

Manuscript Number: JNGSE-D-20-00053R1

Title: Scale-span pore structure heterogeneity of high volatile bituminous coal and anthracite by FIB-SEM and X-ray  $\mu$ -CT

Article Type: Full Length Article

Keywords: coals; scale-span pore structure; FIB-SEM tomography; X-ray  $\mu$ -CT; 3D fractal dimension

Corresponding Author: Dr. Yidong Cai, Ph.D

Corresponding Author's Institution: China University of Geosciences, Beijing

First Author: Qian Li

Order of Authors: Qian Li; Dameng Liu; Yidong Cai, Ph.D; Bo Zhao; Yongkai Qiu; Yingfang Zhou

Abstract: Visualizing and quantifying the pore structure at the nano-micro scale is critical for understanding the micro fluid transport and enrichment in coalbed methane (CBM) reservoirs. In this work, the detailed micro-nano scale pore parameters such as pore counts, pore area, pore volume and pore size distribution can be acquired by the focused ion beam-scanning electron microscopy (FIB-SEM) and X-ray computed micro-tomography (X-ray  $\mu$ -CT) techniques. Meanwhile, the pore network model (PNM) was adopted to describe and quantify the pore throat characteristics, which found that the pore throats of the sample LHG well developed and are conducive to seepage. Additionally, the three-dimensional fractal dimension (D3) by the box-counting method was used to evaluate the pores spatial heterogeneity. The D3 of sample LHG and sample L-1 are 2.23 and 2.04 (for FIB-SEM with pore size of 10 nm to ~1000 nm), 2.69 and 2.51 (for X-ray  $\mu$ CT with pore size over 500 nm), respectively. The results indicate that the pore network has self-similarity with a secondary development. The variable trends from tens of nanometers to micrometers through the FIB-SEM and X-ray  $\mu$ CT images. For the relationship between porosity and D3, two opposite trends have emerged. The positive correlation trend should be related to the complex pore structure. The more complex the pore structure is, the higher the porosity is. The negative correlation should contribute to a lot of mineral-filled pores. Pores filled with minerals that will increase the proportion of small pores and decrease the porosity, which causes that the spatial complexity of the pore networks is increased, and the D3 is increased. Therefore, this work may provide insights into the gas storage and seepage capabilities of coalbed methane (CBM) reservoirs, and thus will be favorable for enhancing CBM recovery.

Research Data Related to this Submission

-----  
There are no linked research data sets for this submission. The following reason is given:

Data will be made available on request

### **Highlights**

- 3D pore networks of coals were compared by FIB-SEM and X-ray  $\mu$ CT.
- Multiscale heterogeneity of pore networks was evaluated by fractal method.
- Factors affecting the pore network complexity were revealed.

# Scale-span pore structure heterogeneity of high volatile bituminous coal and anthracite by FIB-SEM and X-ray $\mu$ -CT

Qian Li<sup>a, b</sup>, Dameng Liu<sup>a, b</sup>, Yidong Cai<sup>a, b, \*</sup>, Bo Zhao<sup>c</sup>, Yongkai Qiu<sup>a, b</sup>, Yingfang Zhou<sup>d</sup>

<sup>a</sup>*School of Energy Resources, China University of Geosciences, Beijing 100083, China*

<sup>b</sup>*Coal Reservoir Laboratory of National Engineering Research Center of CBM Development & Utilization, China University of Geosciences, Beijing 100083, China*

<sup>c</sup>*School of Water Resources and Environment, China University of Geosciences, Beijing 100083, China*

<sup>d</sup>*School of Engineering, Fraser Noble Building, King's College, University of Aberdeen, AB24 3UE Aberdeen, UK*

## Abstract

Visualizing and quantifying the pore structure at the nano-micro scale is critical for understanding the micro fluid transport and enrichment in coalbed methane (CBM) reservoirs. In this work, the detailed micro-nano scale pore parameters such as pore counts, pore area, pore volume and pore size distribution can be acquired by the focused ion beam-scanning electron microscopy (FIB-SEM) and X-ray computed micro-tomography (X-ray  $\mu$ -CT) techniques. Meanwhile, the pore network model (PNM) was adopted to describe and quantify the pore throat characteristics, which found that the pore throats of the sample LHG well developed and are conducive to seepage. Additionally, the three-dimensional fractal dimension ( $D_3$ ) by the box-counting method was used to evaluate the pores spatial heterogeneity. The  $D_3$  of sample LHG and sample L-1 are 2.23 and 2.04 (for FIB-SEM with pore size of 10 nm to ~1000 nm), 2.69 and 2.51 (for X-ray  $\mu$ CT with pore size over 500 nm), respectively. The results indicate that the pore network has self-similarity with

1 23 a secondary development. The variable trends from tens of nanometers to micrometers through the  
2  
3 24 FIB-SEM and X-ray  $\mu$ CT images. For the relationship between porosity and  $D_3$ , two opposite  
4  
5  
6 25 trends have emerged. The positive correlation trend should be related to the complex pore  
7  
8  
9 26 structure. The more complex the pore structure is, the higher the porosity is. The negative  
10  
11  
12 27 correlation should contribute to a lot of mineral-filled pores. Pores filled with minerals that will  
13  
14  
15 28 increase the proportion of small pores and decrease the porosity, which causes that the spatial  
16  
17  
18 29 complexity of the pore networks is increased, and the  $D_3$  is increased. Therefore, this work may  
19  
20  
21 30 provide insights into the gas storage and seepage capabilities of coalbed methane (CBM)  
22  
23  
24 31 reservoirs, and thus will be favorable for enhancing CBM recovery.

25 32 **Keywords:** coals; scale-span pore structure; FIB-SEM tomography; X-ray  $\mu$ -CT; 3D fractal  
26  
27  
28 33 dimension  
29

30 34  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65

## 1. Introduction

With increasing global demand for energy resources, coalbed methane (CBM) stored in coal seam has been paid considerable attention due to its triple play of mining safety, environment amity, and economical energy in recent years (Karacan et al., 2011; Vishal et al., 2015; Zhou et al., 2018).

Coal is usually characterized as a dual-pore system, including matrix pores and cleat systems (macropores and fractures) (Clarkson and Bustin, 1999; Gan et al., 1972; Warren and Root, 1963).

About 95% of the adsorbed gas is stored in the matrix pores of the coal. The cleat system is considered to be essential channels of gas and water output (Liu et al., 2017; Pillalamarry et al., 2011; Weishauptová et al., 2004). The pore structure affects not only the gas flow but also the gas adsorption capability and gas storage capacity (Cai et al., 2013; Clarkson and Bustin, 1999; Crosdale et al., 1998; Liu et al., 2017; Weishauptová et al., 2004; Zheng et al., 2018). The conventional reservoirs (such as sandstone reservoirs) are characterized by micro-scale pores, whereas nano-scale pores usually dominate coal reservoirs (Jiao et al., 2014; Tang et al., 2016). Therefore, the nano-scale pores are of great significance for understanding CBM adsorption and CBM resource assessment.

Experimental works have demonstrated that coal can have a range of pore sizes and a complex pore size distribution (Gan et al., 1972) through multiple techniques including transmission electron microscope (TEM) and field emission scanning electron microscope (FE-SEM) (Pan et al., 2016), mercury intrusion porosimetry (MIP) (Rigby et al., 2008) and nuclear magnetic resonance (NMR) (Zheng et al., 2018); N<sub>2</sub> low-pressure adsorption (Cai et al., 2018) and CO<sub>2</sub> adsorption (Mastalerz et al., 2012); small-angle neutron scattering (SANS) (Sakurovs et al., 2018) and small-angle X-ray scattering(SAXS) (Okolo et al., 2015). The above techniques mainly

1 57 focused on the comprehensive pore characteristics of entire coal core while lacking of the  
2  
3 58 information for realistic pore networks. Therefore, evaluating and quantifying realistic pore-throat  
4  
5  
6 59 characteristic including distribution, location and orientation as well as mineral morphology  
7  
8  
9 60 remain an ongoing challenge, which is worthwhile devoting more efforts. In recent years,  
10  
11  
12 61 reconstructing 3D pore structures has emerged as an exciting technique (Balucan et al., 2018;  
13  
14 62 Fang et al., 2019; Liu et al., 2017; Mathews et al., 2017; Saif et al., 2017).

16  
17 63 For 3D characterization of pore structure, two favorite techniques which can offer 3D parameters  
18  
19  
20 64 of unconventional reservoir (e.g., shale and coal) at high resolution are focused ion beam-scanning  
21  
22  
23 65 electron microscopy (FIB-SEM) and X-ray computed micro-tomography (X-ray  $\mu$ -CT) (Hemes et  
24  
25 66 al., 2015; Liu et al., 2017; Saif et al., 2017; Silin and Kneafsey, 2012). 3D pore structure by  
26  
27  
28 67 FIB-SEM measurement has not been efficiently reported, especially for pores with diameter < 100  
29  
30  
31 68 nm, which is of great significance for CBM adsorption, desorption and diffusion (Cai et al., 2013).

33  
34 69 FIB-SEM combines the imaging capabilities of the SEM with the precise milling and  
35  
36  
37 70 cross-section capability of a FIB. For the regions of interest, the sample can be serially sliced to  
38  
39  
40 71 produce a high-resolution of 10~20 nm/pixel (Wargo et al., 2013) (~10nm/pixel in this article).

41  
42 72 For X-ray  $\mu$ -CT, previous researchers found that X-ray  $\mu$ -CT could effectively and  
43  
44  
45 73 non-destructively acquire the fracture/cleat density, cleat surface morphology and the pore space  
46  
47  
48 74 (Saif et al., 2017). However, due to image resolution limitations, X-ray  $\mu$ -CT may only show the

49  
50 75 | ~~macropore~~-micro-scale pore 3D structure characteristics rather than nano-scale pores or gas  
51  
52  
53 76 adsorption space. The pore structure heterogeneity in coals possibly affects the  
54  
55  
56 77 macro-heterogeneity of the CBM reservoir, thus affecting the storage, seepage, and output of  
57  
58  
59 78 CBM (Zheng et al., 2018). For instance, the effects of pores on gas adsorption and seepage can be

1 79 assessed by the pore fractal characteristics at different sizes (Cai et al., 2013; Peng et al., 2017).  
2  
3 80 Moreover, the seepage-pores contribution on core permeability can be evaluated by using classic  
4  
5  
6 81 geometry and thermodynamics fractal model (Peng et al., 2017). Besides, Nakagawa et al. (2000),  
7  
8  
9 82 Okolo et al. (2015) and Sakurovs et al. (2012) utilized SAXS and SANS techniques to acquire the  
10  
11 83 fractal characteristics and pore size distribution, respectively. X-ray  $\mu$ CT technique has been  
12  
13  
14 84 successfully used to evaluate pore and fracture heterogeneity of different rank coals (Li et al.,  
15  
16  
17 85 2017). Normally, the fractal theory is an efficient way to quantitatively assess the irregularity of coal  
18  
19  
20 86 surface based on scanning electron microscopy and low-temperature nitrogen adsorption (Liu and  
21  
22  
23 87 Nie, 2016). However, a few studies were conducted on the spatial heterogeneity of the pore  
24  
25  
26 88 network by using the box-counting method (Russell et al., 1980). Previous studies (Krohn and  
27  
28  
29 89 Thompson, 1986; Liu and Nie, 2016) also confirmed that the fractal dimension by the  
30  
31 90 box-counting method can be adequately used to characterize the heterogeneity of coal pore  
32  
33  
34 91 distribution. Therefore, the box-counting method was adopted to characterize the 3D pore  
35  
36  
37 92 heterogeneity in this study.  
38  
39 93 In this work, a combined pore size classification of super micropores ( $< 2$  nm), micropores (2-10  
40  
41  
42 94 nm), mesopores ( $10$ - $10^2$  nm), macropores ( $10^2$ - $10^3$  nm), super macropores ( $10^3$ - $10^4$  nm) and  
43  
44  
45 95 micro-fractures ( $> 10^4$  nm) from our previous research (Cai et al., 2013) will be adopted. We  
46  
47  
48 96 combine FIB-SEM and X-ray  $\mu$ CT techniques to evaluate the nano-microscale pore structure  
49  
50  
51 97 combined with fractal analysis. Firstly, the pore networks are established to evaluate the  
52  
53  
54 98 differences in nano and microstructure characteristics with the data of porosity, pore counts, pore  
55  
56  
57 99 area and pore volume. Secondly, the pore network model (PNM) is established by Avizo software to  
58  
59  
60 100 describe and quantify the pore throat. Additionally, with the obtained high-resolution FIB-SEM and  
61  
62  
63  
64  
65

101 X-ray  $\mu$ CT images, the fractal analysis is conducted by using the box-counting method. Finally,  
102 the 3D pore network can be quantitatively evaluated. Therefore, this work may benefit the  
103 understanding of the complex structure of nano-micro-scale pore that affecting gas storage and  
104 seepage capabilities, and also will be conducive to CBM reservoir improvement.

