{\gamma}^{\alpha}$ is the shear strain rate due to slip, \bar{s}^{α} and \bar{m}^{α} are the slip direction and normal to slip plane vectors respectively. After substituting these results in (7), the following relation is obtained for \tilde{L}^* :

$$\tilde{L}^* = \tilde{\Omega}^e + \sum_{\alpha=1}^{N} \dot{\gamma}^{\alpha} \, \tilde{s}^{\alpha} \otimes \tilde{m}^{\alpha} \tag{10}$$

Here, $\widetilde{\Omega}^e = \dot{R}^e R^{e^T}$ represents rigid body elastic spin. \overline{s}^{α} and \overline{m}^{α} are the slip direction and normal respectively. \widetilde{s}^{α} is $R^e \overline{s}^{\alpha}$ and \widetilde{m}^{α} is $R^e \overline{m}^{\alpha}$.

For elasticity, the Second Piola-Kirchhoff stress, \tilde{S} , is given as by:

$$\widetilde{S} = \widetilde{\mathbb{C}^e} \colon \widetilde{E^e}$$
(11)

 $\tilde{\mathbb{C}}^e$ is the anisotropic elasticity tensor and \tilde{E}^e is the Green-Lagrange strain tensor.

We additionally decompose the velocity gradient into a symmetric, d, and skew, w, parts i.e. l = d + w. And in the intermediate configuration, \tilde{B} , the rate of deformation tensor is given as:

$$\widetilde{\boldsymbol{D}} = \boldsymbol{V}^{e^T} \boldsymbol{d} \boldsymbol{V}^e = \dot{\widetilde{\boldsymbol{E}}}^e + \widetilde{\boldsymbol{D}}^*$$
(12)

$$\widetilde{\boldsymbol{D}}^* = \operatorname{sym}(\widetilde{\boldsymbol{C}}^e \widetilde{\boldsymbol{\Omega}}^e) + \sum_{\alpha=1}^{N} \dot{\gamma}^\alpha \operatorname{sym}(\widetilde{\boldsymbol{C}}^e \widetilde{\boldsymbol{Z}}^\alpha)$$
(13)

Spin of the lattice due to plastic deformation is given as:

$$\widetilde{\boldsymbol{W}} = \boldsymbol{V}^{e^{T}} \boldsymbol{w} \boldsymbol{V}^{e} = skew(\boldsymbol{V}^{e^{T}} \dot{\boldsymbol{V}}^{e}) + \widetilde{\boldsymbol{W}}^{*}$$
(14)

$$\widetilde{\boldsymbol{W}}^* = \operatorname{skew}(\widetilde{\boldsymbol{C}}^e \widetilde{\boldsymbol{\Omega}}^e) + \sum_{\alpha=1}^N \dot{\gamma}^\alpha \operatorname{skew}(\widetilde{\boldsymbol{C}}^e \widetilde{\boldsymbol{Z}}^\alpha)$$
(15)

Plastic slip evolution by shear strain rate is defined by the power law in (16). Shear strain rate $\dot{\gamma}^{\alpha}$ on the α^{th} slip system depends on the resolved shear stress and the strength of the slip system.

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$$\dot{\gamma^{\alpha}} = \dot{\gamma_0^{\alpha}} \left[\frac{|\tau^{\alpha}|}{\kappa_s^{\alpha}} \right]^{\frac{1}{m}} \operatorname{sign}(\tau^{\alpha})$$
(16)

 $\dot{\gamma}_0^{\alpha}$ is the reference shear strain rate on the α^{th} slip system, κ_s^{α} is the current slip system strength, τ^{α} is resolved shear stress, *m* is strain rate sensitivity parameter. Voce type hardening was incorporated in the model using the evolution relation in (17). The slip system is made to harden with the evolution of accumulated slip till a saturation value is reached, beyond which it deforms in a perfectly plastic manner.

