

Investigating the evolution of fractures in clay-based ceramics during repeated freeze-thawing cycles using micro X-ray computed tomography and image analysis

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1 Abstract

2 This work presents a study on the fracturing behaviour of a quartz tempered clay-based ceramic
3 subjected to damage in freeze-thaw cycles. X-ray micro-computed tomography (micro-CT) provided
4 high-resolution imaging of the ceramic before and during the freeze-thaw treatment, allowing to
5 analyse a fully water-saturated sample using a special thermal stage designed to keep the sample
6 frozen during analyses. Micro-CT 3D renderings showed the internal features of the specimen (i.e.,
7 quartz grain distribution), the increment of fracture count and size, and the detachment of ceramic
8 and/or temper fragments from the edges of the sample over the cycles. Selected 2D micrographs,
9 before and after freeze-thawing treatment, were analysed using the MATLAB toolbox FracPaQ. This
10 software provided detailed data on fracture length, intensity, density, orientation and connectivity,
11 and enabled to interpret the process of fracture initiation and propagation inside the material. These
12 results showed that the temper plays a crucial role in ceramic fracturing behaviour under freeze-
13 thawing conditions, as damage propagation is influenced by quartz grain distribution and orientation
14 within the material. The study described in this work, not only offers new insights into the fracture
15 dynamics of freeze-thawed clay-based ceramics, but also presents a new methodological approach to
16 quantitatively measure fracture damage in porous materials.

Keywords

Clay-based ceramics / X-ray micro computed tomography / Fractures / Freeze - Thawing / Image analysis

17 1. Introduction

18 Freeze-thaw weathering can affect both natural and artificial porous materials (e.g. soils, rocks,
19 concrete, ceramics, etc.) and has a significant impact on their mechanical properties and durability.
20 The effects of freeze-thaw cycling can be observed in different environments, leading for example to
21 rock fracturing, influencing fluid flow in soils and rocks, favouring buildings decay or damage to

22 architectural heritage and artifacts [1-4]. Fracturing in porous materials under freeze-thawing
23 conditions has been investigated in the last decades and ice crystallization pressure has been identified
24 as the main factor [5-8]. When water infiltrates into pores and fractures and solidifies into ice, it
25 expands by up to 8.7 % causing mechanical stresses and forcing the remainder liquid water in the
26 surroundings of the pores. Once the hydraulic pressure exceeds the tensile strength of the material,
27 fractures start to propagate. Small cracks can therefore evolve into larger fractures due to ice
28 crystallization pressure, allowing further infiltration of the water inside the material after thawing.
29 Alongside mechanical failure, freeze-thaw weathering can promote chemical degradation, i.e.
30 carbonation and/or sulfation, as crack propagation can expose the material to salt crystallization.
31 Hence, studying the evolution of fracture networks in freeze-thawing conditions is crucial as it can
32 provide comprehensive information on the material strength and the related degradation processes.

33 Throughout history, clay-based ceramics have had, and still find, numerous applications for buildings
34 and crafts, from bricks and tiles to water pipes and pottery [9, 10]. Despite the extensive use of clay-
35 based ceramics, studies on the effects that freeze-thaw weathering on these materials are limited,
36 although long-term exposure to the atmospheric environment can damage the ceramic materials,
37 threatening buildings as well as sites and artefacts of historical importance [11-14]. Therefore,
38 understanding and predicting ceramics fracturing behaviour is crucial for their preservation and
39 conservation.

40 Currently, the analysis of fracturing in freeze-thawed samples is performed by means of various non-
41 destructive techniques, such as acoustic emission, X-ray Computed Tomography (X-ray CT),
42 ultrasonic pulse velocity, and resonant frequency [15-18]. Among these, micro X-ray computed
43 tomography (micro-CT) is a powerful tool for the study of materials' microstructure and their changes
44 after physical and/or chemical treatments, such as freeze-thawing [19-26]. Micro-CT allows two-
45 dimensional (2D) and three-dimensional (3D) sub-micrometre imaging of the sample and the pores;
46 matrix, voids and inclusions can be distinguished and quantified via thresholding, according to their
47 X-ray absorption behaviour. During freeze-thaw cycle treatments, X-ray micro-CT allows for the
48 collection and comparison of sample data before and after treatment, thus highlighting the fracture
49 network development. Usually, micro-CT applications to freeze-thaw experiments require the drying
50 of the specimen before scanning, as the presence of water inside the sample may affect the accuracy
51 in the tomography results [16-18]. However, drying a sample after a freeze-thaw treatment can lead
52 to further modifications in the material structure; pores and fractures, once saturated with water and
53 ice, become empty. This may cause a volume reduction resulting in the closure of some fractures,
54 thus biasing the micro-CT data interpretation. Such limitation can be overcome by equipping the CT
55 scanners with customized stages, which allow to control the temperature and to keep the sample
56 frozen during the scanning [20].

57 In this work, a laboratory micro-CT apparatus, equipped with a cooling stage, was used to study the
58 brittle deformation evolution in a clay-based ceramic sample during a series of freeze-thaw cycles.
59 The cooling stage allowed us to scan the sample at -20°C while fully water-saturated; thus, preventing
60 ice melting inside it. Micro-CT renderings provided a comprehensive picture of the fractures and their
61 evolution over ten freeze-thaw cycles, revealing structure distortion, fragmentation and detachments.
62 Coupled to CT imaging, various approaches are currently used for quantitatively studying mechanical
63 damage in brittle materials in pre-post treatment tests (e.g. for in situ compressing tests of concrete);
64 among these, the most common approaches include segmentation techniques [27] and motion-based

65 techniques such as Digital Volume Correlation (DVC) [28-30]. The intrinsic features of the material
66 studied in this work (i.e., low matrix/temper contrast in the micro-CT micrographs and the specimen
67 textural complexity) led us test the application of the new freely available MATLAB™-based
68 toolbox, named FracPaQ [31]. Using this software, which implements manual segmentation it was
69 possible to monitor the process of fracture propagation within the ceramic material by quantifying
70 the variations in fracture length, intensity, density, orientation and connectivity during the different
71 freeze-thaw cycles. The application of non-destructive micro-CT analysis coupled with the analytical
72 advantages offered by FracPaQ make the proposed method readily applicable to the study of fracture
73 evolution in other materials under a variety of deformation conditions.

74

75 **2. Material and methods**

76 *2.1 Sample*

77 Ceramic samples were prepared following the procedure reported in Allegretta et al. (2015) [32].
78 Briefly, a kaolin clay was mixed with 25 vol.% of quartz temper (grain size of 1 mm) and 5 vol.% of
79 water. The briquette was moulded by uniaxial pressure (25 MPa), left drying at 100 °C for 24 hours
80 and fired at 1000 °C using a heating rate of 150 °C/h and a soaking time of 1h. Then, 5mm-side cubes
81 were cut from the briquette and they were used as testing material.

82 Production of earthenware crafts (i.e. not glazed relatively coarse clay-based ceramics) dates back as
83 early 29,000 – 20,000 BCE [33, 34]. The general formulation of traditional clay-based ceramics has
84 not changed through the centuries and comprises a clay matrix (e.g. kaolin) and commonly calcite or
85 quartz as mineral phases used for tempering [32]. The material used in this work mimics the
86 formulation of archaeological and traditional clay-based ceramics, allowing us to generalise our
87 finding to traditional and archaeological earthenware crafts.

88 *2.2 Experimental design*

89 The experiment was carried out as follows:

- 90 i. The dry ceramic specimen was initially analysed with micro-CT under ambient temperature
91 conditions (20 °C) – Pre sample;
- 92 ii. The specimen was saturated with distilled water through complete immersion (6 h), then
93 removed from the water and frozen overnight (- 20 °C) in a freezer;
- 94 iii. The specimen was taken from the freezer and immediately transferred to the sample holder of
95 the cooling stage of the micro-CT instrument, whose temperature was set at -20°C. CT
96 analyses were carried out under constant controlled temperature (-20 °C);
- 97 iv. After the analysis, the specimen was warmed through immersion in distilled water (at ambient
98 temperature) for 6 hours and then placed in the freezer overnight at -20 °C.

