Process-based modelling of microbial community dynamics in the human colon

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September 15, 2022

Abstract

The human colon contains a dynamic microbial community whose composition has important implications for human health. In this work we build a process-based model of the colonic microbial ecosystem and compare with general empirical observations and the results of in-vivo experiments. Our model comprises a complex microbial ecosystem along with absorption of short chain fatty acids (SCFA) and water by the host through the gut wall, variations in incoming dietary substrates (in the form of "meals" whose composition varies in time), bowel movements, feedback on microbial growth from changes in pH resulting from SCFA production, and multiple compartments to represent the proximal, transverse and distal colon. We verify our model against a number of observed criteria, e.g. total SCFA concentrations, SCFA ratios, mass of bowel movements, pH and water absorption over the transit time; and

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then run simulations investigating the effect of colonic transit time, and

¹⁶ the composition and amount of indigestible carbohydrate in the host diet,

 $_{\rm 17}$ $\,$ which we compare with in-vivo studies. The code is available as an R $\,$

¹⁸ package (microPopGut) to aid future research.

¹⁹ Introduction

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The human colon harbours a dense and diverse community of microbiota whose 20 interactions with the host can have a profound effect on human health (e.g. 21 Rios-Covian et al. (2016), Morrison and Preston (2016)). Due to the location of 22 this community within its host, data collection and experimentation are prob-23 lematic. Information on this system mostly comes from volunteer experiments 24 in which diet and stool samples are monitored or from laboratory experiments 25 using the microbes found in stool samples. Another approach is to put current 26 knowledge into a mathematical framework and run simulations of the system to 27 test our understanding and identify knowledge gaps. To this end a number of 28 mathematical models of this system have been developed - e.g. Cremer et al. 29 (2016), Cremer et al. (2017), Munoz-Tamayo et al. (2010), Smith et al. (2021), 30 Moorthy et al. (2015). 31

When developing a model, a number of assumptions about the system are 32 made in order to reduce complexity/dimensionality so that the model is easier to 33 parameterise, run and analyse. Some modellers choose to reduce the microbial 34 complexity and focus on the physics of the gut (e.g. Cremer et al. (2016), 35 Cremer et al. (2017)), some try to achieve a balance of both (e.g. Munoz-Tamayo 36 et al. (2010)) and some choose to develop the microbial community (e.g. Smith 37 et al. (2021)). The model described here focuses on the microbial community 38 dynamics and on interactions with the host, with a fairly simple model of the 39 colon. We include the simulation of 'meals' (of random composition and size) 40 arriving at the colon and look at the effects of bowel movements, both of which, as far as we are aware, have not been previously incorporated into such models. 42

Having developed a complex model of human gut microbiota in a fermentor system (Kettle et al., 2015), and publicly available software (microPop - an R package for modelling microbial communities (Kettle et al., 2018)) we now incorporate this 10-group microbial ecosystem model (Table 1) into a model of the human gut in order to simulate the effects of diet and host on the microbial composition and subsequent short chain fatty acid (SCFA) production.

Since approximately 95% of the SCFA produced by the microbes during 49 growth are absorbed by the host through the gut wall this represents a strong 50 interaction between the microbes and the host. Indeed the ratio of the 3 main 51 SCFAs (acetate, butyrate and propionate) is known to have a significant effect 52 on human health (Louis et al. (2014), Morrison and Preston (2016)). Thus, 53 we prioritise information on the values of these ratios in our model verification. 54 Similarly approximately 90% of the water flowing into the colon is absorbed. 55 Changes in the volume of water have a significant effect on the concentration of 56 the molecules in the colon which in turn affects pH which then affects microbial 57 growth, all of which are included in our model. 58

Due to its shape within the body, the colon is commonly divided into 3 59 different regions - the proximal, transverse and distal sections running from 60 beginning to end (Fig. 1A and B). The availability of substrate, microbial 61 growth and hence pH vary along the colon, therefore, although our model is not 62 spatial we simulate these three regions explicitly, with flow from one to another. 63 Furthermore, as well as incorporating varying substrate inflow in the form of 64 meals we also add in the release of mucins along the length of the colon which 65 can be microbially broken down to release proteins and carbohydrates, allowing 66 for further microbial growth away from the beginning of the colon where the 67 substrates enter. A graphical summary of the model is shown in Fig. 2, the 68 microbial functional groups are shown in Table 1 and the model state variables 69 are summarised in Table 2. 70

We use the following criteria to verify our model captures the main features
established for the system:

73	1.	Total SCFA (TSCFA) concentration in the proximal, transverse and distal
74		compartments should be around 123, 117 and 80 mM respectively accord-
75		ing to sudden death human autopsies (Cummings et al., 1987)
76	2.	Acetate:Propionate:Butyrate ratios are similar (around $3:1:1$) in all regions
77		of the colon and around $60{:}20{:}20~\mathrm{mM}$ (Cummings et al., 1987)
78	3.	Over 95% of SCFA are absorbed by the host (Topping and Clifton, 2001)
79	4.	Approx. 90% of incoming water is absorbed by the host (Phillips and
80		Giller, 1973)
81	5.	pH in the proximal, transverse and distal compartments should be around
82		5.7, 6.2 and 6.6 respectively (Cummings et al. (1987), and telemetry data
83		from Mikolajczyk et al. (2015), Bown et al. (1974))
84	6.	Normal daily fecal output in Britain is 100-200 g d^{-1} of which 25-50 g is
85		solid matter (i.e. 50-175 g d^{-1} is water). Bacteria make up about 55%
86		of the solid matter i.e. 14-28 g d^{-1} of microbes emitted (Stephen and
87		Cummings, 1980).

7. TSCFA concentration decreases with transit time (Lewis and Heaton,
 1997)

After model verification we examine the effects of including meals, bowel movements and fixed/varying pH into the model. We then use the model to look at how carbohydrate composition (based on the fractions of resistant starch (RS) and non-starch polysaccharides (NSP)) and total carbohydrate affect the microbial community and SCFA composition. The simulations are then compared with in-vivo data from human volunteer experiments.

Although gut microbiota are highly complex and not fully understood, here we show that it is nonetheless possible to develop predictive models of key components of this ecological system. An important goal of our modelling is to aid and inform the interpretation of data obtained, mostly from faecal samples, in



Figure 1: A. Colon schematic, B. Table of typical values for physical properties (length, volume, pH and TSCFA) and C. plots of summarised model simulations for average TSCFA and pH for comparison with typical values. Red dots show results from meals-inflow averaged over 4 random seeds; blue dots show results from continuous substrate inflow.

- ¹⁰⁰ studies on diet and health in humans. Our results show promise and we believe
- ¹⁰¹ this model represents a significant step forward in analysing this highly complex
- ¹⁰² system. We refer to the model as "microPopGut" and to aid future research the
- ¹⁰³ code is available as an R-package on github (https://github.com/HelenKettle/microPopGutCode)
- ¹⁰⁴ and instructions on how to use the package are given in the supplementary file
- ¹⁰⁵ 'getStartedWithMicroPopGut.pdf'.

106 **Results**

¹⁰⁷ Standard Model

The model settings which give the best fit to our criteria are shown in Table 4 (colon parameters and dietary inflow). The microbial group parameters are listed in Supp. Info. (section 3). These define our default model. From this we investigate the effects of different model configurations, e.g. with/without bowel movements, meals and variable pH, for a range of transit times. Simulations with meals have a random component therefore the model is run for a number of



Figure 2: Model system with the microbial ecosystem comprising 10 microbial functional groups (Table 1) which consume substrates (RS, NSP and protein) and water. The microbes produce metabolites some of which are consumed by other MFGs ('cross-feeding'). SCFA and water are absorbed through the colon wall (at a different specific rates). The system shown within the dashed line is repeated in each of the modelled regions of the colon (proximal, transerve, and distal) with the contents of the previous region, flowing into the next. The first compartment (proximal) has inflow from the small intestine - this can be constant inflow or simulated meals whose composition varies randomly in time. The third model compartment (distal) has outflow to stool which can be constant or evacuation via bowel movements can be simulated. pH varies with the TSCFA concentration and affects the rate of microbial growth differently for each MFG.

Table 1: Microbial functional groups included in the model (and the R package microPop (Kettle et al., 2018)) and described by Kettle et al. (2015). Users should be aware that the parameter values given in the data frames in the software will almost certainly change with increasing knowledge of gut microbiota and in some cases are simply a "best guess".