## 105 **2. Samples and methodology**

### 106 **2.1. Sample preparation and basic information**

107 Two coal samples were collected from the Liu Huanggou block of the southern Junggar Basin  
108 (LHG, 0.98%  $R_{o,m}$ ) and the Zhengzhuang block of the southern Qinshui basin (L-1, 2.73%  $R_{o,m}$ ),  
109 China. Measurements of maximum vitrinite reflectance ( $R_{o,m}$ ) (immersion in oil) and maceral  
110 composition were conducted with a microscope photometer (MPV-III, Leitz Company of  
111 Germany) as in our previous research (Cai et al., 2018). An automatic proximate analyzer  
112 5E-MACIII was used to analyze the moisture, ash yield, volatile matter, and fixed carbon contents.  
113 Table 1 shows the  $R_{o,m}$ , maceral composition, and the proximate analysis of the coals. The  
114 maximum vitrinite reflectance in oil immersion ( $R_{o,m}$ ) of the two coals is 0.98% and 2.73% that  
115 belongs to the high-volatile bituminous coal and anthracite respectively, the coal composition of  
116 which varies markedly as shown in Table 1. Macerals are mainly composed of vitrinite of 53.40%  
117 and 66.80%, part of inertinite of 19.70% and 14.40%, less exinite of 0.37% and 0% and  
118 well-developed minerals of 26.50% and 18.80% for sample LHG and sample L-1, respectively.  
119 The proximate analysis shows that the LHG and L-1 coals are having of 35.63% and 17.33% ash  
120 yields, and 0.76% and 7.71% moisture contents respectively.

### 121 **2.2. Methodologies for FIB-SEM and X-ray $\mu$ -CT**

122 Before FIB-SEM imaging, sample preparation was firstly performed. Two cubic samples of  $\sim 0.5$



123 | cm<sub>x</sub>1 cm<sub>x</sub>1 cm were polished using dry emery paper to form a flat surface (as shown in Fig. 1),  
124 | which was then polished by argon ions. The polished coal samples were dried for 12 h at 65 °C  
125 | and then coated with carbon. These two samples were then put into the Zeiss Crossbeam540  
126 | system for imaging. The area of the scanning area is approximately 10 μm<sub>x</sub> 10 μm. In the  
127 | FIB-SEM experiment, the cutting of the focused ion beam is performed simultaneously with the  
128 | imaging of the scanning electron microscope. The acceleration voltage is 1kV during the  
129 | experiment, the current is 0.8 nA, and the test time is 10 hours. A thousand SEM images of each  
130 | coal obtained with resolution of ~10 nm were used to describe the pore network.

131 | Before performing the X-ray μ-CT scanning measurements, two coal pillars with a diameter of  
132 | ~1.0 mm and a height of ~2.0 mm were first drilled. The scan was then carried out using a Nano  
133 | Voxel-3000 X-ray 3D microscope with a 20x lens detector (Sanying Precision Instruments Co., Ltd.,  
134 | China). The scanning area of X-ray μ-CT was a columnar region having a diameter of ~1 mm and  
135 | a height of ~1 mm. The experimental conditions were a voltage of 80 kV and a current of 95 μA.  
136 | Finally, each 3D data set of the two samples includes more than 1000 CT scan images. The  
137 | resolutions of the samples LHG and L-1 were 0.55 μm and 0.63 μm, respectively. The data  
138 | obtained from both experiments were stacked and analyzed by Avizo software as our previous  
139 | study (Li et al., 2017). The porosity was calculated by the *volume fraction* module in Avizo  
140 | software.

### 141 | 2.3. Fractal analysis in coals

142 | Fractal geometry was proposed by Benoit Mandelbrot in 1982, which can be used to effectively  
143 | characterize the heterogeneity of pore structure in porous media with fractal dimension  
144 | (Mandelbrot, 1983). The larger the fractal dimension is, the stronger heterogeneity of the pore

1 145 structure is (Reich et al., 1992). In this work, the fractal dimension was used as the evaluation  
2  
3 146 parameter of heterogeneity. Fractal dimension of pore structure can be determined by the data  
4  
5  
6 147 from mercury intrusion porosimetry (Peng et al., 2017), low-temperature nitrogen adsorption  
7  
8  
9 148 (Mahnke and Mögel, 2003) and related images (e.g. SEM images and CT images) (Liu and Nie,  
10  
11  
12 149 2016; Wu et al., 2019). Several methods based on image calculation (Krohn and Thompson, 1986;  
13  
14  
15 150 Lopes and Betrouni, 2009; Russell et al., 1980) were proposed including the box-counting method,  
16  
17 151 fractional Brownian motion method and area measurement method. In this study, the popular  
18  
19  
20 152 box-counting method will be utilized. The main principle is as follows:

21  
22 153 Firstly, let A be any non-empty bounded subset of the space  $R^n$ . ~~If For any~~  $\delta > 0$ ,  $N_\delta(A)$   
23  
24  
25 154 represents the minimum number of n-dimensional boxes with a side length  $\delta$  required to cover  
26  
27 155 A. When  $\delta \rightarrow 0$ , a relationship exists:

$$28 \quad 29 \quad 30 \quad 31 \quad 156 \quad N_\delta(A) \propto \delta^{-D} \quad (1)$$

32  
33 157 Where  $D$  is the fractal dimension of space A. And when there is only one  $k$ , there is:

$$34 \quad 35 \quad 36 \quad 37 \quad 158 \quad \lim_{\delta \rightarrow 0} \frac{N_\delta(A)}{\delta^{-D}} = k \quad (2)$$

38  
39 159 Take the logarithm of both sides of the equation at the same time, we can acquire:

$$40 \quad 41 \quad 42 \quad 43 \quad 160 \quad \lim_{\delta \rightarrow 0} (\log N_\delta(A) + D \log \delta) = \log k \quad (3)$$

44  
45 161 Which can be a substitute as:

$$46 \quad 47 \quad 48 \quad 49 \quad 162 \quad D = \lim_{\delta \rightarrow 0} \frac{\log k - \log N_\delta(A)}{\log \delta} = - \lim_{\delta \rightarrow 0} \frac{\log N_\delta(A)}{\log \delta} \quad (4)$$

50  
51 163 The side length  $\delta_i$  of the box takes a series of values and counts the number  $N_{\delta_i}(A)$  of boxes  
52  
53 164 required to cover A. The  $[\log \delta_i, \log N_{\delta_i}(A)]$  line is drawn in the coordinate system with  $\log \delta$   
54  
55 165 as the abscissa and  $\log N_{\delta_i}(A)$  as the ordinate. The straight line is fitted by the least square  
56  
57  
58 166 method, and the slope is the fractal dimension  $D$ .

1 167 In this work, the 3D fractal dimension ( $D_3$ ) and 2D fractal dimension ( $D_2$ ) are calculated based on  
2  
3  
4 168 high-resolution FIB-SEM and CT images. In the above algorithm, A is a binarized high-resolution  
5  
6 169 FIB-SEM/CT image with side length of  $M \times M$  or  $M \times M \times M$ . If A cannot be divided by the  
7  
8  
9 170 box with the side length  $\delta$ , the box-counting method will produce areas smaller than  $\delta \times \delta$  (or  
10  
11  
12 171  $\delta \times \delta \times \delta$ ) at the edge of the image. The information contained in these areas will be ignored  
13  
14 172 during the calculation process, which is the boundary effect. To avoid the loss of image  
15  
16  
17 173 information, the common factor of the length and width of the original image is taken as the side  
18  
19  
20 174 length of a series of boxes (Wu et al., 2019). Noise will be generated due to the volatility of the  
21  
22  
23 175 incident electrons during the imaging process. Therefore, the images should be denoised first by  
24  
25  
26 176 the median filtering method. Then, the threshold is determined for the binarized image with the  
27  
28  
29 177 commonly used Otsu algorithm (i.e., the global threshold method) due to its high efficiency,  
30  
31 178 conciseness and remarkable effect (Otsu, 1979; Prakongkep et al., 2010; Zhou and Xie, 2003).  
32  
33  
34 179 Finally, fractal dimension of pores is calculated by the box-counting method. The 3D analysis was  
35  
36  
37 180 conducted with the voxels of  $500 \times 500 \times 500$  when calculating spatial fractal  $D_3$ . Due to the  
38  
39  
40 181 limitation of the computer's operating performance (the larger the size, the better the computer's  
41  
42  
43 182 operating performance is needed), and the need to avoid the impact of other variables caused by  
44  
45  
46 183 the different sizes, so the size of the selected region is  $500 \times 500 \times 500$  voxels. Besides, the size of  
47  
48  
49 184  $500 \times 500 \times 500$  voxels is sufficient for evaluating the heterogeneity of the pore network in coal  
50  
51  
52 185 samples. To eliminate the inaccurate result caused by the different initialization positions, the  
53  
54  
55 186 domain of the 3D model constructed by different cubes is initialized from 9 locations of eight  
56  
57  
58 187 vertices and the center point of the cube. The size of the cube grows by 10 pixels per time. In other  
59  
60  
61 188 words, if there is a cube with a side length of 500, a total of 450 cubes of different side lengths

1 189 will be produced in 9 different directions. Due to nine cubes are identical, the original cube with a  
2  
3  
4 190 side length of 500 will be divided into 442 different cubes. The average value of the nine  
5  
6 191 directions is deemed as the  $D_3$  of the fractal spatial pore structure of the various box size.  
7  
8  
9 192 Simultaneously, the the 2D fractal dimension of the cube with different sizes is also assessed .  
10  
11  
12 193 Combining the above theories, the box-counting method is automatically programmed based on  
13  
14 194 Matlab software to calculate the fractal dimension. In this work, the spatial fractal of  $D_3$  for pore  
15  
16  
17 195 structure of coals will be discussed in detail.

### 196 **3. Results and Discussions**

#### 197 **3.1. Pore-fracture in 2D morphology**

198 The pore size, type, and structure of coal reservoirs are extremely inconsistent due to the  
199 fundamental differences in plant remains and a series of changes in the process of coalification. In  
200 this study, the pore morphology, structure, and distribution of selected coal samples were  
201 qualitatively described by the argon-ion polishing-SEM technique. Based on pore genesis and  
202 distribution characteristics, matrix pores in coal can be divided into two main types: (1) organic  
203 matter (OM) pores, including stomas and shrinkage pores; and (2) mineral associated (MA) pores,  
204 including intragranular pores in minerals and intergranular pores between crystals and matrix  
205 (Loucks et al., 2012). Using argon-ion polishing-SEM images, it was found that a wide variety of  
206 OM pores and MA pores were developed in the two coal samples, and some micro-scale fractures  
207 | existed (Figs. 4-2 and 23). For the high volatile bituminous coal (sample LHG), a large amount of  
208 gas is produced in the early stage of coalification, and the shapes of pores are mostly round with a  
209 smooth edge. However, due to the higher pressure of the overburden, the pores are compressed,  
210 thereby exhibiting various irregular shapes (including slit-like and wedge shape, as shown in Fig.

211 [2f](#)) and exhibiting a clear directional arrangement (Fig. [2c](#)). Meanwhile, due to the compression  
212 and destruction of the overburden pressure, some of the pores appear connected. Besides, some of  
213 the pores are accompanied by the phenomenon of being filled with minerals (Fig. [2e](#)). Clustered  
214 pores are visible in some areas (Fig. [2f](#)). As the coalification progresses, a large number of pores  
215 are formed in the anthracite L-1, which are round or other irregular shapes and are present in  
216 clusters in the coal matrix (Fig. [2f](#)). Some pores and fractures are filled with minerals (Fig.  
217 [3a-d](#)). Due to fluid erosion, there are erosive pores in the sample (Fig. [3e](#)).