99 Steps ii, iii and iv were repeated ten times. Micro-CT analyses were performed after 3 (Post 3 sample),
100 7 (Post 7 sample) and 10 (Post 10 sample) freeze-thaw cycles.

101

102 *2.3 Micro-CT analyses*

103 Micro-CT analyses were performed at the Micro X-ray Lab of the University of Bari, Italy. A
104 SkyScan 1272 micro-CT instrument (Bruker Nano GmbH, Berlin, Germany) equipped with a W
105 micro-focus source (90 kV, 111 μ A, $<5 \mu\text{m}$ spot size) and a 16 mega-pixel CCD detector was used.
106 A rotating cooling stage (CS) was employed instead of the conventional rotation stage of the
107 instrument, to keep the temperature low and steady ($-20 \text{ }^\circ\text{C}$) during the scanning, thus preserving the
108 frozen water infiltrating the specimen. In particular, after sample immersion in distilled water and
109 overnight freezing at $-20 \text{ }^\circ\text{C}$, the ceramic cube was immediately applied upon the “copper finger” of
110 the CS (Fig. 1 Supplementary) by means of a drop of liquid distilled water, which rapidly and stably
111 fixed the sample once frozen. Radiographies were acquired setting a pixel size of $2.0 \mu\text{m}$, a rotation
112 step of 0.2 degrees (from 0 to 180°) and an exposure time of 3400 ms , for a total scan duration of $\sim 4\text{h}$:
113 23m . In order to improve data quality, flat field correction, averaging of 3 frames and random
114 movement of 10 pixels were used during acquisition. Further, an Al-Cu filter (Al $0.5 + \text{Cu } 0.038 \text{ mm}$
115 thickness) was applied to reduce beam hardening. A total of 949 angular projections were acquired
116 and then reconstructed using the software NRecon version $1.6.10.4$ that generated ~ 2600 -slides stack
117 of 4900×4900 pixels (pixel size $2.0 \mu\text{m}$). Volumes’ registration of Post 3, Post 7 and Post10 volumes
118 was carried out with the software DataViewer (version $1.5.2.4$, (c) Bruker μ -CT), using the Pre
119 (initial dry ceramic) volume as reference. The software CTAnalyser (version $1.15.4.0 +$, (c) Bruker
120 μ -CT) and CTvox (version $3.1.1 \text{ r1191}$, (c) Bruker μ -CT) were used for measuring quantitative
121 parameters and for the 3D rendering, respectively.

122

123 *2.4 Fracture Network Analysis*

124 To obtain information on the evolution of fracture attributes (i.e., length, orientation) and on their
125 mutual geometrical relationships (i.e., density and connectivity of the fracture network) a freely
126 available MATLABTM software package called FracPaQ has been used [31]. FracPaQ was designed
127 to generate quantitative fracture pattern data, with user control over the outputs [31]. FracPaQ can
128 quantify the length, orientation, connectivity, intensity and density of any 2D fracture pattern.

129 This software comprises a suite of tools that allow to consistently quantify fracture patterns and their
130 variations in two-dimensions (2D). Fracture maps were produced by manually tracing all the fracture
131 visible on 2D selected micrographs obtained through micro-CT, using the software Adobe
132 IllustratorTM. Although time-consuming and potentially susceptible to some subjectivity [35], manual
133 tracing allows the expert user to discern and identify specific features (e.g., discriminating fractures
134 from pores and artefacts) which can be difficult to distinguish by an automated analysis [36, 37]. In
135 order to avoid misinterpretations when tracing fractures onto the micro-CT image, using threshold
136 images as references. The aim of this approach is to minimize the users’ interpretation biases while
137 identifying fractures and, consequently, the errors in the final output.

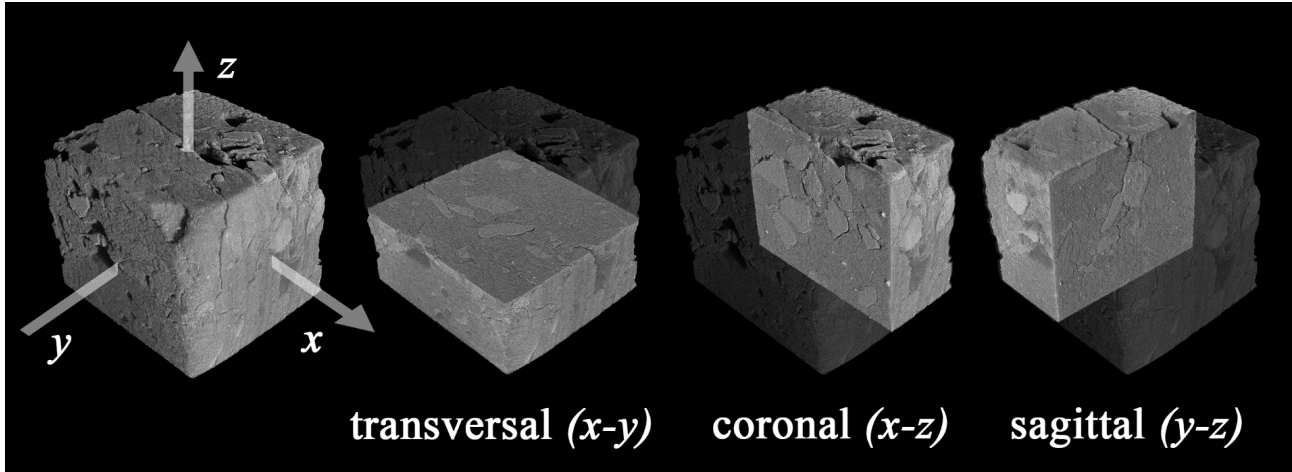
138 Once the fracture trace map is created – and saved as a Scalable Vector Graphics (SVG) file – it is
139 imported into FracPaQ. The software reads the SVG file extracting the x - y coordinates of each
140 fracture trace. The quantification of lengths and orientations is then reduced to simple operation in
141 coordinate geometry [31]. In FracPaQ, a fracture *trace* is defined as a continuous line composed of
142 one or more straight *segments*. The software assumes that fracture orientations (i.e. their strike) are
143 measured clockwise for the positive Y-axis. From these inputs FracPaQ generates several diagrams

144 (e.g., colour-coded maps for fracture and segment lengths) and plots (e.g. orientation distribution,
145 histogram of lengths) which help to visualise areal distribution of fracture attributes in a material.

146 From the initial input data FracPaQ can also produce maps of fracture spatial arrangement. In
147 particular, maps of fracture intensity, defined as the total length of fracture in a given area (here
148 expressed in mm^{-1}), and of fracture density, which is defined as the number of fractures per unit area
149 (in mm^{-2}), were created. Fracture intensity and density are estimated using the circular scan window
150 method of Mauldon et al. [38], applied to our coordinate geometry of fractures. The circle used to fit
151 within a fracture trace map can be visualised on a separate diagram, and the user can adjust the number
152 of circles fitting the map and their diameters. Fracture intensity is calculated as $n/4r$, where ‘ n ’ is the
153 number of fractures intersecting the perimeter of the circle of radius ‘ r ’; fracture density instead is
154 calculated as $m/2\pi^2$, where ‘ m ’ is the number of fractures terminating within the circle [39-40].