$$\dot{\kappa}_{s}^{\alpha} = h_{0} \left(\frac{\kappa_{s,s}^{\alpha} - \kappa_{s}^{\alpha}}{\kappa_{s,s}^{\alpha} - \kappa_{s,0}^{\alpha}} \right) \sum_{\alpha=1}^{N} |\dot{\gamma}^{\alpha}|, \ \kappa_{s,s}^{\alpha} = \kappa_{s,s0}^{\alpha} \left[\frac{\sum_{\alpha} |\dot{\gamma}^{\alpha}|}{\dot{\gamma}_{s0}} \right]^{1/m'} \tag{17}$$

 $\dot{\kappa}_s^{\alpha}$ is the current rate of hardening, κ_s^{α} is the current slip system strength, h_0 is the reference hardening coefficient, $\kappa_{s,s}^{\alpha}$ is the saturation value of strength which depends on the accumulated slip $\sum_{\alpha} |\dot{\gamma}^{\alpha}|$, and its evolution is given by a power law. $\kappa_{s,0}^{\alpha}$, $\dot{\kappa}_{s,50}^{\alpha}$, $\dot{\gamma}_{s,0}^{\alpha}$ and m' are the material parameters controlling the evolution of strength in the crystal. Critical resolved shear stress (CRSS) of each of the slip systems are assigned as $\kappa_s^{\alpha}(t=0)$ in (17).

3. EFFECTS OF HYDROGEN

Hydrogen atoms can be introduced into austenitic stainless steel during manufacturing, fabrication (e.g. welding), in service (transport/storage of hydrogen containing fluid, cathodic protection etc.) or generated from chemical dissociation of water due to corrosion reactions [21]. Hydrogen atoms will either reside at normal interstitial lattice sites (NILS) or in trap sites introduced to the material by plastic deformation [22]. According to Oriani's theory, hydrogen residing in these two sites are in equilibrium such that the total hydrogen concentration C_{Total} is defined by the relationship below [22]:

$$\mathsf{C}_{Total} = \mathsf{C}_L + \mathsf{C}_T \tag{18}$$

 C_L and C_T represent hydrogen atoms residing in NILS and trap sites respectively. According to Fick's first law, there would be transfer of hydrogen atoms between sites if a concentration gradient exist. The proportional relationship between the hydrogen activity in traps a_T and NILS a_L is captured by the equilibrium constant K_T

$$\mathbf{a}_T = \mathbf{K}_T \boldsymbol{a}_L \tag{19}$$

The hydrogen activity a_i in each site relates to fraction of species occupancy θ_i as follows;

$$a_i = \frac{\theta_i}{1 - \theta_i} \tag{20}$$

Starting from a reference of $a_i = \theta_i$ tending towards zero and combining (19) and (20) gives;

$$\frac{\theta_{\rm T}}{1-\theta_{\rm T}} = K_{\rm T} \frac{\theta_L}{1-\theta_L} \tag{21}$$

 θ_T is hydrogen occupancy of trap sites, θ_L is hydrogen occupancy of lattice sites and K_T is equilibrium constant. Concentration of hydrogen residing in trapping sites C_T is given as:

$$C_{\rm T} = \theta_{\rm T} \psi N_{\rm T} \tag{22}$$

 ψ is the number of sites per trap and N_T is the number of traps per unit lattice given as:

$$N_{\rm T} = \frac{\sqrt{3}}{a_{fcc}}\rho \tag{23}$$

 a_{fcc} is lattice parameter for FCC metal. Evolution of bulk dislocation density ρ is given as:

$$\int_{0}^{t} \dot{\rho} \, dt = (k_1 \sqrt{y}) \int_{0}^{t} / \dot{\gamma} / dt$$
(24)