### 218 3.2. Quantitative 3D pore networks

219 [3](#) Fig. [4](#) shows 3D reconstruction images ([a<sub>1</sub>-d<sub>1</sub>](#)) and corresponding pore network ([a<sub>2</sub>-d<sub>2</sub>](#))  
220 extracted with Avizo software. In the images on the left, black is pore-fracture, gray is coal  
221 matrix and white is mineral. On the right, blue is the extracted pore network. Both reconstruction  
222 blocks have a dimension of  $10\ \mu\text{m} \times 10\ \mu\text{m} \times 10\ \mu\text{m}$  by FIB-SEM data. The data volume sizes of  
223 the X-ray  $\mu\text{CT}$  experiments are  $275\ \mu\text{m} \times 275\ \mu\text{m} \times 275\ \mu\text{m}$  and  $315\ \mu\text{m} \times 315\ \mu\text{m} \times 315\ \mu\text{m}$ ,  
224 respectively. For the FIB-SEM experimental data set, the area of characterization is small and the  
225 computer running performance is not high when the algorithm is running. Therefore, the 1000  
226 slices obtained from the experiment were applied to 3D reconstruction to completely restore the  
227 pore network characteristics at the nanoscale. For the CT experiment, the area of its  
228 characterization is relatively large, and the data set of more than 1000 slices is too high for  
229 computer performance. Therefore, the uniform characterization size selected here is  $500 \times 500 \times$   
230  $500$  voxels, which can better display the three-dimensional distribution characteristics of the pore  
231 network at the micrometer scale. Quantitative characterization of the pore network was performed  
232 by the Avizo software, as shown in Table 2. The porosities of sample LHG and sample L-1 at

1 233 different scales were 5.23% and 1.06% for FIB-SEM, 20.41% and 8.67% for X-ray  $\mu$ CT,  
2  
3  
4 234 respectively. The mesopores are the most developed in FIB-SEM data, while the macropores and  
5  
6 235 super-macropores are extensive development in the CT data, resulting in the calculated porosity of  
7  
8  
9 236 the FIB-SEM data in the same sample being lower than that calculated from the CT data. ~~Fig. 4~~Fig.  
10  
11 237 ~~5~~ shows the 3D spatial distribution of the pore network in different ranges of the two samples. ~~Fig.~~  
12  
13 238 ~~4~~ and suggests that the 3D spatial pore network has obvious heterogeneity. Besides, X-ray  $\mu$ CT  
14  
15 239 shows a larger number of pore-fractures than the FIB-SEM. The FIB-SEM data for LHG and L-1  
16  
17 240 in Table 2 showed the pore numbers of 36712 and 11762, the total pore areas of 2105.45  $\mu\text{m}^2$  and  
18  
19 241 515.33  $\mu\text{m}^2$ , and the total pore volumes of 51.63  $\mu\text{m}^3$  and 10.56  $\mu\text{m}^3$ , respectively. This result  
20  
21 242 indicates that the LHG can provide more storage volume for methane than that of the L-1. The  
22  
23 243 X-ray  $\mu$ CT data for LHG and L-1 showed the pore numbers of 180977 and 198822, the total pore  
24  
25 244 area of 8685787.31  $\mu\text{m}^2$  and 5760660.30  $\mu\text{m}^2$ , and the total pore volume of 4114728.90  $\mu\text{m}^3$  and  
26  
27 245 2354981.18  $\mu\text{m}^3$ , respectively. And the two samples have well developed 2811 and 177  
28  
29 246 micro-fractures respectively, which should be the essential seepage channel for CBM. In other  
30  
31 247 words, LHG has a better percolation ability than the sample L-1. ~~Fig. 5~~Fig. 6 depicts the pore  
32  
33 248 distribution and volume percentage in different ranges. For the FIB-SEM (~~Fig. 5~~Fig. 6a and 65c),  
34  
35 249 the pore sizes exhibit bimodal distribution. The peaks of LHG and L-1 are located at 10 nm - 20  
36  
37 250 nm and 300 nm - 500 nm, 20 nm - 30 nm and 300 nm - 500 nm, respectively. Also, in the two  
38  
39 251 samples, the pores with the range of 300-500 nm contributed the most to the porosity at the  
40  
41 252 nanometer scale. For the X-ray  $\mu$ CT, the pore size distribution of the LHG presents a three-peak  
42  
43 253 characteristic (~~Fig. 5~~Fig. 6b) with three peaks around 0.5  $\mu\text{m}$  - 0.7  $\mu\text{m}$ , 1  $\mu\text{m}$  - 2  $\mu\text{m}$  and 9  $\mu\text{m}$  - 10  
44  
45 254  $\mu\text{m}$ . Moreover, the pores with sizes of 1  $\mu\text{m}$  - 2  $\mu\text{m}$ , 11  $\mu\text{m}$  - 12  $\mu\text{m}$ , 15  $\mu\text{m}$  - 20  $\mu\text{m}$  contribute  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65

1 255 more to the microscale porosity. The pore size distribution of L-1 shows a bimodal structure (Fig.  
2  
3 256 ~~Fig. 6d~~) with two peaks at 0.7  $\mu\text{m}$  - 0.9  $\mu\text{m}$  and 1  $\mu\text{m}$  - 2  $\mu\text{m}$ . And the pores of 3  $\mu\text{m}$  - 4  $\mu\text{m}$   
4  
5  
6 257 contribute most to microscale porosity.

7  
8  
9 258 The pore networks are established with the Avizo software , and the 3D pore throat structures are  
10  
11 259 displayed and quantified as shown in ~~Fig. 6~~Fig. 7 and Table 3. The two FIB-SEM data volumes  
12  
13  
14 260 used here is still 10  $\mu\text{m}$   $\times$  10  $\mu\text{m}$   $\times$  10  $\mu\text{m}$ . With the X-ray  $\mu\text{CT}$  data, the analyzed volumes were  
15  
16  
17 261 110  $\mu\text{m}$   $\times$  110  $\mu\text{m}$   $\times$  110  $\mu\text{m}$  for LHG and 126  $\mu\text{m}$   $\times$  126  $\mu\text{m}$   $\times$  126  $\mu\text{m}$  for L-1. Because if the  
18  
19  
20 262 original voxel size is used, it is not conducive to further observation of pore throat characteristics.

21  
22 263 The analysis parameters including counts, area, average channel length, total channel length and  
23  
24  
25 264 volume vary markedly as shown in Table 3. The throats of the LHG are well developed as

26  
27  
28 265 presented in ~~Fig. 6~~Fig. 7 a<sub>1</sub> and b<sub>1</sub>, and the pore-fractures are well connected through the throat.

29  
30  
31 266 ~~Fig 6a<sub>2</sub>~~7a<sub>2</sub>, b<sub>2</sub> with Table 3 show that the pore throats in the range of 100 nm – 200 nm and 3000  
32  
33  
34 267 nm – 4000 nm contribute the most to the seepage pore network of the LHG. In contrast, the throats

35  
36  
37 268 of L-1 develop locally at the nanoscale as shown in Fig 7c<sub>1</sub>. ~~Fig. 6~~Fig. 7c<sub>2</sub> and Table 3 exhibit  
38  
39 269 that the pore throats in the range of 100 nm – 200 nm dominate the seepage network of the L-1.

40  
41  
42 270 However, L-1 develops fewer throats at the microscale as shown in ~~Fig. 6~~Fig. 7d, and the pores  
43  
44  
45 271 are isolated. Therefore, the LHG should have a better permeability than that of L-1.

### 272 3.3. Pore heterogeneity by fractal dimension

46  
47  
48  
49  
50 273 The  $D_3$  results calculated based on the box-counting method (Liu and Nie, 2016; Wu et al., 2019)  
51  
52 274 are presented in ~~Fig. 7~~Fig. 8, which indicates that  $D_3$  floats within a certain size range, but remains

53  
54  
55  
56 275 essentially unchanged if the calculation domain size exceeds a critical value. To determine the  
57  
58  
59 276 critical value, the first derivative by the function of  $D_3$  varies with increasing computation domain

1 277 size was evaluated. The point that first approaches 0 after the first derivative undergoes a  
2  
3 278 significant change is defined as a turning point, which is expressed as  $D_3$  almost stops growing  
4  
5  
6 279 from this point. The critical value determined by the fractal dimension is referred to as the  
7  
8  
9 280 representative elementary volume (REV) (Wu et al., 2019), and the fractal dimension value of the  
10  
11 281 REV will represent the fractal characteristics of the sample. As shown in ~~Fig. 7~~Fig. 8, the side  
12  
13  
14 282 lengths of the REV of the four data sets (sample LHG of FIB-SEM, sample L-1 of FIB-SEM,  
15  
16  
17 283 samples LHG and L-1 of CT) are 80, 280, 100 and 100 pixels, the corresponding  $D_3$  are 2.23, 2.04,  
18  
19  
20 284 2.69 and 2.51, respectively. REV demonstrates that the pore networks of the selected coals have  
21  
22  
23 285 self-similarity. Simultaneously, the spatial pore networks of the two coals are complex, and the  
24  
25  
26 286 heterogeneity of the LHG is stronger.

27  
28 287 For the same coal, the FIB-SEM and the X-ray  $\mu$ -CT images represent two different scales, that is,  
29  
30  
31 288 nanoscale and microscale. The image resolution of the FIB-SEM is 10 nm/pixel, and the image  
32  
33  
34 289 resolutions of the X-ray  $\mu$ -CT are 0.55  $\mu$ m/pixel for LHG and 0.63  $\mu$ m / pixel for L-1, respectively.  
35  
36  
37 290 The smallest box size in the box-counting method is  $100 \times 100 \times 100 \text{ nm}^3$  and  $5.5/6.3 \times 5.5/6.3 \times$   
38  
39 291  $5.5/6.3 \text{ }\mu\text{m}^3$ , respectively. ~~Fig. 7~~Fig. 8 shows the existence of REV at both the nanoscale and  
40  
41  
42 292 microscale; that is, the self-similarity pattern has been built at the nanoscale before the self-similar  
43  
44  
45 293 model is formed at the microscale. Therefore, the pore network is not an isolated development but  
46  
47  
48 294 a secondary development.

49  
50 295 Besides,  $D_2$  has a very significant linear relationship with  $D_3$  as shown in ~~Fig. 8~~Fig. 9, which is  
51  
52  
53 296 very close to  $D_3 = D_2 + 1$  when the porosity is 100% as proven by Wu et al. (2019). The reason for  
54  
55  
56 297 some errors may be that the pore network-fracture system in the coal reservoir has mineral filling  
57  
58  
59 298 or sedimentation during development, which deviates from the original state. The realistic  
60  
61  
62  
63  
64  
65



1 299 relationship between the porosity and three-dimensional fractal dimension is shown in ~~Fig. 9~~Fig.  
2  
3 300 10, which may be due to the pore network in the coal reservoir having mineral filling. Therefore,  
4  
5  
6 301 two different trends have emerged. ~~Fig. 9~~Fig. 10b shows that the porosity increases with  
7  
8  
9 302 increasing  $D_3$ ; that is, the porosity of L-1 in FIB-SEM increases as the spatial complexity of pore  
10  
11  
12 303 network increases. ~~Fig. 9~~Fig. 10a, c, and d display that the porosity decreases with the increasing  
13  
14 304  $D_3$ . The positive trend should be closely related to the complex pore structure. The more complex  
15  
16  
17 305 the pore structure is, the higher the porosity is. The negative correlation should be contributed to a  
18  
19  
20 306 large amount of mineral filling pores. Pores filled with minerals will increase the proportion of  
21  
22  
23 307 small pores and decrease the porosity, which increases the spatial complexity of the pore networks.  
24  
25  
26 308 Therefore, the  $D_3$  increases.