155 Another important measurement FracPaQ can provide is fracture connectivity. This parameter is
156 relevant to assess if a fluid (water in this case) can percolate throughout the whole material. The
157 software draws a ternary plot of fracture connectivity [41] with the three vertices of the triangle
158 denoting I, Y, X nodes in the fracture network. Nodes are classified as ‘I’ for isolated ends of fracture
159 traces, ‘Y’ for branching, splays or abutments and ‘X’ for cross-cutting intersections. More connected
160 networks plot towards the lower Y-X tie of the diagram, whereas less connected networks plot
161 towards the I apex. The relative proportions of I, Y and X nodes are then calculated with respect to
162 the total number of intersections found.

163



164

165 **Figure 1** From left to right, 3-d rendering of the analysed ceramic specimen (Post 10) and
166 visualization of the three selected sections for fracture analysis.

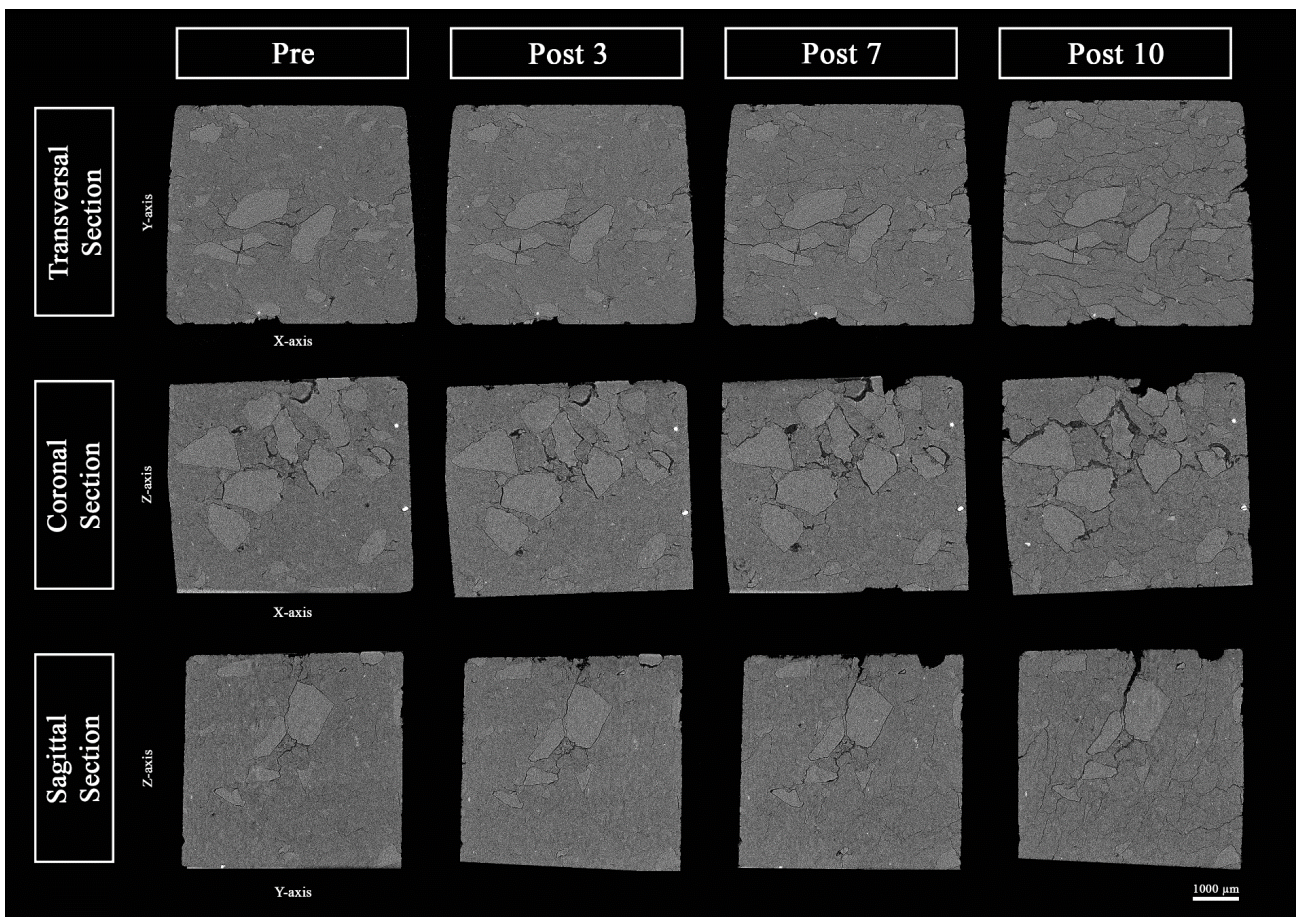
167

168 **3. Results and discussion**

169 *3.1 Micro-CT Analyses*

170 After micro-CT acquisition and datasets reconstruction and registration (full micro-CT 3D rendering
171 is shown in Fig. 1), three mutually orthogonal planes passing through the centre of the ceramic
172 specimen (i.e. transversal (X-Y), coronal (X-Z) and sagittal (Z-Y) planes) were chosen for
173 investigating the fracture evolution over ten freeze-thaw cycles (Fig. 1). Figure 2 (see also Video 1)

174 shows the transversal, coronal and sagittal sections of the untreated ceramic (Pre) and those after 3
 175 (Post 3), 7 (Post7) and 10 (Post10) freeze-thaw cycles, for the same specimen. A preliminary
 176 overview of the greyscale micrographs (where grey values, ranging from black to white, are
 177 associated with increasing values of density) allows to visualise the most relevant internal features of
 178 the sample. Hence, black and/or very dark portions of the micrographs are correlated with less dense
 179 materials (air, water or ice), while white speckles correspond to denser components (i. e. denser
 180 inclusions and/or minerals). The ceramic matrix is therefore identifiable as dark grey colour, while
 181 the quartz grain temper is dispersed in it, visible as lighter grey inclusions. The lighter chemical
 182 composition and the diffused porosity (about 40%) are responsible for the lighter density of the matrix
 183 when compared to the quartz grains [42, 43]. Quartz grains, angular and sub-angular in shape, appear
 184 particularly abundant in the coronal section. In the transversal and sagittal sections, the quartz grains
 185 are mostly visible at the centre of the images, along the x-axis and the z-axis of the transversal and
 186 sagittal section, respectively. These zones of temper clustering correspond to the cross-cutting planes
 187 between the coronal and the other two sections. The preferential orientation of the quartz grain temper
 188 is related to the briquettes' manufacture procedure: because of the uniaxial pressing of the mixture,
 189 the temper grains orientate with their major axis perpendicular to the stress direction (i.e. laying on
 190 the coronal section).