microPop Name	Abbr.	Description	Examples
Bacteroides	В	Acetate-propionate-	Bacteroides spp., Prevotella spp.,
		succinate group	Akkermansia muciniphila (Verru-
			comicrobia)
NoButyStarchDeg	NBSD	Non-butyrate-forming	Ruminococcaceae related to Ru-
		starch degraders	<i>minococcus bromii</i> . Also includes
			certain Lachnospiraceae
NoButyFibreDeg	NBFD	Non-butyrate-forming fi-	Ruminococcaceae related to Ru-
		bre degraders	minococcus albus, Ruminococcus
			flavefaciens. Also includes certain
	TD	.	Lachnospiraceae
LactateProducers	LP	Lactate producers	Actinobacteria, especially Bi-
			fidobacterium spp., Collinsella
ButvrateProducers1	BP1	Butvrate Producers	Lachnosniraceae related to Eubac-
Datyrater roducersi		Dutyrate 1 loudeels	terium rectale, Roseburia spp.
ButyrateProducers2	BP2	Butyrate Producers	Certain Ruminococcaceae, in
		-	particular Faecalibacterium praus-
			nitzii
PropionateProducers	PP	Propionate producers	Veillonellaceae e.g. Veillonella
			spp., Megasphaera elsdenii
ButyrateProducers3	BP3	Butyrate Producers	Lachnospiraceae related to Eubac-
			terium hallii, Anaerostipes spp.
Acetogens	A	Acetate Producers	Certain Lachnospiraceae, e.g.
			$Blautia\ hydrogenotrophica$
Methanogens	М	Methanogenic archaea	Methanobrevibacter smithii

different starting seed values. Due to the random fluctuations these simulations will not reach steady state therefore the summary values are taken as the mean from day 7 (to remove the effect of the initial conditions) to the end of the simulation (28 days) and are averaged over multiple seeds.

Table 3 gives summary results of the model simulations without bowel movements but with varying pH for each bowel region. Fig. 3 shows results from more simulations but for the distal colon only. Fig. 3a shows that although bowel movements make a difference to the total biomass and the TSCFA they do not have a large effect on the community composition or the SCFA ratios. Thus in the interests of model simplicity we decide to not include bowel movements in later simulations. However, varying pH with TSCFA can be seen to Table 2: State variables included in the model. They are all in units of mass (g; with the exception of pH) and they are computed for each model compartment (e.g. prox., trans. and dist.). They are derived automatically from the substrates and metabolites specified for each microbial functional group (MFG) in the input file/dataframe to the R package microPop Kettle et al. (2018).

Name	Details
Microbial biomass	Computed for each of the 10 MFGs (Table 1)
water	from dietary intake or from microbial metabolism
Protein	from dietary intake or mucin
Resistant starch (RS)	from dietary intake or mucin
Non-starch polysaccharides (NSP)	from intake or mucin
pH	Computed from TSCFA (Eq. 5)
Acetate	metabolite
Butyrate	metabolite
Propionate	metabolite
Formate	metabolite
Carbon dioxide	metabolite
Methane	metabolite
Ethanol	metabolite
Lactate	metabolite
Succinate	metabolite
Hydrogen	metabolite

make a large difference to the microbial community (Fig. 3b) and also improves the SCFA ratios with respect to our verification criteria. The addition of meals makes a significant difference which increases with increasing transit time (Fig. 3c). In Fig. 4 the time series output from the model shows how the mealsinflow allows the community to experience large shifts over time (on a much longer time scale than the variations in the input), as opposed to the fixed state approached using a constant substrate inflow.

Fig. 1C shows the average pH and TSCFA for the proximal, transverse 132 and distal compartments. A decrease in TSCFA (and concomitant increase in 133 pH) with longer transit time is predicted in the proximal colon both for meal 134 inflow and continuous input and this is in broad agreement with experimental 135 findings (Lewis and Heaton 1997). In section 2 of the Supp. Info. we suggest 136 a mathematical explanation for this based on the supposition that the specific 137 rate of absorption of water through the gut wall is slower than that for SCFA. 138 Regarding Table 3, for some criteria, e.g. pH, the continuous inflow setting 139

gives results closer to our verification values, but in other cases, e.g. A:B:P 140 in distal colon, simulating meals gives closer results. Note that we consider a 141 transit time of 1 day the most typical of the three transit times, and the one 142 that should be compared with our verification criteria, the others are included to 143 show the variation in results. Ideally TSCFA should be 123, 117 and 80 mM for 144 prox., trans., dist. but the best match we have to this is for a 3 d transit time and 145 continuous inflow. This is most likely due to the fact that our model has fixed 146 rates of specific absorption of SCFA and water throughout the colon. However, 147 our TSCFA values are within a reasonable range and display the general trend 148 of decreasing TSCFA from the proximal to distal colon. The microbe output, 149 i.e. the outflow of fecal microbes is steady at around 20 g d^{-1} in all cases which 150 fits well in the verification range (14-28 g d^{-1}). The water fraction is the ratio 151 of the rate of fecal water over the rate of water flowing into the colon, since 90%152 of water is absorbed this should be 0.1. This is approximately correct for our 1 153 d simulations (0.14) but, as expected, when transit time increases this decreases 154 significantly. In summary, comparing these simulation results with our list of 155 model verification criteria shows that in general our model is fit for purpose, 156 and that the inclusion of meals-inflow and varying pH improve our simulations. 157