 $\dot{\rho}$ represents incremental changes in dislocation density. $\dot{\gamma}$ represents incremental changes in strain. k_1 is a constant associated with immobilised dislocation and \sqrt{y} is average spacing between dislocations [23]. Equation (24) considers the effects of hydrogen on material behaviour during early stages of deformation (stages 1 and 2). Experimentally, it has been observed that dislocation annihilation only becomes significant during the later stages (stage 3) of deformation [24]. We assume total hydrogen concentration is constant at each material point due to low diffusion of hydrogen in austenitic stainless steels [25]. It is important to note that although total hydrogen concentration C_{Total} is constant, there is a transfer of hydrogen atoms from NILS to more energetically favourable traps created during plastic deformation. C_{T} is expressed as a function of C_{Total} and the number of traps N_T by the Krom's relationship [26]

$$C_{\rm T} = \frac{1}{2} \left[\frac{N_{\rm L}}{K_{\rm T}} + C_{\rm Total} + N_{\rm T} - \sqrt{\left(\frac{N_{\rm L}}{K_{\rm T}} + C_{\rm Total} + N_{\rm T} \right)^2 - 4N_{\rm T}C_{\rm Total}} \right]$$
(25)

 N_L is the number of atoms per unit NILS. We introduce two dimensionless terms to account for the changes to the material properties due to the presence of atomic hydrogen;

Hydrogen initial strength coefficient H_i which quantifies the effect of hydrogen on initial crystal strength.
 Hydrogen hardening coefficient H_f that quantifies effect of hydrogen on strain hardening.

Initial crystal strength $\kappa_{h,0}^{\alpha}$ in the presence of hydrogen is given by the following expression;

$$\kappa_{h,0}^{\alpha} = \kappa_{s,0}^{\alpha} * \left(1 + \mathrm{H_i}\mathrm{C_{initial}}\right) \tag{26}$$

 $\kappa_{s,0}^{\alpha}$ is crystal strength in hydrogen free condition. $C_{initial}$ is the amount of hydrogen in trapping sites before plastic deformation and relates to hydrogen uptake given by Caskey Jr [27]

$$C_{\text{initial}} = f C_L e^{18400} / (\text{RT})$$

$$(27)$$

f is a fraction of alloy atoms which are associated with a unit length of dislocation and is a function of initial dislocation density (in a strain free state). C_L is the concentration of hydrogen in the lattice sites. 18400 J/mol is bonding energy for hydrogen to dislocations in austenitic stainless steels. The form of (27) is consistent with Oriani's theory (see equation 22). Hydrogen concentration in traps existing before deformation, $C_{initial}$ is shown to be directly proportional to the amount of hydrogen residing in NILS, C_L . The term f is a material property which captures the amount of dislocations expected in austenitic stainless steel not subject to loading and is obtained empirically from testing [27].

The evolution of crystal strength given in (17) is modified as follows:

$$\dot{\kappa}_{s}^{\alpha} = h_{0} \left(\frac{\kappa_{s,s}^{\alpha} - \kappa_{s}^{\alpha}}{\kappa_{s,s}^{\alpha} - \kappa_{s,0}^{\alpha}} \right) (1 + \mathrm{H}_{\mathrm{f}} \mathrm{C}_{\mathrm{T}})$$
(28)

4. METHODOLOGY AND RESULTS

Finite Element Model (FEM) simulations have been performed using ABAQUS/Standard analysis [28]. Threedimensional RVE models were constructed and meshed using the ABAQUS/CAE function with reduced-integrated, first-order linear brick elements (C3D8R). Load was applied to the RVE using displacement controlled analysis. Material response relationships and equations presented in sections 2 and 3 have been implemented numerically using the User Material (UMAT) function in ABAQUS. FEM simulations were performed by replicating the case of an austenitic stainless steel single crystal subjected to uniaxial tension oriented for multi-slip with displacement control loading applied. Tensile tests performed on the RVE specimen were done by applying identical conditions and parameters used in the real world experiments. Comparisons have then been made between simulated results and experimental data for model validation. Experimental tensile tests referenced, were performed on AISI316LN austenitic stainless steel single crystals of nominal chemical composition 18Cr-12Ni-2Mo alloyed with 0.5 wt. % of nitrogen by Yagodzinskyy et al [8]. Samples were cut parallel to the (110) crystal plane and tensile loaded in the <001> direction at a strain rate of 8 x 10^{-4} s⁻¹ with atomic hydrogen content of 0.64%. Figure 2 show that the FEM simulated analysis and experimental results are generally in agreement. It is noted from figure 2 that there is an difference in elastic modulus for the specimen exposed to hydrogen in the experimental data presented. This differs from model results which assumes that elastic properties are unchanged by hydrogen. Plastic work is spent solely in the generation and migration of dislocation, so hydrogen (which affects only the plastic component) will not change the elastic constants. In experiments, a small disruption in lattice structural and elastic constants may occur as observed by Lee [29] so it is inferred that this change is reflected in the observed discrepancy in the elastic part of the deformation. The current study seeks to understand the effect of hydrogen on plastic deformation and fracture vis-a-vis the HELP mechanism using the large strain theory. Plastic deformation is much larger in comparison to this discrepancy so these minor excursions in elasticity have been ignored but will be included in future model. Model parameters used are presented in Table 1.