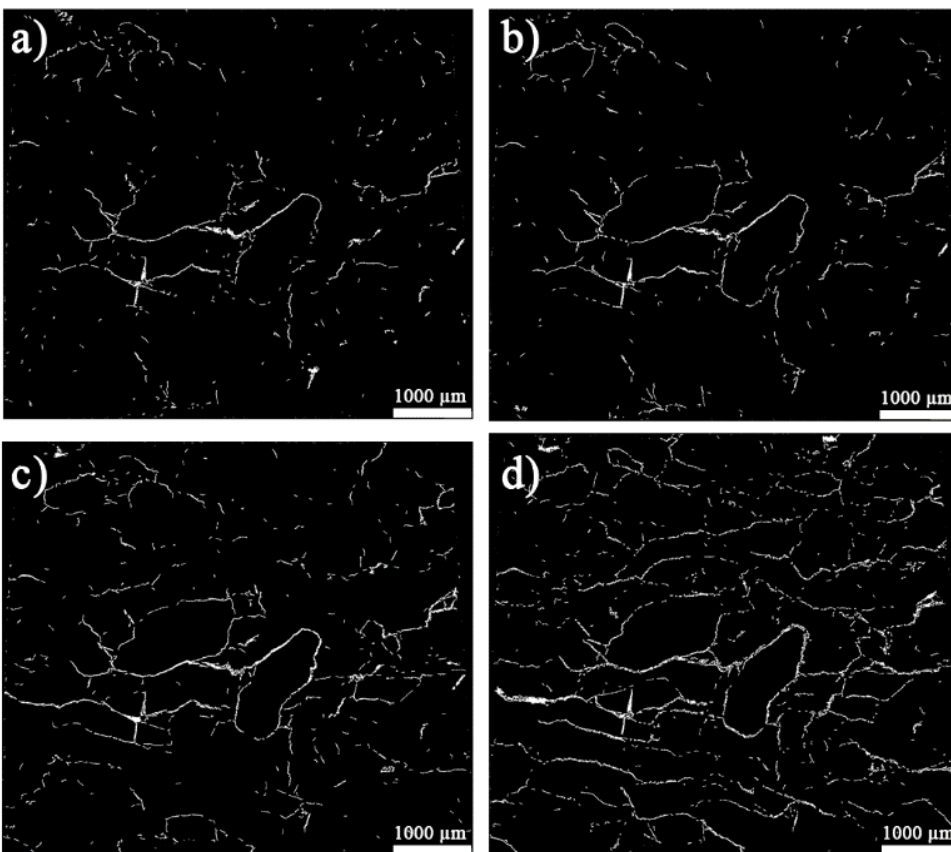
191

192 **Figure 2** Overview of the three orthogonal sections captioned from the micro-CT.

193 For both the untreated and treated samples, the blank and dark-grey features visible in micrographs
 194 (Figure 2) correspond to air or ice inside pores, fissures and fractures. In particular, fractures
 195 surrounding the quartz grain boundaries are associated with the α - β quartz phase transition, occurring

196 during the firing of the ceramic (at around 573 °C), with a volume expansion [44]. In fact, such phase
197 transition is reversible, and causes a detachment surface between the quartz grain and the matrix once
198 the ceramic cools down after firing. Finally, small bright spots, particularly visible in the coronal
199 section, can be associated with denser minerals (i.e. rutile, anatase, iron oxides).

200 The micro-CT technique is very effective when studying pre vs. post-treatment structural
201 modifications and requires the 3D registration of the different scans for facilitating the comparison.
202 The high-resolution micrographs in Fig. 1 are perfectly comparable and show that the number of
203 fractures increases as the freeze-thaw treatment is repeated. In particular for transversal and coronal
204 sections, it can be noticed that the fractures around the quartz grains gradually migrate through the
205 ceramic body, reaching the surface of the briquette in the Post 10 micrographs. Moreover, at the upper
206 edge of the coronal section, a detachment of a temper fragment at the Post 7 stage occurs. It is clear,
207 particularly from the Post 7 and Post 10 Coronal sections (Figure 2), that quartz grain-boundaries
208 serve as major discontinuities for the localisation and propagation of fractures. This is also visible in
209 the sagittal section, where another phenomenon also becomes evident: superficial small fractures not
210 detectable in the Pre-sample micrograph (in particular, in the upper-right edge of the sample) increase
211 their size and length towards the inside of the sample, and stop when they reach a quartz grain. Such
212 behaviour has been observed in other brittle materials, where inclusions (as well as pores) have the
213 ability to stop the fracture propagation and improve the toughness of the ceramic [32, 45, 46].



214
215 **Figure 3** Segmentation of fractures via thresholding of the transversal section: a) Pre b) Post 3 c) Post
216 7 d) Post 10.

217 The fracture network segmentation was performed on micro-CT micrographs via thresholding
218 (Figure 3). For each of the selected sections, fracture area (F) and the relative percentage of fracture

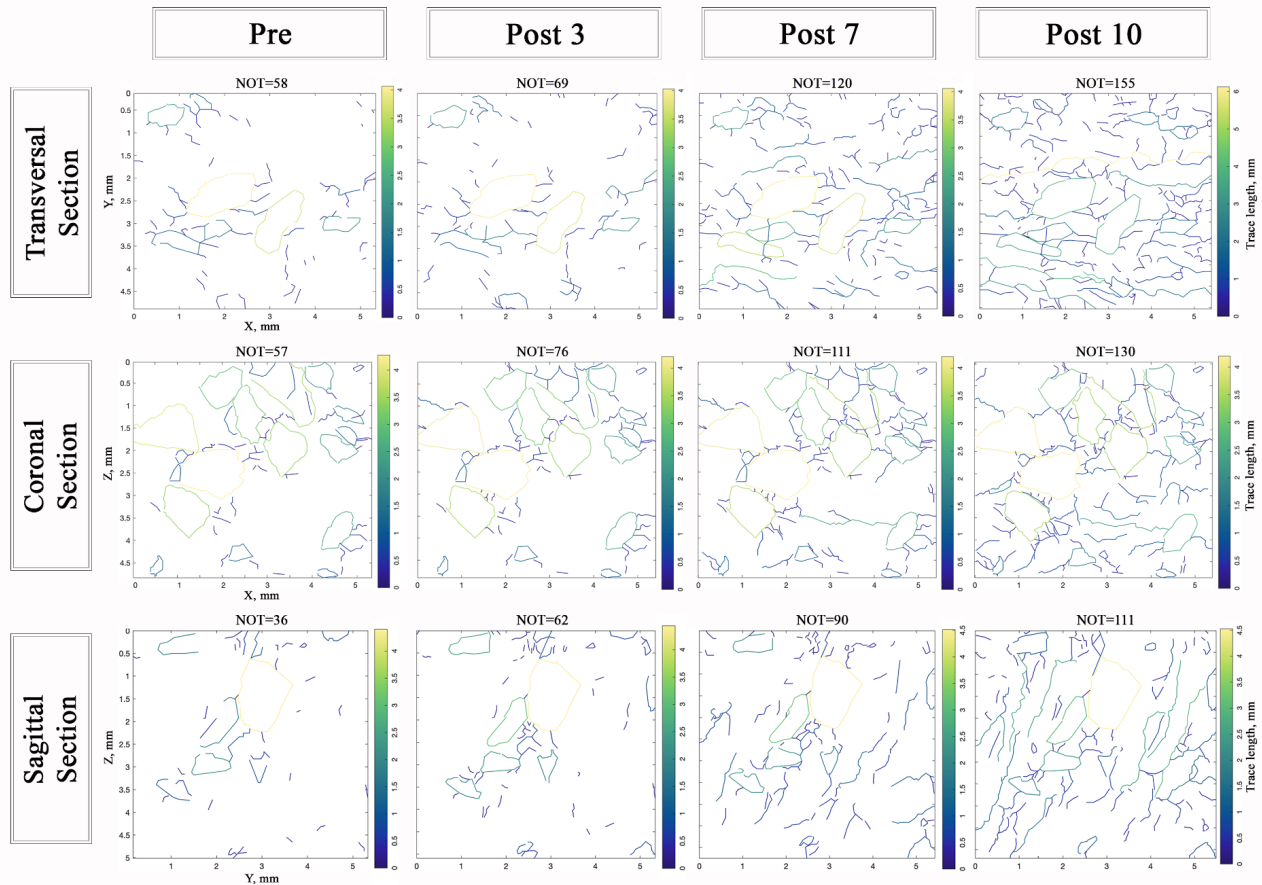
219 (%_F) were calculated (Table 1). F values increase from Pre- to Post10 sample, in all three investigated
 220 planes. In particular, the coronal section shows the highest value of %_F moving from the Pre- (2.8 %) to the Post10 stage (5.1%). Such high values can be associated with higher concentrations of the
 221 quartz temper and to the formation of wider fractures in this section (as compared to transversal and
 222 sagittal sections), created by ice expansion during the freeze-thawing steps.
 223

224

	Transversal Section				Coronal Section				Sagittal Section			
	Pre	Post3	Post7	Post10	Pre	Post3	Post7	Post10	Pre	Post3	Post7	Post10
ROI Area (mm ²)	27.85	27.99	28.17	28.82	27.2	26.91	27.05	27.11	24.72	24.37	24.77	25.16
Fracture Area (mm ²)	0.44	0.44	0.7	1.1	0.77	0.8	1.09	1.37	0.4	0.43	0.55	0.73
Fracture Area (%)	1.6	1.6	2.5	3.8	2.8	3	4	5.1	1.6	1.8	2.2	2.9

225 **Table 1** Fracture area evolution over the freeze-thaw cycles. ROI Area: overall surface of the selected
 226 section (region of interest); Fracture Area (F): total fracture surface as obtained via thresholding of
 227 the selected section; Fracture Area (%_F): fracture surface relative percentage.