#### 27 28 309 **4. Conclusions**

29  
30  
31 310 In this work, FIB-SEM and X-ray  $\mu$ CT techniques with fractal methods provided a synergistic  
32  
33  
34 311 multiscale and multidimensional evaluation of pore networks. The 3D pore networks and their  
35  
36  
37 312 quantitative analysis of the LHG and L-1 coals were carefully carried out. Additionally, the  
38  
39  
40 313 box-counting method is adopted to acquire the three dimensional complexity ( $D_3$ ) of the pore  
41  
42  
43 314 networks, which can quantitatively evaluate the spatial structure of the pore networks. Moreover,  
44  
45  
46 315 factor affecting the complexity of the pore networks including minerals, pore size and porosity  
47  
48  
49 316 were found. Therefore, the following conclusions can be made:

50  
51 317 1) With the images of FIB-SEM and X-ray  $\mu$ -CT, the pore size distribution and porosity of the  
52  
53  
54 318 selected two coals at different scales is determined. The pore size distribution indicates that pores  
55  
56  
57 319 in the main size range of 300-500 nm, 1  $\mu$ m – 2  $\mu$ m, 11  $\mu$ m – 12  $\mu$ m, and 15  $\mu$ m – 20  $\mu$ m  
58  
59 320 contribute significantly to the porosity of the LHG; for the L-1, pores in the range of 300-500 nm  
60  
61  
62  
63  
64  
65

1 321 and 3  $\mu\text{m}$  – 4  $\mu\text{m}$  contribute most to porosity, which vary markedly. The porosities of LHG and  
2  
3 322 L-1 at different scales are 5.23% and 1.06% for FIB-SEM, 20.41% and 8.67% for X-ray  $\mu\text{CT}$ ,  
4  
5  
6 323 respectively, which indicates that the LHG can provide more storage volume for CBM than that of  
7  
8  
9 324 the L-1.

10  
11 325 2) The spatial pore networks and the pore throat are well established, which shows that the LHG  
12  
13 326 has both well developed nanoscale and microscale pores. Whereas the L-1 locally develops a  
14  
15  
16  
17 327 small number of throats at the nanometer scale, and no throat at the micrometer scale. Therefore,  
18  
19  
20 328 the LHG should have a better permeability than that of L-1.

21  
22 329 3) Based on the box-counting method,  $D_3$  values of four data sets (the LHG for FIB-SEM, the L-1  
23  
24  
25 330 for FIB-SEM, the LHG for CT and the L-1 for CT) are 2.23, 2.04, 2.69 and 2.51, respectively,  
26  
27  
28 331 which demonstrates that the spatial pore networks of the selected coals have self-similarity with a  
29  
30  
31 332 secondary development. Porosity affecting the complexity of the pore networks was found that for  
32  
33  
34 333 the relationship between porosity and  $D_3$ , two opposite trends exist considering the complex pore  
35  
36  
37 334 structure and a large amount of mineral filling pores.

38  
39 335

#### 40 41 42 336 **Acknowledgements**

43  
44  
45 337 This research was funded by the National Natural Science Foundation of China (grant nos.  
46  
47  
48 338 41830427, 41922016, and 41772160) and the Fundamental Research Funds for Central  
49  
50  
51 339 Universities (grant no. 2652018002).

52  
53 340

#### 54 55 341 **References**

56  
57  
58 342 Balucan, R.D., Turner, L.G., Steel, K.M., 2018. X-ray  $\mu\text{CT}$  investigations of the effects of cleat  
59  
60  
61  
62  
63  
64  
65

1 343 demineralization by HCl acidizing on coal permeability. *J. Nat. Gas. Sci. Eng.* 55, 206-218.  
2  
3 344 Cai, Y.D., Li, Q., Liu, D.M., Zhou, Y.F., Lv, D.W., 2018. Insights into matrix compressibility of coals  
4  
5  
6 345 by mercury intrusion porosimetry and N<sub>2</sub> adsorption. *Int. J. Coal Geol.* 200, 199-212.  
7  
8  
9 346 Cai, Y.D., Liu, D.M., Pan, Z.J., Yao, Y.B., Li, J.Q., Qiu, Y.K., 2013. Pore structure and its impact on  
10  
11 347 CH<sub>4</sub> adsorption capacity and flow capability of bituminous and subbituminous coals from  
12  
13 348 Northeast China. *Fuel* 103, 258-268.  
14  
15  
16  
17 349 Clarkson, C.R., Bustin, R.M., 1999. Effect of pore structure and gas pressure upon the transport  
18  
19 350 properties of coal: a laboratory and modeling study. 1. Isotherms and pore volume distributions.  
20  
21 351 *Fuel* 78, 1333-1344.  
22  
23  
24  
25 352 Crosdale, P.J., Beamish, B.B., Valix, M., 1998. Coalbed methane sorption related to coal composition.  
26  
27 353 *Int. J. Coal Geol.* 35, 147-158.  
28  
29  
30  
31 354 Fang, H.H., Sang, S.X., Liu, S.Q., Du, Y., 2019. Methodology of three-dimensional visualization and  
32  
33 355 quantitative characterization of nanopores in coal by using FIB-SEM and its application with  
34  
35  
36 356 anthracite in Qinshui basin. *J. Pet. Sci. Eng.* 182, [1-11](#).  
37  
38  
39 357 Gan, H., Nandi, S.P., Walker Jr, P.L., 1972. Nature of the porosity in American coals. *Fuel* 51, 272-277.  
40  
41  
42 358 Hemes, S., Desbois, G., Urai, J.L., Schröppel, B., Schwarz, J.-O., 2015. Multi-scale characterization of  
43  
44 359 porosity in Boom Clay (HADES-level, Mol, Belgium) using a combination of X-ray  $\mu$ -CT, 2D  
45  
46 360 BIB-SEM and FIB-SEM tomography. *Micropor. Mesopor. Mat.* 208, 1-20.  
47  
48  
49  
50 361 Jiao, K., Yao, S.P., Liu, C., Gao, Y.Q., Wu, H., Li, M.C., Tang, Z.Y., 2014. The characterization and  
51  
52 362 quantitative analysis of nanopores in unconventional gas reservoirs utilizing FESEM-FIB and  
53  
54 363 image processing: An example from the lower Silurian Longmaxi Shale, upper Yangtze region,  
55  
56 364 China. *Int. J. Coal Geol.* 128, 1-11.  
57  
58  
59  
60  
61  
62  
63  
64  
65

1 365 Karacan, C.Ö., Ruiz, F.A., Cote, M., Phipps, S., 2011. Coal mine methane: A review of capture and  
2  
3 366 utilization practices with benefits to mining safety and to greenhouse gas reduction. *Int. J. Coal*  
4  
5  
6 367 *Geol.* 86, 121-156.  
7  
8  
9 368 Krohn, C.E., Thompson, A.H., 1986. Fractal Sandstone Pores - Automated Measurements Using  
10  
11 369 Scanning-Electron-Microscope Images. *Phys. Rev B.* 33, 6366-6374.  
12  
13  
14 370 Li, Z.T., Liu, D.M., Cai, Y.D., Ranjith, P.G., Yao, Y.B., 2017. Multi-scale quantitative characterization  
15  
16  
17 371 of 3-D pore-fracture networks in bituminous and anthracite coals using FIB-SEM tomography and  
18  
19  
20 372 X-ray  $\mu$ -CT. *Fuel* 209, 43-53.  
21  
22  
23 373 Liu, S.Q., Sang, S.X., Wang, G., Ma, J.S., Wang, X., Wang, W.F., Du, Y., Wang, T., 2017. FIB-SEM  
24  
25 374 and X-ray CT characterization of interconnected pores in high-rank coal formed from regional  
26  
27  
28 375 metamorphism. *J. Pet. Sci. Eng.* 148, 21-31.  
29  
30  
31 376 Liu, X.F., Nie, B.S., 2016. Fractal characteristics of coal samples utilizing image analysis and gas  
32  
33 377 adsorption. *Fuel* 182, 314-322.  
34  
35  
36 378 Lopes, R., Betrouni, N., 2009. Fractal and multifractal analysis: A review. *Med. Image. Anal.* 13,  
37  
38  
39 379 634-649.  
40  
41  
42 380 Loucks, R.G., Reed, R.M., Ruppel, S.C., Hammes, U., 2012. Spectrum of pore types and networks in  
43  
44  
45 381 mudrocks and a descriptive classification for matrix-related mudrock pores. *AAPG Bull.* 96,  
46  
47  
48 382 1071-1098.  
49  
50  
51 383 Mahnke, M., Mögel, H.J., 2003. Fractal analysis of physical adsorption on material surfaces. *Colloids.*  
52  
53 384 *Surfaces. A.* 216, 215-228.  
54  
55  
56 385 Mandelbrot, B.B., 1983. The Fractal Geometry of Nature. *Sciences* 23, 63-68.  
57  
58  
59 386 Mastalerz, M., He, L., Melnichenko, Y.B., Rupp, J.A., 2012. Porosity of Coal and Shale: Insights from  
60  
61  
62  
63  
64  
65

1 387 Gas Adsorption and SANS/USANS Techniques. *Energ. Fuel.* 26, 5109-5120.

2

3 388 Mathews, J.P., Campbell, Q.P., Xu, H., Halleck, P., 2017. A review of the application of X-ray

4

5

6 389 computed tomography to the study of coal. *Fuel* 209, 10-24.

7

8

9 390 Nakagawa, T., Komaki, I., Sakawa, M., Nishikawa, K., 2000. Small angle X-ray scattering study on

10

11 391 change of fractal property of Witbank coal with heat treatment. *Fuel* 79, 1341-1346.

12

13

14 392 Okolo, G.N., Everson, R.C., Neomagus, H.W.J.P., Roberts, M.J., Sakurovs, R., 2015. Comparing the

15

16

17 393 porosity and surface areas of coal as measured by gas adsorption, mercury intrusion and SAXS

18

19

20 394 techniques. *Fuel* 141, 293-304.

21

22

23 395 Otsu, N., 1979. A Threshold Selection Method from Gray-Level Histograms. *IEEE . T. Syst. Man. Cy.*

24

25 396 9, 62-66.

26

27

28 397 Pan, J., Wang, K., Hou, Q., Niu, Q., Wang, H., Ji, Z., 2016. Micro-pores and fractures of coals analysed

29

30

31 398 by field emission scanning electron microscopy and fractal theory. *Fuel* 164, 277-285.

32

33

34 399 Peng, C., Zou, C.C., Yang, Y.Q., Zhang, G.H., Wang, W.W., 2017. Fractal analysis of high rank coal

35

36 400 from southeast Qinshui basin by using gas adsorption and mercury porosimetry. *J. Pet. Sci. Eng.*

37

38

39 401 156, 235-249.

40

41

42 402 Pillalamarry, M., Harpalani, S., Liu, S.M., 2011. Gas diffusion behavior of coal and its impact on

43

44

45 403 production from coalbed methane reservoirs. *Int. J. Coal Geol.* 86, 342-348.

46

47

48 404 Prakongkep, N., Suddhiprakarn, A., Kheoruenromne, I., Gilkes, R.J., 2010. SEM image analysis for

49

50 405 characterization of sand grains in Thai paddy soils. *Geoderma* 156, 20-31.

51

52

53 406 Reich, M.H., Snook, I.K., Wagenfeld, H.K., 1992. A fractal interpretation of the effect of drying on the

54

55

56 407 pore structure of Victorian brown coal. *Fuel* 71, 669-672.

57

58

59 408 Rigby, S.P., Chigada, P.I., Evbuomvan, I.O., Chudek, J.A., Miri, T., Wood, J., Bakalis, S., 2008.