				parameters		
Model Parameters	H _i	C _{INITIAL} (%at)	$K_1 \sqrt{y}$	N_L/K_T	c _{Total} (%at)	H _f
	1.6	0.05	2.4	5.5e+26	0.64	0.05

Table 1 Model validation parameters

 $C_{initial}$ is calculated from relationship in (27). N_L is a material constant given by N_A/V_M . N_A is Avogadro's number

and V_M is molar volume. K_T is the equilibrium constant given by $\exp\left(\frac{W_B}{RT}\right) W_b$ is binding energy, R is universal gas constant and T is absolute temperature. C_{Total} is selected to match experimental data used for validation. $K_1 \sqrt{y}$ is a material constant that captures athermal dislocation multiplication with respect to straining during stages 1 and 2. K_1 is a constant associated with athermal storage of moving dislocations which become immobilised after traveling a distance proportional to the average spacing between dislocations, \sqrt{y} . H_i and H_f are selected to match experimental results for hydrogen charged samples- both terms are zero in a material not exposed to hydrogen. To investigate the effects of hydrogen and other key parameters, a parametric review has been performed. H_i , H_f $C_{initial}, C_{Total}$, $k_1\sqrt{y}$ and other parameters have been varied over selected ranges to observe the individual effects on the material stress – strain response. The stress - strain relationship of the material with different values of H_i and H_f are presented in Figure 3 and Figure 4 respectively. Parameters used for these assessments are presented in Table 2 and Table 3



Figure 2 Simulated results with experiments data (Yagodzinskyy 2014)



Figure 3 Stress strain curves with varying Hi

Results observed were consistent with experimental observations, the initial critical resolved shear stress in-

creased with H_i (see Figure 3). There was also a shift in the graph to higher stresses required for plastic deformation to occur representing the "locking" effect hydrogen has on Frank-Read and other sources of dislocation. Material work hardening was observed to increase with H_f (see Figure 4). The increase in slope of the curve represents the ageing effect of dislocation by hydrogen atoms in austenitic stainless steel grains. Figure 5 shows the variance in the stress strain curve with hydrogen content. It can be observed that there was an increase in uniaxial tension yield strength of the austenitic stainless steel single crystals as reported by experiments performed by Yagodzinskyy et al [30]. There is also a visible increase in work hardening as observed by Delafosse [31].





Figure 5 Stress strain curves with varying Hydrogen content

Table 2 Model validation parameters (for H _i)							
Model Parameters	H _i	C _{INITIAL} (%at)	$K_1 \sqrt{y}$	N_L/K_T	c _{Total} (%at)	H _f	
	1, 2.5, 3.75, 5.0, 6.25, 7.5	0.05	2.4	5.5e+26	0.64%	0.05	

Table 5 Woder variation parameters (101 11f)							
Model Parameters	H _i	C _{INITIAL} (%at)	$K_1 \sqrt{y}$	N_L/K_T	c _{Total} (%at)	H _f	
	10	0.05	2.4	5.5e+26	0.64%	$0.05, \overline{0.5}, 1.0, 1.5, 2.0, 2.5$	

Table 3 Model validation parameters (for H_f)

For the void growth analysis, an RVE model with an embedded void of known initial void fraction is constructed and meshed using ABAQUS/CAE with reduced-integration elements (C3D8R) (see illustration of void model in Figure 6).