228



229

230 **Figure 4** Maps of fracture trace length. Colour-coded based on fracture length (as reported in the
 231 scale bars). The number of traces (NOT) is reported above each map.

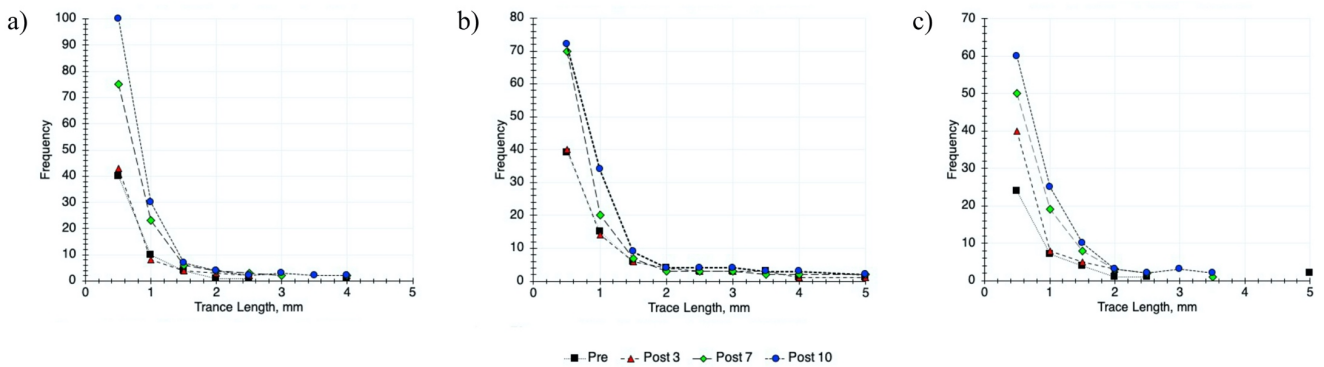
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233 3.2 FracPaQ fracture network analysis after freeze-thaw testing

234 3.2.1 Fracture length

235 Figure 4 shows trace length maps obtained analysing the selected sections of the Pre, Post 3, Post 7
 236 and Post 10 cycles with FracPaQ. The colour of the fractures moves from blue to yellow with
 237 increasing length. For all three sections at the Pre stage, most of the fractures correspond to the quartz
 238 grain-boundaries and are the longest fractures at this stage, exceeding 4 mm (Figure 4).

239 These features are particularly visible in the coronal section where the uneven distribution of quartz
 240 —grains creates a large cluster of stiff material towards the top edge of the sample. On the other hand,
 241 fractures within the matrix are scarce and mostly concentrate near the quartz grains. These fractures
 242 mostly fall in the range between 0.5 – 1.0 mm (Figure 5).



243
 244 **Figure 5** Frequency distribution of fracture lengths for the three sections: a) Transversal; b) Coronal;
 245 c) Sagittal. Samples deriving from different freeze-thaw cycles are represented with different symbols
 246 and colours. Markers plot the number of fractures for a specific class, with binning every 0.5 mm.

247
 248 Overall, the number of fracture traces increases with each freeze-thaw cycle (Table 2), although the
 249 increase is more prominent after the Post 3 stage (Figure 4). Figure 5 shows that, in all sections, the
 250 increase in the number of small fractures (less than 1 mm) is significantly higher than the increase in
 251 the number of longer fractures (more than 1 mm). These results indicate that, while some of the pre-
 252 existing fractures lengthen, the newly formed fractures remain small in comparison to the pre-existing
 253 grain boundary fractures.

254 Looking in more detail at the increase in the number of fractures in each section (Table 2), it can be
 255 observed that the transversal and coronal sections experience the highest increase in fracture numbers
 256 between the Post 3 and Post 7 stages. Differently, the sagittal section shows the highest increase in
 257 fracture numbers between the Pre and Post 3 stages. This behaviour is most likely related to the
 258 detachment of temper grains, visible through comparison of the Pre and Post 3 sagittal sections in
 259 Figure 2 and Figure 4.

260 Fracture length gradually increases during the treatment, and its effect is particularly noticeable in
 261 the Post 10 stage, where fractures cutting almost the entire sample can be observed in the transversal
 262 and sagittal sections (Figure 4). This phenomenon can be explained by a widespread coalescence of
 263 smaller fractures that must have happened between the seventh and the tenth treatment cycle. This
 264 interpretation is also supported by the increase in the number of fractures longer than 1 mm (Figure
 265 5).

	Transversal Section				Coronal Section				Sagittal Section			
	Pre	Post3	Post7	Post10	Pre	Post3	Post7	Post10	Pre	Post3	Post7	Post10

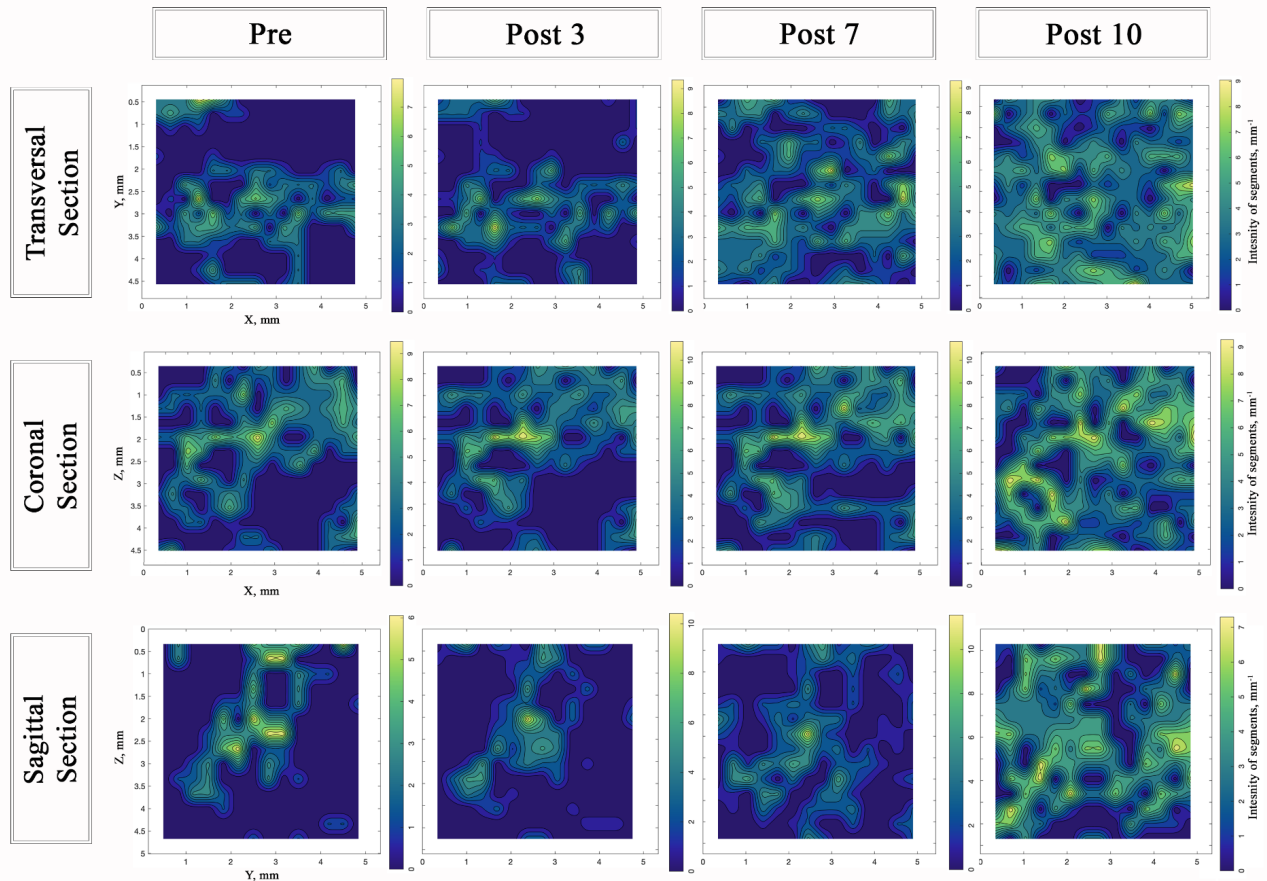
Number of Traces (NOT)	58	64	117	153	57	76	111	130	35	58	85	107
Variation in the NOT (%)	–	8	90	38	–	33	46	17	–	66	47	26
Number of Segments (NOS)	212	245	491	796	438	555	729	917	137	248	392	666
Variation in the NOS (%)	–	17	95	49	–	27	31	26	–	81	58	70
Intensity (segment/mm)	1.3	1.4	2.6	3.6	2.1	2.3	2.9	3.4	0.9	1.3	1.8	2.7
Variation in Intensity (%)	–	8	90	38	–	6	25	19	–	44	38	50
Density (segment/mm²)	8.3	9.7	18.9	28.3	17.2	20.9	27.5	34.6	5.3	9.6	13.7	23.2
Variation in Density (%)	–	17	95	49	–	22	32	26	–	81	43	70