60

61

62

63

64

65

1 409 Experimental and modelling studies of the kinetics of mercury retraction from highly confined  
2  
3 410 geometries during porosimetry in the transport and the quasi-equilibrium regimes. Chem. Eng. Sci.  
4  
5  
6 411 63, 5771-5788.  
7  
8  
9 412 Russell, D.A., Hanson, J.D., Ott, E., 1980<sup>b</sup>. Dimension of strange attractors. Phys. Rev. Lett. 45,  
10  
11  
12 413 1175–1178.  
13  
14 414 Saif, T., Lin, Q.Y., Butcher, A.R., Bijeljic, B., Blunt, M.J., 2017. Multi-scale multi-dimensional  
15  
16  
17 415 microstructure imaging of oil shale pyrolysis using X-ray micro-tomography, automated ultra-high  
18  
19  
20 416 resolution SEM, MAPS Mineralogy and FIB-SEM. Appl. Energ. 202, 628-647.  
21  
22  
23 417 Sakurovs, R., He, L.L., Melnichenko, Y.B., Radlinski, A.P., Blach, T., Lemmel, H., Mildner, D.F.R.,  
24  
25  
26 418 2012. Pore size distribution and accessible pore size distribution in bituminous coals. Int. J. Coal  
27  
28  
29 419 Geol. 100, 51-64.  
30  
31 420 Sakurovs, R., Koval, L., Grigore, M., Sokolova, A., Ruppert, L.F., Melnichenko, Y.B., 2018.  
32  
33  
34 421 Nanometre-sized pores in coal: Variations between coal basins and coal origin. Int. J. Coal Geol.  
35  
36  
37 422 186, 126-134.  
38  
39 423 Silin, D., Kneafsey, T., 2012. Shale Gas: Nanometer-Scale Observations and Well Modelling. J. Can.  
40  
41  
42 424 Petrol. Technol. 51, 464-475.  
43  
44  
45 425 Tang, X.L., Jiang, Z.X., Jiang, S., Li, Z., 2016. Heterogeneous nanoporosity of the Silurian Longmaxi  
46  
47  
48 426 Formation shale gas reservoir in the Sichuan Basin using the QEMSCAN, FIB-SEM, and  
49  
50  
51 427 nano-CT methods. Mar. Petrol. Geol. 78, 99-109.  
52  
53  
54 428 Vishal, V., Singh, T.N., Ranjith, P.G., 2015. Influence of sorption time in CO<sub>2</sub>-ECBM process in Indian  
55  
56  
57 429 coals using coupled numerical simulation. Fuel 139, 51-58.  
58  
59  
60 430 Wargo, E.A., Kotaka, T., Tabuchi, Y., Kumbur, E.C., 2013. Comparison of focused ion beam versus  
61  
62  
63  
64  
65

1 431 nano-scale X-ray computed tomography for resolving 3-D microstructures of porous fuel cell  
2  
3 432 materials. *J. Power. Sources.* 241, 608-618.  
4  
5  
6 433 Warren, J.E., Root, P.J., 1963. The Behavior of Naturally Fractured Reservoirs. SPE-426-PA 3,  
7  
8 434 245-255.  
9  
10  
11 435 Weishauptová, Z., Medek, J., Kovář, L., 2004. Bond forms of methane in porous system of coal II. *Fuel*  
12  
13 436 83, 1759-1764.  
14  
15  
16  
17 437 Wu, H., Zhou, Y.F., Yao, Y.B., Wu, K.J., 2019. Imaged based fractal characterization of micro-fracture  
18  
19 438 structure in coal. *Fuel* 239, 53-62.  
20  
21  
22 439 Zheng, S.J., Yao, Y.B., Liu, D.M., Cai, Y.D., Liu, Y., 2018. Characterizations of full-scale pore size  
23  
24 440 distribution, porosity and permeability of coals: A novel methodology by nuclear magnetic  
25  
26 441 resonance and fractal analysis theory. *Int. J. Coal Geol.* 196, 148-158.  
27  
28  
29 442 Zhou, H.W., Xie, H., 2003. Direct estimation of the fractal dimensions of a fracture surface of rock.  
30  
31 443 *Surf. Rev. Lett.* 10, 751-762.  
32  
33  
34  
35  
36 444 Zhou, H.W., Zhong, J.C., Ren, W.G., Wang, X.Y., Yi, H.Y., 2018. Characterization of pore-fracture  
37  
38 445 networks and their evolution at various measurement scales in coal samples using X-ray mu CT  
39  
40 446 and a fractal method. *Int. J. Coal Geol.* 189, 35-49.  
41  
42  
43  
44  
45 447  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65

1 448 **Captions for Figures and Tables**

2  
3 449 Fig. 1. Pictures of samples used in FIB-SEM experiments. (a) is a front view and (b) is a top view.

4  
5  
6 450 Fig. ~~1~~2. The pore-fracture morphology of the sample LHG. (a) and (b) observe the pore-fracture  
7  
8  
9 451 distribution and morphology of the sample from a large viewing angle. (c) exhibits a directional  
10  
11  
12 452 alignment and some irregularly shaped pores; (d) shows irregular pores; (e) presents the phenomenon  
13  
14  
15 453 of mineral filling and partially connected pores; (f) shows the clustered pores.

16  
17 454 Fig. ~~2~~3. The pore-fracture morphology of the sample L-1. (a) and (b) observe the fractures  
18  
19  
20 455 distribution, morphology and some fractures filled with mineral. (c) and (d) exhibits pores of different  
21  
22  
23 456 shapes and filled with mineral; (e) presents fluid erosion pores; (f) shows the clustered pores.

24  
25 457 Fig. ~~3~~4. 3D reconstruction images (a<sub>1</sub>-d<sub>1</sub>) and corresponding extracted pore-fracture system (a<sub>2</sub>-d<sub>2</sub>)  
26  
27  
28 458 by Avizo2019 : (a<sub>1</sub>), (a<sub>2</sub>) - FIB-SEM data of sample LHG; (b<sub>1</sub>), (b<sub>2</sub>) - X-ray  $\mu$ CT data of sample LHG;  
29  
30  
31 459 (c<sub>1</sub>), (c<sub>2</sub>) - FIB-SEM data of sample L-1; (d<sub>1</sub>), (d<sub>2</sub>) - X-ray  $\mu$ CT data of sample L-1. In the images on the  
32  
33  
34 460 left, black is pore-fracture, gray is the coal matrix, and white is mineral. On the right, blue is the  
35  
36  
37 461 extracted pore network.

38  
39 462 Fig. ~~4~~5. 3D spatial distribution of pore-fraction system in different ranges. a<sub>1</sub>-a<sub>3</sub>: FIB-SEM data of  
40  
41  
42 463 sample LHG; b<sub>1</sub>-b<sub>3</sub>: X-ray  $\mu$ CT data of sample LHG; c<sub>1</sub>-c<sub>3</sub>: FIB-SEM data of sample L-1; d<sub>1</sub>-d<sub>3</sub>: X-ray  
43  
44  
45 464  $\mu$ CT data of sample L-1.

46  
47 465 Fig. ~~5~~6. Histogram depicting results of pore distribution and volume percentage in different ranges.  
48  
49  
50 466 (a): FIB-SEM data of sample LHG; (b): X-ray  $\mu$ CT data of sample LHG; (c): FIB-SEM data of sample  
51  
52  
53 467 L-1; (d): X-ray  $\mu$ CT data of sample L-1.

54  
55 468 Fig. ~~6~~7. Pore network model showing 3D pore-throat skeletal structure and distribution of throats.  
56  
57  
58 469 a<sub>1</sub>-a<sub>2</sub>: FIB-SEM data of sample LHG; b<sub>1</sub>-b<sub>2</sub>: X-ray  $\mu$ CT data of sample LHG; c<sub>1</sub>-c<sub>2</sub>: FIB-SEM data of  
59  
60  
61  
62  
63  
64  
65



1 470 sample L-1; d: X-ray  $\mu$ CT data of sample L-1.

2  
3 471 ~~Fig. 7~~Fig. 8. The relationship between the three-dimensional fractal dimension ( $D_3$ ) and box size. (a<sub>1</sub>) -  
4  
5  
6 472 (d<sub>1</sub>) is the trend of  $D_3$  with the box size. It indicates that  $D_3$  floats within a certain size range, but  
7  
8  
9 473 remains essentially unchanged if the calculation domain size exceeds a critical value. (a<sub>2</sub>) - (d<sub>2</sub>) is the  
10  
11  
12 474 first derivative of the left curve, which is used to characterize the rate of change of  $D_3$ . The point that  
13  
14  
15 475 first approaches 0 after the first derivative undergoes a significant change is defined as a turning point,  
16  
17  
18 476 which is expressed as  $D_3$  almost stops growing from this point.

19  
20 477 ~~Fig. 8~~Fig. 9 The relationship between two-dimensional ( $D_2$ ) fractal dimension and three-dimensional  
21  
22  
23 478 fractal dimension ( $D_3$ ). It is found that the two-dimensional fractal dimension has a very significant  
24  
25  
26 479 linear relationship with the three-dimensional fractal dimension.

27  
28 480 ~~Fig. 9~~Fig. 10. Relationship between three-dimensional fractal dimension and porosity. (b) shows that  
29  
30  
31 481 the porosity increases with increasing  $D_3$ ; that is, the porosity of sample L-1 increases as the  
32  
33  
34 482 three-dimensional spatial distribution complexity of pore-fracture system increases. (a) (c) and (d)  
35  
36  
37 483 display that the porosity decreases with the rise of  $D_3$ .

38  
39 484 Table 1 Sample information and basic parameters of the selected Chinese coals

40  
41  
42 485 Table 2 Pore size distribution characteristics of the pore-fracture system for the selected coals

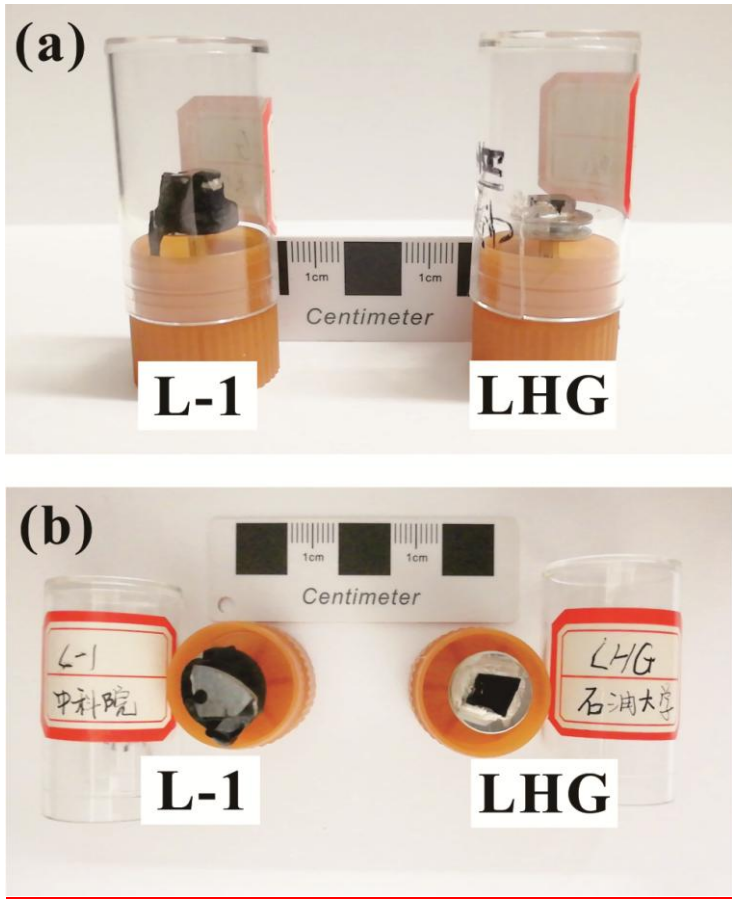
43  
44  
45 486 Table 3 Pore throat parameter information calculated by the PNM module in Avizo