Figure 6 RVE Specimen half sectioned to show spherical embedded void

The porous crystal plasticity model and the relationship between void growth, strain, stress triaxiality, initial void size and crystal orientation have been discussed by other authors [32, 33, 34] so only a summary is given here. Void fraction evolution is defined as follows;

$$f_o = \frac{V_{void}}{V_{Total}} \tag{29}$$

 V_{void} is the void volume and V_{total} is the total volume of the element i.e. solid material and void. Using the validated material parameters from Table 1, void growth analyses have been performed over selected ranges of hydrogen to observe the effects on the material stress strain response and analyse the effect of hydrogen on void growth. Displacements in the lateral direction were tuned to keep applied stress triaxialities constant using a multipoint constraint (MPC) user subroutine of the ABAQUS software, while volume averaged stress triaxiality was varied depending on the void growth. Figure 7 shows that for the RVE embedded with a void, hydrogen was observed to increase the overall equivalent plastic stresses for similar equivalent strain values. This indicates a hardening effect of atomic hydrogen. Results also show higher values of void fraction at stress triaxiality of 3 when compared to stress triaxiality of 1 (Figure 8). This was observed for both hydrogen containing and hydrogen free conditions. Atomic hydrogen is inferred to have slowed void growth for both triaxialities 1 and 3 as lower void fraction values were observed for hydrogenated element for similar equivalent strain values. This observation is consistent with experimental findings for austenitic stainless steels and other FCC metals exposed to hydrogen [35, 36]. Hydrogen in traps concentrate around the boundary of the embedded void during elastic deformation and there is little hydrogen concentration in traps observed in regions remote from the void (Figure 9a & 9b). As equivalent stress values approach yield, hydrogen transfer becomes more intense in areas in close proximity to the void (Figure 9c) and then extends to regions which are remote from the void (See Figure 9d). This progression in hydrogen exchange from NILS to trapping sites is induced by increased deformation at these sites and is consistent with observations in literature [37]. As noted in the introduction section, experimental observations have shown that hydrogen atoms act to "pin" down dislocations groups [8]. It can be inferred from results that hydrogen reduces void growth by immobilising dislocations immediately bounding the void. This leads to an increase in the work hardening and slowdown in dislocation motion in the material region which would restrict void expansion. This phenomenon has not been observed in the hydrogen free simulations where a higher values of void fraction have been reported for similar equivalent strains values.



Figure 8 Normalised void fraction relationship with equivalent strain



(c) Equivalent strain = 2.68%

(d) Equivalent strain =5%

Figure 9 Concentration of hydrogen in trapping sites expressed in % atom (SDV 71) (a) No strain applied (b) During elastic deformation (c) Early stages of plastic deformation (d) Later stages of plastic deformation

5. CONCLUSIONS

The model presented simulates the hydrogen induced stress corrosion cracking mechanism by capturing experimental knowledge of hydrogen -dislocation interactions within a crystal plasticity computational framework. Hydrogen concentration in traps have been modelled to increase the critical resolved shear stress and work hardening of the material. These have been captured by introducing two terms. The hydrogen initial strength coefficient H_i quantifies the effect of hydrogen on the initial yield strength of the crystal. Hydrogen in traps increase dislocations density which leads to macroscopic crystal hardening and this has been captured by a term called hydrogen hardness coefficient (H_f). Void growth is slowed by hydrogen which accumulate around the void boundary during the elastic part but its effects extend to areas remote from the void as plastic deformation progresses. Higher critical resolved stress values were observed in the presence of hydrogen for various stress triaxialities for both voided and nonvoided RVE samples. Hydrogen was found to reduce void growth by immobilising dislocations leading to an increase in the work hardening. Experimental results have shown that an increase in void density and coalescence is favoured instead of void growth in FCC structured austenitic stainless steels in the presence of hydrogen [8, 16, 38]. This phenomenon is typically characterised by a reduction in the average size of dimples on fracture surfaces observed after failure of austenitic stainless steel [35]. Hydrogen effects on void density have not be captured in this model but is subject to future consideration and future work will extend the model to capture the effect of hydrogen on void coalescence.

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