267 **Table 2.** Overview of the variation for number of fracture traces and segments, and for fracture
268 intensity and density in the three sections. Differences in values compared to the previous freeze-
269 thaw cycle are reported as percentage of variation (%) for each parameter in table.

270

271 *3.2.2 Intensity and density of fractures*

272 In all sections at Pre stage, fracture intensity and fracture density maps (Figure 6 and Figure 7,
273 respectively) show higher values (green and yellow portions) mainly at the centre of the sample. The
274 comparison of these maps with the micro-CT micrographs (Figure 2) immediately shows that high
275 values in intensity and density correspond to the grain-boundary fractures.



276

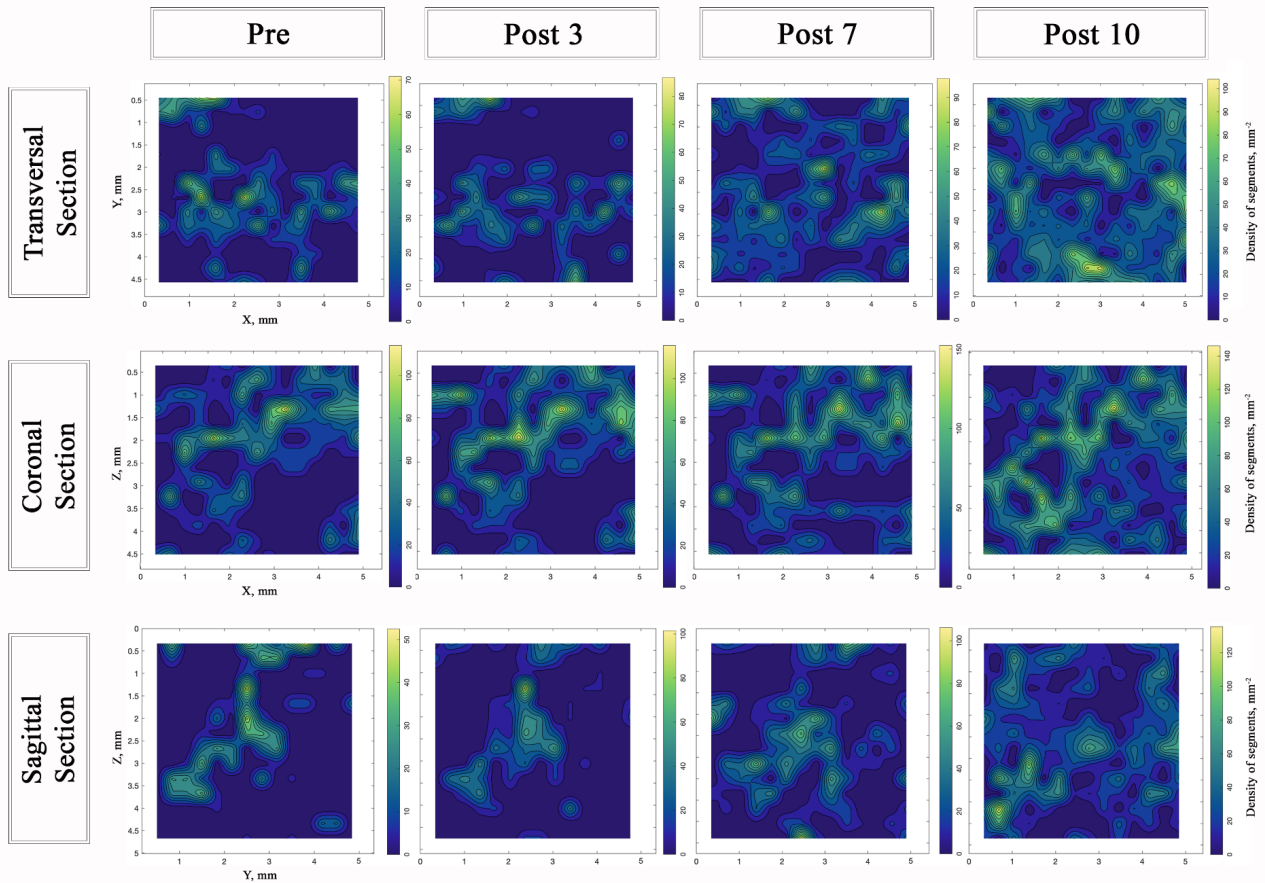
277 **Figure 6** Fracture intensity maps. Brighter colours correspond to higher fracture intensity.

278

279 It was observed an overall increase in the values of fracture intensity and density during the freeze-
280 thaw cycles (Table 2). In particular, after the first 3 freeze-thaw cycles, areas of high intensity and
281 density are still mostly confined to the central portions of the sections, highlighting the grain-
282 boundary fractures. When comparing the variation in the average intensity and density values

283 between the Pre and the Post 3 across the different sections (Table 2), the transversal and coronal
284 sections show a relatively small change (increments of 8-10 % and 17-22 % respectively), while in
285 the sagittal section variations are more marked (increment of 44 and 81%, respectively).

286 Variations occurring between the third and the seventh freeze-thaw cycle are mostly evident in the
287 transversal and sagittal sections, with average intensity and density values for the transversal section
288 that nearly double moving from Post 3 to Post 7 (Table 2). From the fracture intensity maps, it
289 emerges that, after repeated freeze-thaw cycles, fractures are distributed anisotropically within the
290 sample: in the sagittal section, the alignment has a clear inclined spread (Post 7, Figure 6), while in
291 the transversal section the broadening appears horizontal. It is not coincidentally that these
292 preferential directions, which also mark the quartz grain orientation distribution, correspond to the
293 cross-cutting planes with the coronal section. When comparing the Post 7 and the Post 10 intensity
294 maps (Figure 6) a further propagation of the fractures throughout the whole ceramic is observed.
295 Bright areas broaden and create fracture ‘corridors’ that connect the inner portions of the sample with
296 its edges. This transition is consistent with the stage of fracture length extension and coalescence
297 described for the fracture trace maps (Figure 4).