46  
47 487

48  
49 488

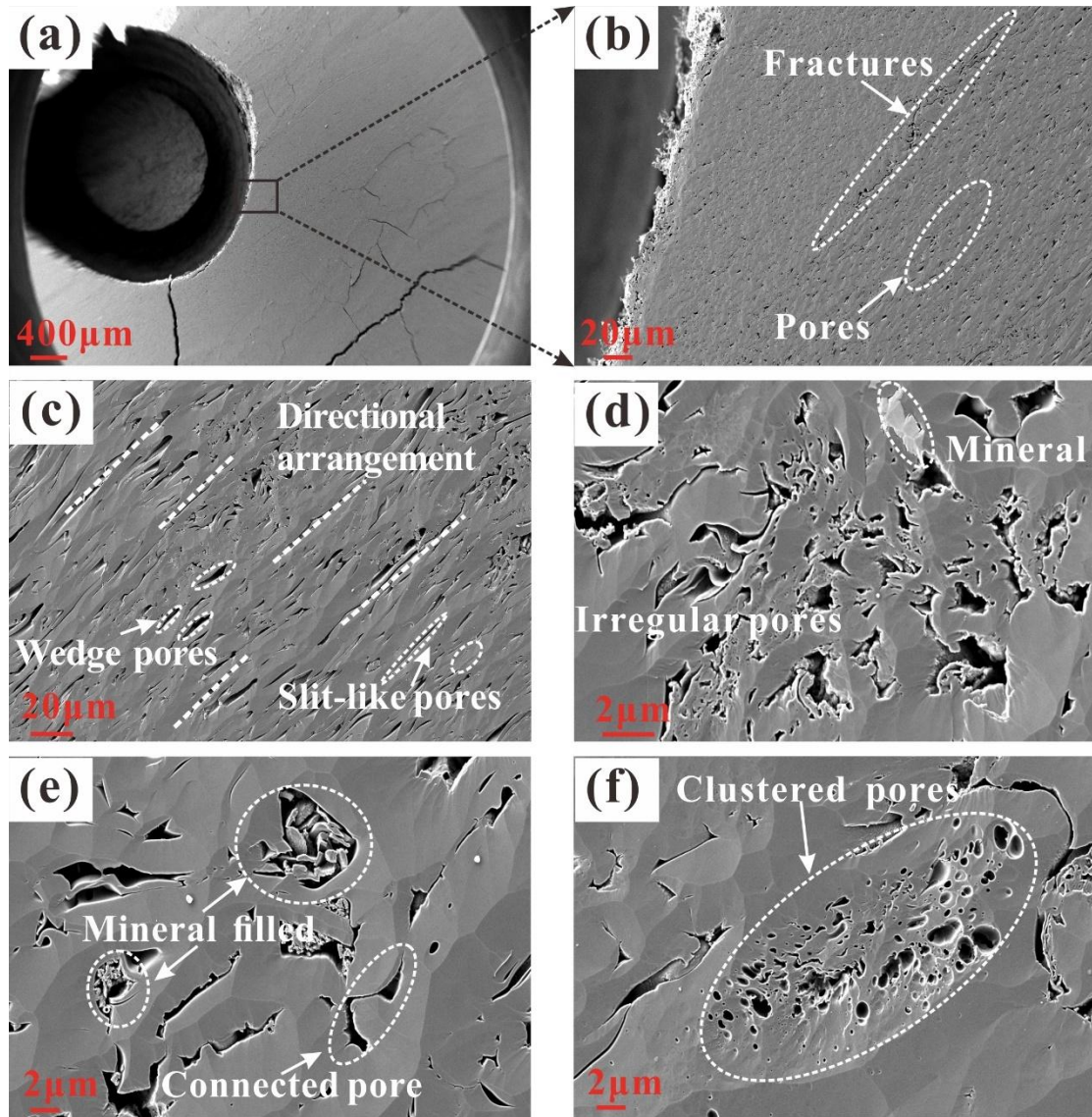
50  
51 489

1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65

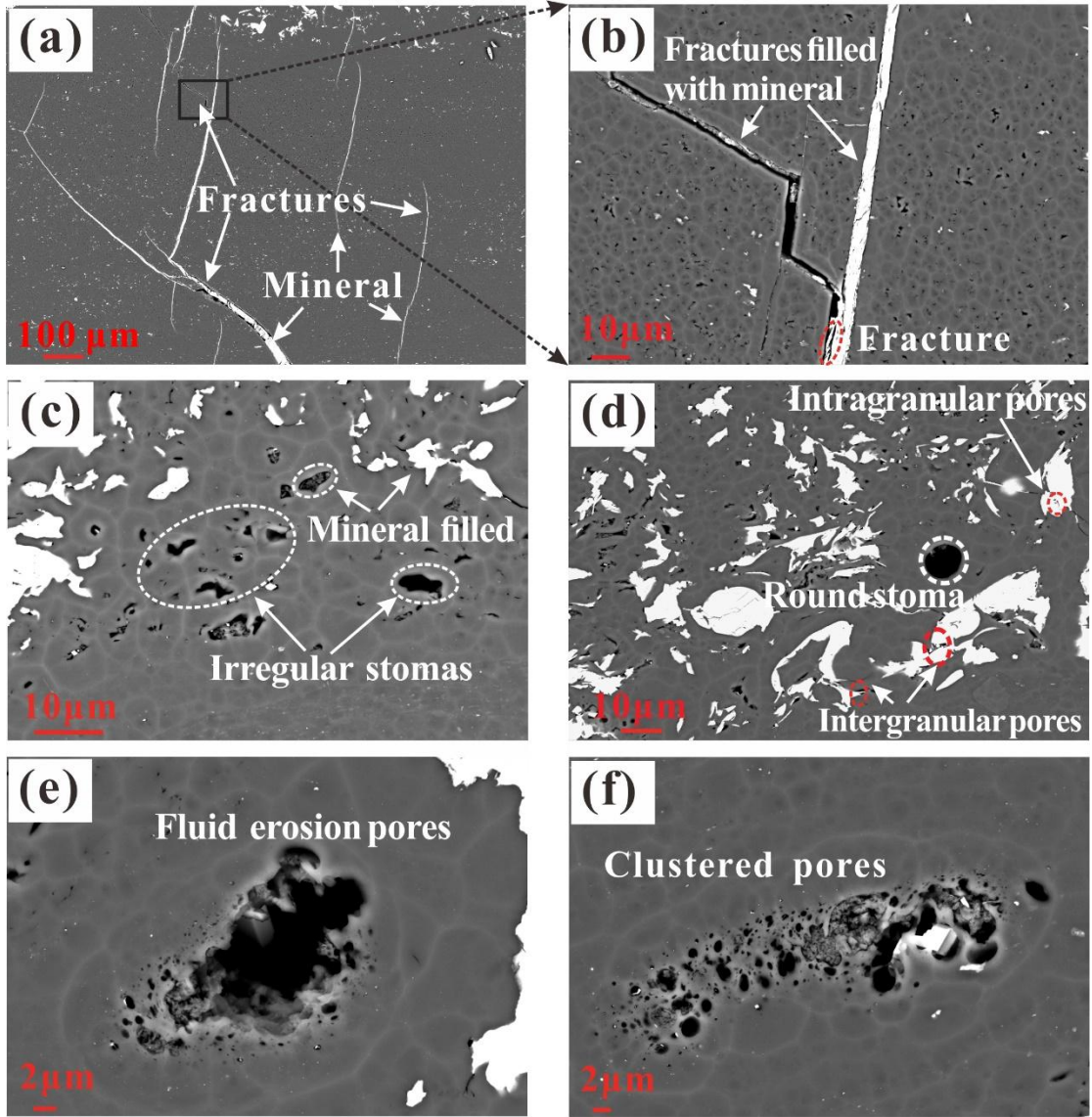


490  
491  
492

Fig. 1. Pictures of samples used in FIB-SEM experiments. (a) is a front view and (b) is a top view.



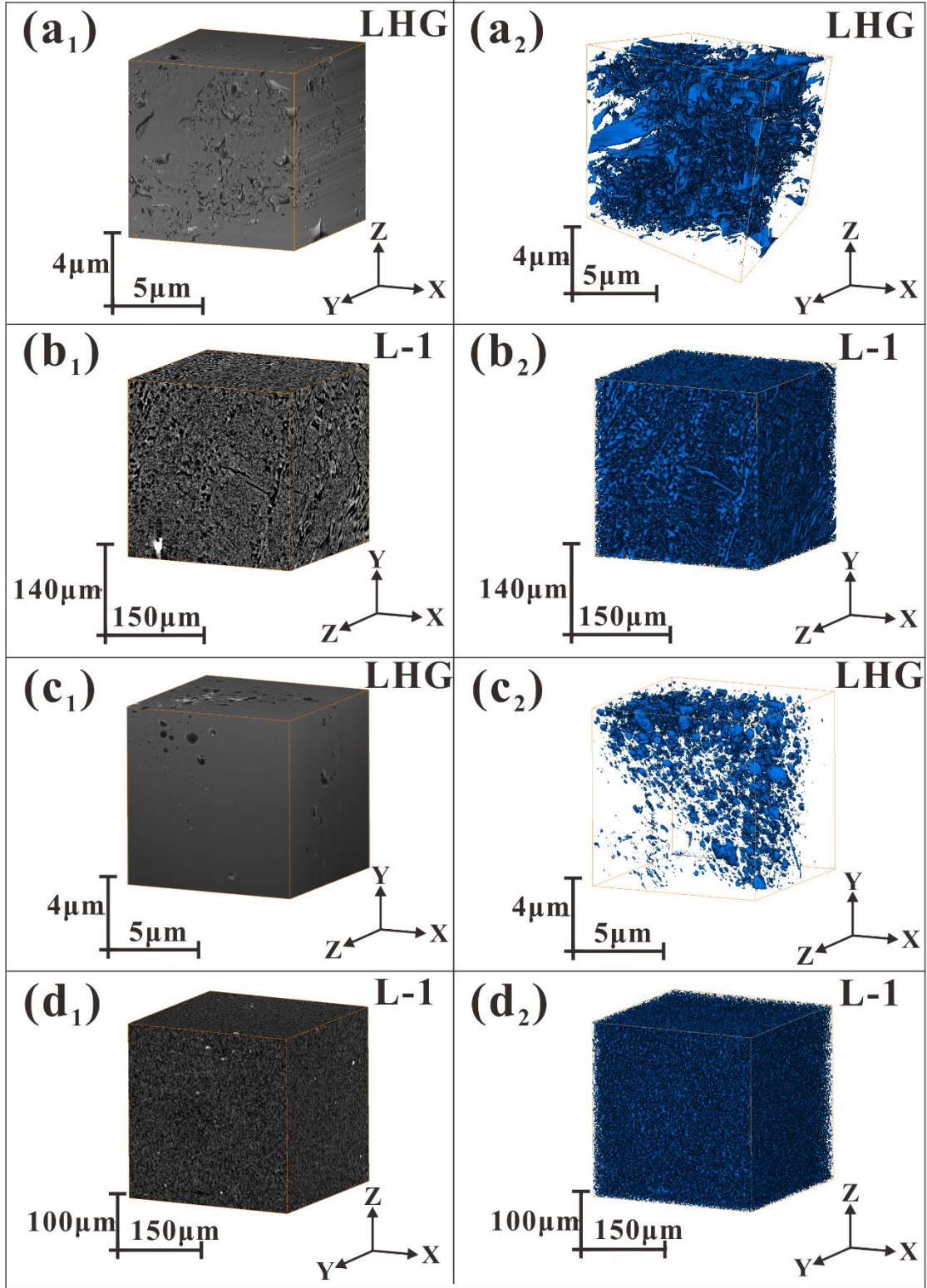
493  
 494 Fig. 42. The pore-fracture morphology of the sample LHG. (a) and (b) observe the pore-fracture distribution and  
 495 morphology of the sample from a large viewing angle. (c) exhibits a directional alignment and some irregularly  
 496 shaped pores; (d) shows irregular pores; (e) presents the phenomenon of mineral filling and partially connected  
 497 pores; (f) shows the clustered pores.