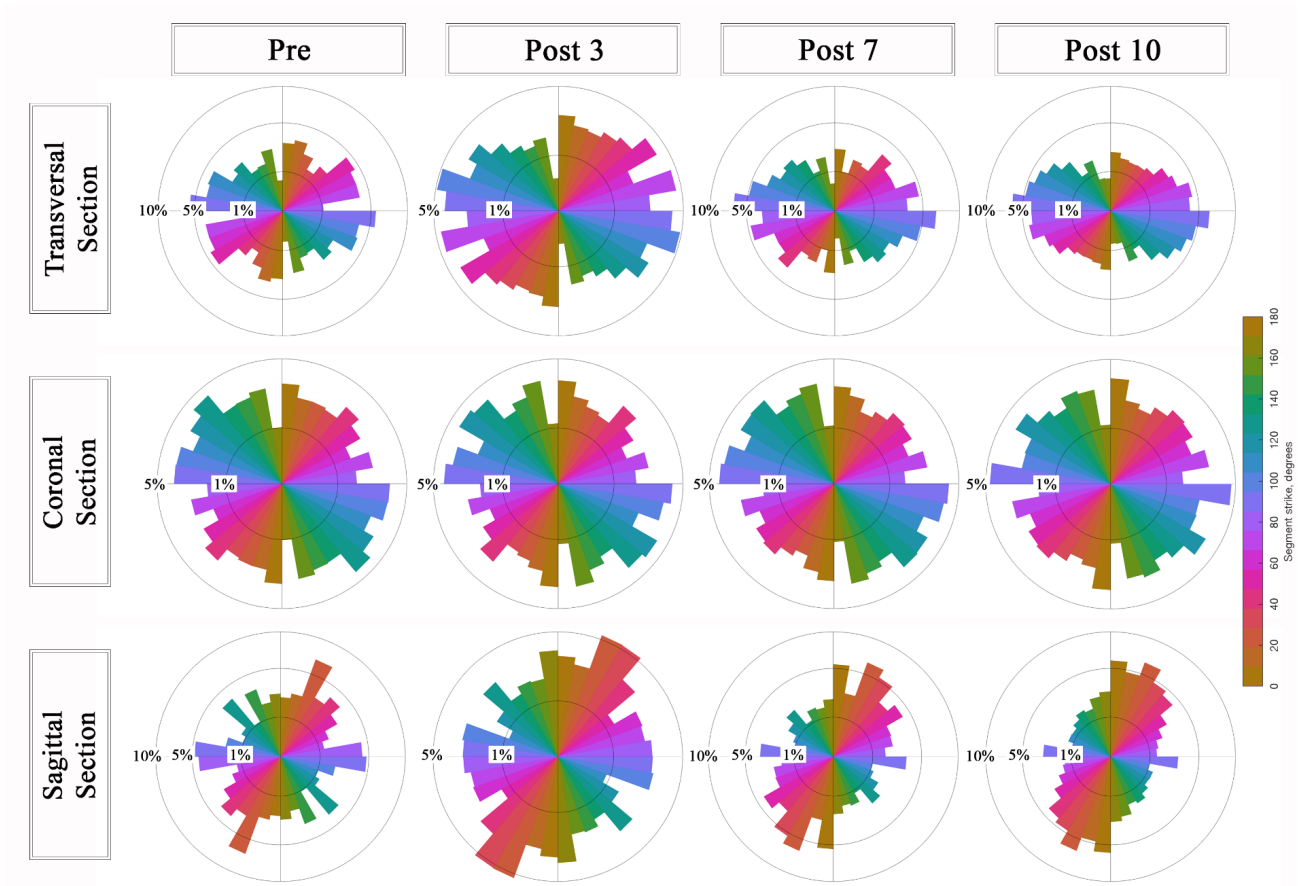


298
299 **Figure 7** Fracture density maps. Brighter colours correspond to higher fracture density.

300
301 Similarly to intensity maps, density maps (Figure 7) show that as the deformation advances fractures
302 tend to create clusters within the ceramic matrix that from the inner portion (compare Post 3 and Post
303 7, Figure 7) moves and grow towards the edges of the ceramic material. In particular, for the coronal
304 section, density reaches the highest values (Post 7 and Post 10), although the areas with higher fracture

305 density remain concentrated around the quartz grains. For the other two sections, it seems that in Post
306 10 (Figure 7) the density clusters have moved to the edge of the sample.

307



308

309 **Figure 8** Rose diagrams visualising the variations in fracture trends with freeze-thaw cycles.

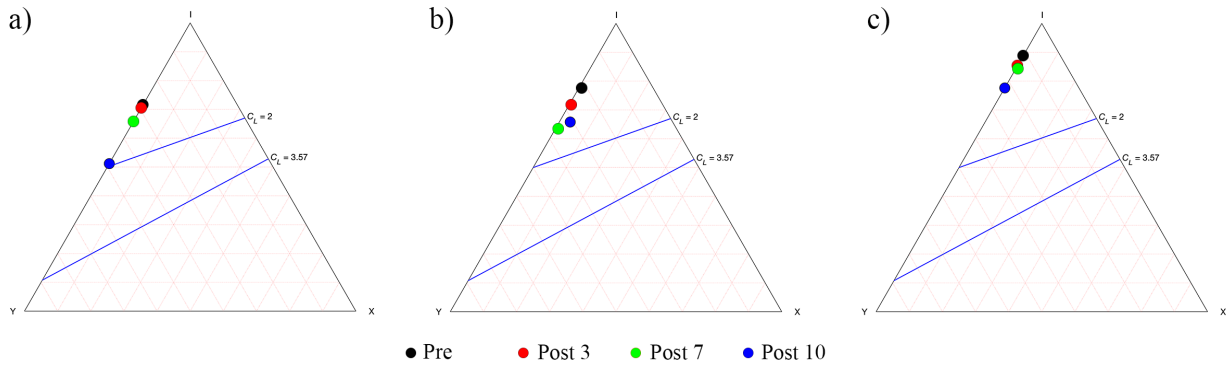
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311 3.2.3 Orientation of fractures

312 Variations in fracture orientation have been visualised using rose plots (Figure 8). This data
313 visualisation can help to assess fracture abundance as a function of their orientation [31]. The rose
314 plots in Figure 8 show variations with number of cycles (from Pre- to Post 10) as well as between the
315 three orthogonal sections (from Pre- to Post 10). In particular, in the transversal sections, fractures
316 tend to strike preferentially in a horizontal direction (along the x-axis). This preferential distribution
317 becomes more evident with increasing freeze-thaw cycles, and at final stage of deformation almost
318 the totality of fractures distributes within 80° and 100° from the vertical (Figure 8). Similarly, in the
319 sagittal sections, fractures show a preferential alignment which becomes increasingly consistent with
320 the number of freeze-thaw cycles. When comparing the rose diagram for these sections with the maps
321 of trace length and density, it becomes evident that is the original orientation of the quartz grains (and
322 therefore of the grain-boundary fractures) that guides the development of fractures. This is well
323 captured by the rose diagram of the Sagittal Pre-treatment section, where the most prominent petal of
324 the rose plot inclined at 30° from the vertical correspond to the orientation of the quartz grain-
325 boundary fractures (Figure 4). Conversely, the rose plots for the coronal section do not show any

326 preferential fracture orientation (Figure 8). This observation can be directly related to the presence of
 327 the large quartz grains and, therefore, to the high number grain-boundary fractures whose segments
 328 orient isotropically around the temper grains.

329



330

331 **Figure 9** Ternary plots of fracture connectivity for the fracture pattern in the Transversal (a), Coronal
 332 (b), and Sagittal (c) sections showing the progression in fracture connectivity in the three orthogonal
 333 sections for increasing number of freeze-thaw cycles. Two contour lines for Connections per line
 334 (CL) are also shown, using indicative values as described by Sanderson & Nixon [47].

335

336 3.2.4 Fracture connectivity

337 The anisotropy given by the alignment of quartz grains, also determines the evolution of fracture
 338 connectivity within the sample, as observed in the three sections. In Figure 9, the connectivity
 339 evolution with the application of freeze-thaw cycles is drawn for each section. In the triangular
 340 diagrams (Figure 9), C_L , indicates the number of connections per line: this parameter can be used as
 341 a measure of connectivity of a fracture network. Particularly interesting are specific values of C_L
 342 which ‘contour’ the IYX ternary diagram: any network of fractures that lies above the line $C_L = 2$
 343 is considered disconnected, irrespectively of its density; whereas connectivity values lying below the
 344 $C_L = 3.57$ represent fully connected networks. If fracture network connectivity falls in the region
 345 bounded by $2 \leq C_L < 3.57$, it is indicative of a network whose fractures are connected in clusters,
 346 however these clusters are not connected [41].

347 In our case study, the connectivity plots (Figure 9) show increase in connectivity with the application
 348 of freeze-thaw cycles. In all three sections, a similar trend of fracture network development can be
 349 observed: (i) the Pre stage show low connectivity (i.e. more I-nodes than Y- or X-nodes) resulting in
 350 low connectivity ratios; (ii) then, moving towards the tenth cycle, more Y-nodes form. Even if freeze-
 351 thawing improves the connectivity of the fractures, all the fracture networks over the 10 cycles remain
 352 in the region above the $C_L = 2$ contour, meaning that the networks are not fully connected. The Post
 353 10 transversal section measures the highest value of network connectivity with a value close to the
 354 $C_L = 2$ contour.

355 The increase of the connectivity between fractures also cause the improvement of the ability of the
 356 fracture network to carry fluid flow. Although the threshold of two connections per line ($C_L = 2$ line
 357 in Figure 9) is never crossed, the overall proportion of Y-nodes (particularly within the fracture
 358 corridors highlighted by the intensity and density maps in Figures 6 and 7, respectively), suggests

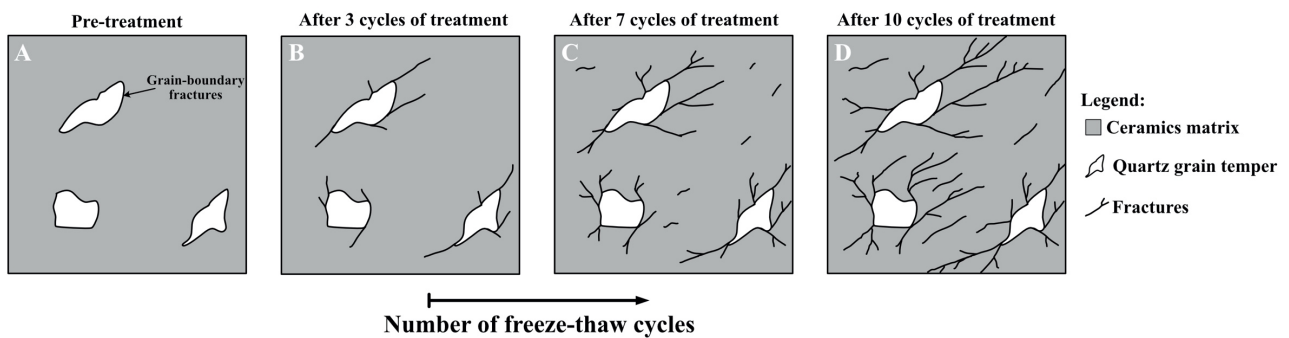
359 that moving from the Pre- to the Post 10 cycle, fractures are likely to be linked and form continuous
360 pathways through the ceramic material.

361

362 4. Summary and Implications

363 It has been generally observed that during brittle deformation of materials pre-existing flaws act to
364 concentrate stresses thereby acting as the loci for the initiation and propagation of cracks and fractures
365 [9, 48, 49]. In this studied case the main discontinuities are represented by the grain-boundary
366 fractures related to volume contraction (β to α phase transition) of the quartz grains after firing of the
367 ceramic. The influence of the quartz temper shape and size has already been proven to affect the
368 mechanical properties of the material and the propagation of the fractures within a ceramic body [50,
369 51]. Additionally, in terms of mechanical properties of the material, the presence of pre-existing
370 fractures (and the temper itself), while reducing the strength of the material, can improve its toughness
371 [9].

372 Quantitative results produced by FracPaQ on selected micro-CT micrographs provided insights on
373 the dynamic of the fracture network created under repeated freeze-thaw cycles. Fracture length maps
374 allowed us to visually and quantitatively measure fracture growth between cycles. Together with
375 these data, comparisons of the variation of intensity and density values offer a criterion for
376 interpreting fracture evolution during the freeze-thaw treatment. Considering that intensity expresses
377 the measure of fracture segments' length per area, while density measures the number of fracture
378 segments in an area, it was observed that the percentages of variation for these two parameters are
379 coupled over the whole experiment: meaning a simultaneous lengthening of existing fractures and
380 formation of new fractures. This observation was interpreted as evidence that new fractures formed
381 by branching off existing fractures. This interpretation is also consistent with the data obtained for
382 network connectivity, which showed that the connectivity of fractures in the ceramic sample was
383 achieved via Y-nodes. From the length, intensity and density maps, it could be also deduced that most
384 of the damage was accumulated between the third (Post 3) and seventh (Post 7) cycle of the treatment.
385 In this interval FracPaQ registered the highest percentage of variation in all these three parameters
386 (Table 2 and Figures 4, 6 and 7). Overall, micro-CT imaging and FracPaQ outputs show that the
387 presence of pre-existing (i.e. pre-treatment) grain-boundary fractures, together with the size and the
388 distribution of quartz grains within the samples, exerts a critical influence on the evolution of the
389 fracture network in the ceramic material. Moreover, the anisotropic distribution of the quartz grains
390 along the coronal section directly affected the direction of fracture propagation (Figure 10).



391

392 **Figure 10** Cartoon showing the evolution of fractures within the ceramic sample and the role exerted
393 by the temper grains in the initiation and propagation of fractures.

394 In summary, a commercial micro-CT instrument equipped with a cooling stage allowed us to analyse
395 the same ceramic sample over many cycles of freeze-thawing while water-saturated and frozen. Both
396 2D and 3D micro-CT imaging revealed fractures' initiation and propagation, structural distortion,
397 fragmentation and detachments. In addition, implementing FracPaQ analysis on three orthogonal
398 internal planes of the sample provided near-3D quantitative insights of the fracturing behaviour of
399 the studied material. Work is underway to develop a 3D version of FracPaQ which, using stereology,
400 can integrate the 2D data to derive the 3D pattern and its associated network properties. The versatility
401 of the presented method renders it applicable to many fields in environmental and material sciences
402 for the analysis of fracturing in man-made and natural materials, such as concrete, soils and rocks.

CRedit authorship contribution statement

Carlo Porfido: Conceptualization, Methodology, Investigation, Writing – original draft, Visualization. **Roberto Emanuele Rizzo:** Methodology, Investigation, Writing – original draft, Visualization. **David Healy:** Writing - review & editing. **Matteo Spagnuolo:** Writing - review & editing, Resources. **Roberto Terzano:** Writing - review & editing, Resources. **Ignazio Allegretta:** Investigation, Writing – original draft, Supervision.

Data Availability

The raw/processed data required to reproduce these findings cannot be shared at this time as they include more than 4TB of raw micro-tomographic data. However, for those researchers interested in analysing this dataset, tomographic data will be made available upon request by contacting the Dr. Carlo Porfido (e-mail: carlo.porfido@uniba.it). The FracPaQ toolbox, used for image analysis, is freely available to download from the following addresses: <http://fracpaq.com/index.html>.

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