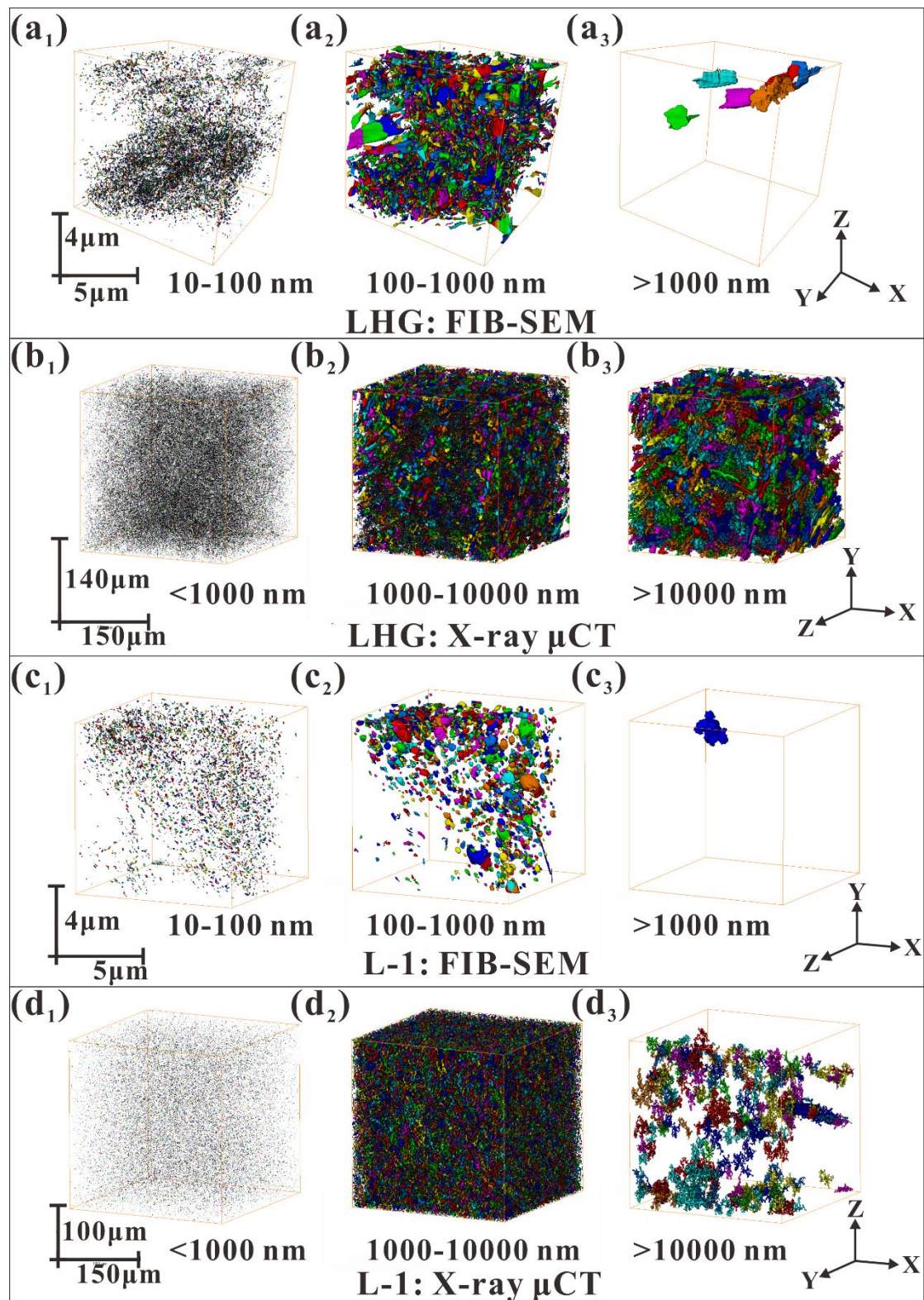
499

500 **Fig. 3.** The pore-fracture morphology of the sample L-1. (a) and (b) observe the fractures distribution,  
 501 morphology and some fractures filled with mineral. (c) and (d) exhibits pores of different shapes and filled with  
 502 mineral; (e) presents fluid erosion pores; (f) shows the clustered pores.

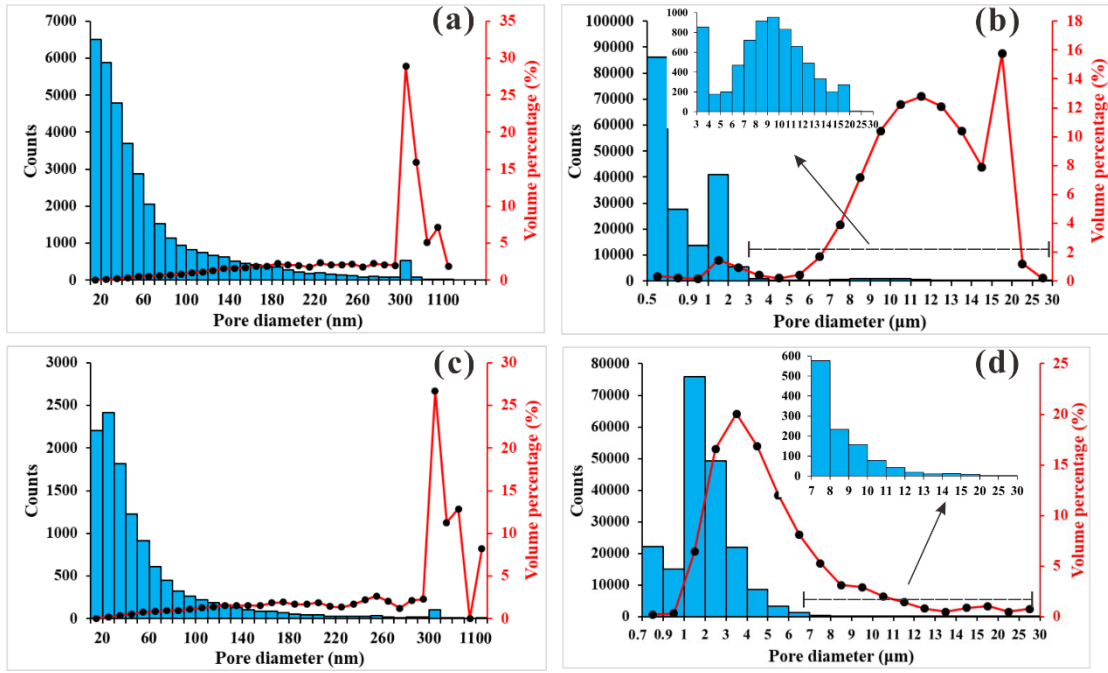




503  
 504 **Fig. 4.** 3D reconstruction images (a<sub>1</sub>-d<sub>1</sub>) and corresponding extracted pore-fracture system (a<sub>2</sub>-d<sub>2</sub>) by  
 505 Avizo2019 : (a<sub>1</sub>), (a<sub>2</sub>) - FIB-SEM data of sample LHG; (b<sub>1</sub>), (b<sub>2</sub>) - X-ray µCT data of sample LHG; (c<sub>1</sub>), (c<sub>2</sub>) -  
 506 FIB-SEM data of sample L-1; (d<sub>1</sub>), (d<sub>2</sub>) - X-ray µCT data of sample L-1. In the images on the left, black is  
 507 pore-fracture, gray is the coal matrix, and white is mineral. On the right, blue is the extracted pore network.



508  
 509 **Fig. 5.** 3D spatial distribution of pore-fraction system in different ranges. a<sub>1</sub>-a<sub>3</sub>: FIB-SEM data of sample  
 510 LHG; b<sub>1</sub>-b<sub>3</sub>: X-ray μCT data of sample LHG; c<sub>1</sub>-c<sub>3</sub>: FIB-SEM data of sample L-1; d<sub>1</sub>-d<sub>3</sub>: X-ray μCT data of sample  
 511 L-1.



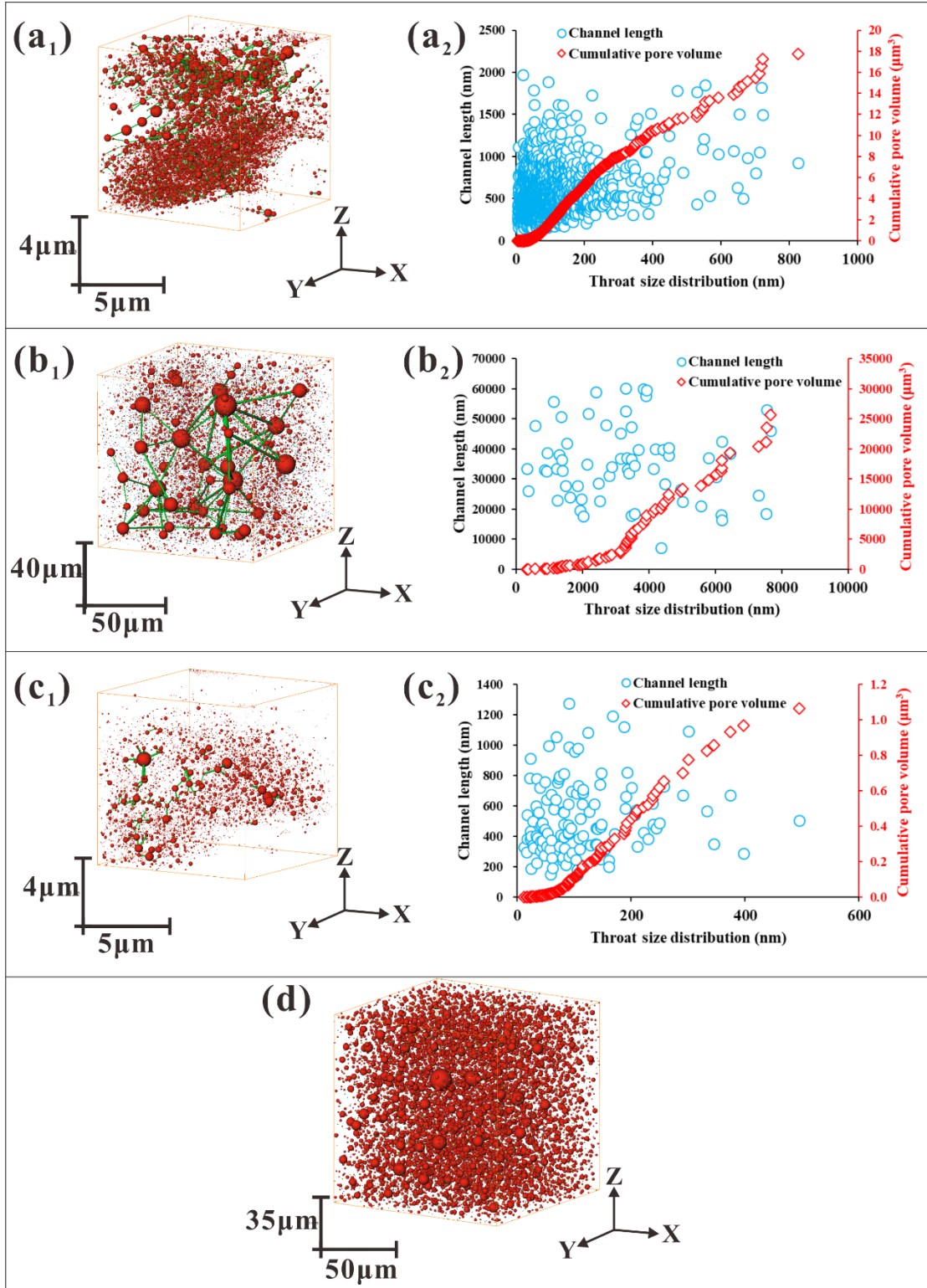
514

515 | **Fig. 6** Histogram depicting results of pore distribution and volume percentage in different ranges. (a):  
 516 FIB-SEM data of sample LHG; (b): X-ray  $\mu$ CT data of sample LHG; (c): FIB-SEM data of sample L-1; (d): X-ray  
 517  $\mu$ CT data of sample L-1.

518

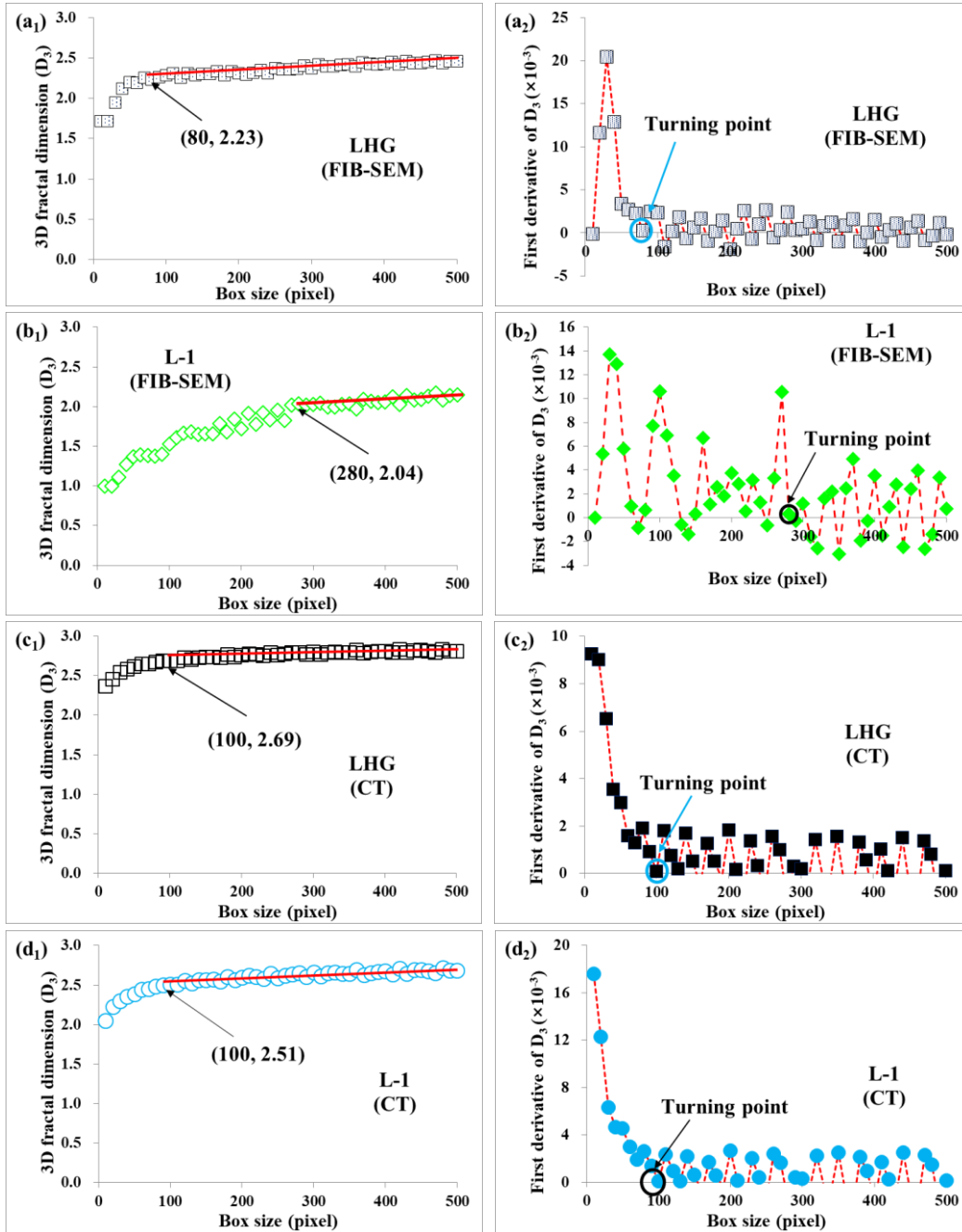
519





520  
 521 **Fig. 7.** Pore network model showing 3D pore-throat skeletal structure and distribution of throats. a<sub>1</sub>-a<sub>2</sub>:  
 522 FIB-SEM data of sample LHG; b<sub>1</sub>-b<sub>2</sub>: X-ray  $\mu$ CT data of sample LHG; c<sub>1</sub>-c<sub>2</sub>: FIB-SEM data of sample L-1; d:  
 523 X-ray  $\mu$ CT data of sample L-1.





**Fig. 7** Fig. 8. The relationship between the three-dimensional fractal dimension ( $D_3$ ) and box size. (a<sub>1</sub>) - (d<sub>1</sub>) is the trend of  $D_3$  with the box size. It indicates that  $D_3$  floats within a certain size range, but remains essentially unchanged if the calculation domain size exceeds a critical value. (a<sub>2</sub>) - (d<sub>2</sub>) is the first derivative of the left curve, which is used to characterize the rate of change of  $D_3$ . The point that first approaches 0 after the first derivative undergoes a significant change is defined as a turning point, which is expressed as  $D_3$  almost stops growing from this point.

1 539

2  
3 540

4  
5

6

7

8

9

10

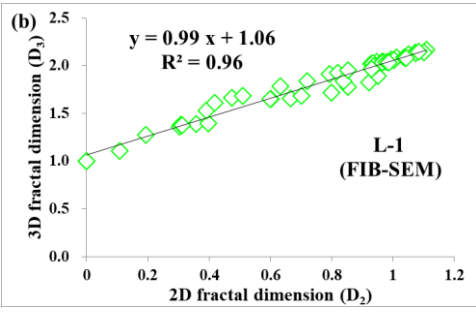
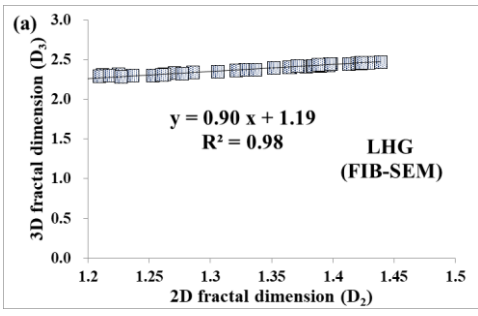
11

12

13

14

15 541



16

17

18

19

20

21

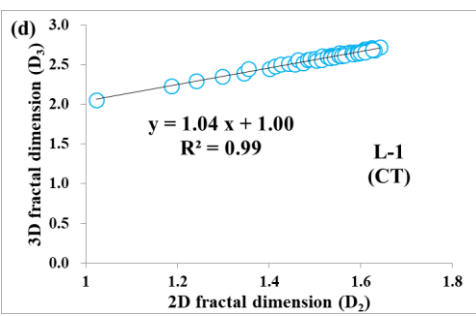
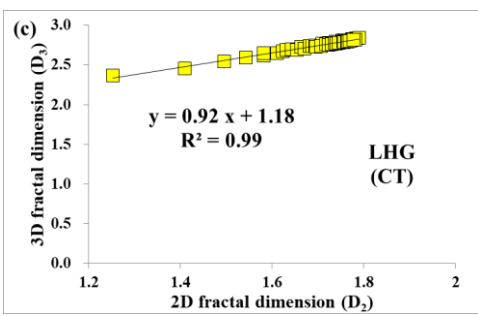
22

23

24

25

26 542



27 543

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46

47

48

49

50

**Fig. 8** Fig. 9. The relationship between two-dimensional ( $D_2$ ) fractal dimension and three-dimensional fractal dimension ( $D_3$ ). It is found that the two-dimensional fractal dimension has a very significant linear relationship with the three-dimensional fractal dimension.

51

52

53

54

55

56

57

58

59

60

61

62

63

64

65

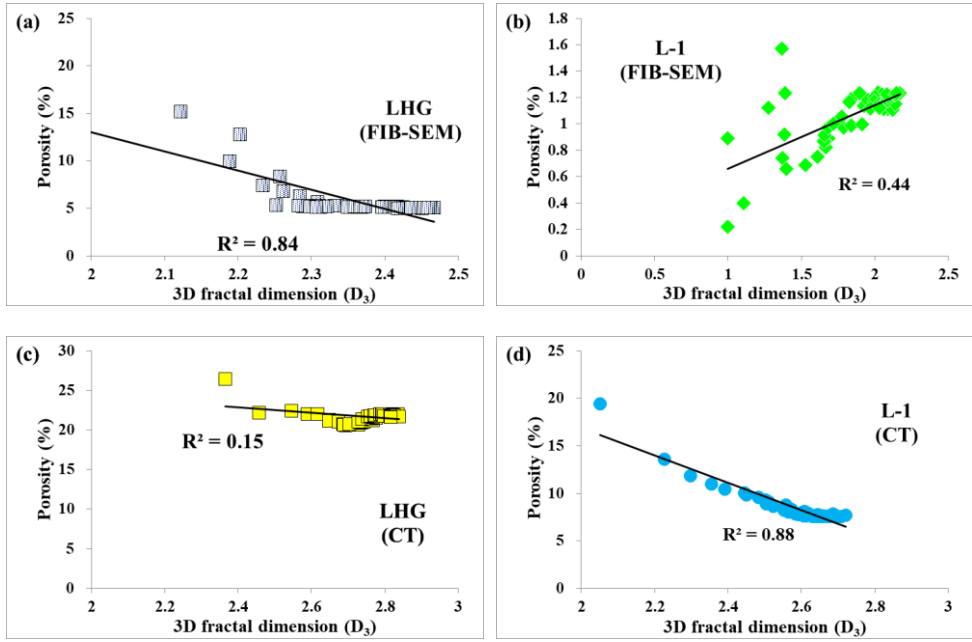


Fig. 9 Fig. 10. Relationship between three-dimensional fractal dimension and porosity. (b) shows that the porosity increases with increasing  $D_3$ ; that is, the porosity of sample L-1 increases as the three-dimensional spatial distribution complexity of pore-fracture system increases. (a) (c) and (d) display that the porosity decreases with the rise of  $D_3$ .

555

Table 1 Sample information and basic parameters of the selected Chinese coals

Sample No.	Basins	Coal Rank	R <sub>o,m</sub> (%)	Maceral and mineral (vol%)				Prox (wt%)			
				V	I	E	M	M <sub>ad</sub>	A <sub>ad</sub>	V <sub>ad</sub>	FC <sub>ad</sub>
LHG	Junggar	High-volatile bituminous	0.98	53.40	19.70	0.37	26.50	0.76	35.63	1.28	62.33
L-1	Qinshui	Anthracite	2.73	66.80	14.40	0.00	18.80	7.71	17.33	12.03	62.93

556 Note: V- Vitrinite; I - Inertinite; E- Exinite; M- Mineral; Prox- Proximate analysis; ad- as received basis; M<sub>ad</sub> =  
557 moisture content; A<sub>ad</sub> = ash yield; V<sub>ad</sub> = volatile matter content; FC<sub>ad</sub> = fixed carbon content.

558

1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65

559

Table 2 Pore size distribution characteristics of the pore-fracture system for the selected coals

Experiments	Pore diameter (nm)	Sample LHG			Sample L-1		
		Counts	Pore area ( $\mu\text{m}^2$ )	Pore volume ( $\mu\text{m}^3$ )	Counts	Pore area ( $\mu\text{m}^2$ )	Pore volume ( $\mu\text{m}^3$ )
FIB-SEM	10-100	29423	240.42	2.02	10240	89.78	0.62
	100-1000	7283	1807.86	45.37	1521	411.64	9.07
	>1000	6	57.18	4.24	1	13.92	0.87
	Total	36712	2105.45	51.63	11762	515.33	10.56
X-ray $\mu\text{CT}$	500-1000	127364	160218.62	30463.70	37177	60923.18	13292.30
	1000-10000	50802	2408362.97	1098227.32	161468	5301502.38	2151999.46
	>10000	2811	6117205.73	2986037.87	177	398234.74	189689.42
	Total	180977	8685787.31	4114728.90	198822	5760660.30	2354981.18

560

561

562

Table 3 Pore throat parameter information calculated by the PNM module in Avizo

Sample	Throat size (nm)	Counts	Area ( $\mu\text{m}^2$ )	Average channel length ( $\mu\text{m}$ )	Total channel length ( $\mu\text{m}$ )	Volume ( $\mu\text{m}^3$ )
LHG FIB-SEM	0-100	1188	3.23	0.52	277.70	1.69
	100-200	397	6.00	0.58	328.47	3.52
	200-300	100	4.53	0.63	228.67	2.83
	300-400	32	3.13	0.75	62.96	2.38
	400-500	9	1.37	0.88	24.12	1.25
	500-600	7	1.69	1.13	7.93	1.90
	600-700	5	1.70	0.94	4.68	1.58
	700-800	4	1.60	1.29	5.17	2.09
	800-900	1	0.54	0.92	0.92	0.50
LHG X-ray $\mu$ CT	300-500	2	0.19	29.69	59.39	5.67
	500-1000	4	2.20	37.99	151.95	80.10
	1000-2000	13	23.59	33.40	434.14	732.30
	2000-3000	9	43.51	36.39	327.50	1589.28
	3000-4000	16	154.23	41.79	668.60	6541.93
	4000-5000	8	126.17	31.67	253.34	3984.68
	5000-6000	3	70.40	26.83	80.49	1929.62
L-1 FIB-SEM	6000-7000	5	151.54	29.23	146.16	4453.54
	7000-8000	4	177.06	35.60	142.41	6352.96
	10-50	29	0.03	0.46	13.30	0.01
	50-100	37	0.17	0.52	19.42	0.09
	100-200	36	0.55	0.56	20.03	0.32
L-1 FIB-SEM	200-300	12	0.52	0.53	6.40	0.28
	300-400	5	0.49	0.59	2.96	0.27
	400-500	1	0.19	0.50	0.50	0.10

563 Note: X-ray  $\mu$ CT data of sample L-1 has no throat in the analysis.

564

565

566

### **CRedit author statement**

Dameng Liu and Yidong Cai: Conceptualization and Methodology; Qian Li: Data curation,  
Writing- Original draft preparation; Bo Zhao: Validation; Yongkai Qiu and Yingfang Zhou:  
Writing- Reviewing and Editing.