Table 3: Summary of model results (for comparison with our list of criteria) for 3 different transit times, with meals or continuous inflow and with pH varying with TSCFA. Microbe output is the mass of microbes leaving the colon per day and the water fraction is amount of water leaving the colon per day divided by the amount entering. All simulations were run for 28 days and the results shown are the average over days 7-28. The results for the simulations with meals are averaged over 4 random seeds. 'A:B:P dist' refers to the Acetate:Butyrate:Propionate ratio (mM) in the distal colon.

		Meals	Con	tinuous in	flow	
transit time	1d	2d	3d	1d	2d	3d
TSCFA prox (mM)	115.3	110.3	105.2	124.4	123.5	122.1
TSCFA trans (mM)	102.1	88.1	83.4	75.5	96.1	111.1
TSCFA dist (mM)	107.6	64.8	69.0	89.5	62.0	83.3
A:B:P dist (mM)	62:28:17	31:23:10	34:23:12	56:27:7	38:18:6	59:17:7
pH prox	6.0	6.1	6.2	5.9	5.9	5.9
pH trans	6.2	6.5	6.6	6.7	6.4	6.1
pH dist	6.2	6.9	6.8	6.5	6.9	6.6
microbe output $(g d^{-1})$	20.2	20.1	20.1	20.0	20.1	20.0
water fraction	0.14	0.04	0.02	0.14	0.04	0.02



Figure 3: Summary results (averaged over days 7-28 and over random seeds) for the distal compartment for continuous inflow or fluctuating inflow (i.e. 'meals') for continuous outflow from colon or for 2 bowel movements per day ('2 BM/d'). The RS fraction is 0.78 (i.e. 78% of the dietary carbohyrate is resistant starch and 22% is NSP) and the transit time is 0.93 d for a), 1.25 d for b) and at 0.25, 0.5, 1, 1.5, 2, 2.5 and 3 days for c). The top row shows the biomass of each group, the bottom row shows the SCFA.

158 Model Experiments

We now use our model to simulate two scenarios – firstly, the effects of decreasing 159 total carbohydrate intake and secondly, the effects of changing carbohydrate 160 composition (whilst keeping total intake fixed) on the microbial commuty and 161 associated SCFA production. Comparing our simulations with data from human 162 volunteer experiments is not straightforward since in order to run our model, 163 ingested food must be translated to non-digestable substrates reaching the colon. 164 This is problematic due to unknown water consumption and transit times and 165 uncertainties associated with the absorption rates of the ingested carbohydrate 166 and protein higher up the digestive tract. Thus we do not attempt to reproduce 167 human experiments exactly but rather we run simulations based on variations 168 to our standard model set up which are qualitatively similar, and then compare 169 our results with the trends in the available data. 170



Figure 4: Simulation results for the distal compartment for continuous inflow (first plot on each row) or fluctuating inflow (i.e. 'meals') for transit times of 1 d (top row) and 2 d (bottom row) and for 2 random seeds. Modelled pH varies with TSCFA and the RS fraction is 0.78. There are no bowel movements (i.e. outflow is continuous). See Table 1 for microbial groups.

171 Effects of total dietary carbohydrate

In this model experiment we investigate the effects of decreasing carbohydrate 172 on the microbial community. Here we compare our results qualtitatively with 173 the human dietary study of Duncan et al. (2007) which explored the impacts of 174 carefully controlled decreases in carbohydrate intake upon weight loss and mi-175 crobial fermentation products in obese subjects using 3 diets – a maintenance 176 (M) diet, a high protein, moderate carbohydrate diet (HPMC) and a high pro-177 tein, low carbohydrate diet (HPLC) (see Fig. 5 for details). This is of course, 178 the composition for ingested food, which is not easily translated into substrate 179 concentrations entering the colon. However, we can look at the general trends 180 in SCFA and microbial composition with changing colonic carbohydrate intake 181 rate. Thus, in these model experiments we keep protein inflow to the colon at 182 10 g d⁻¹ (our default value) and then increase inflowing non-digestable (ND) 183 carbohydrate from 10 g d⁻¹ to 60 g d⁻¹ in 10 g d⁻¹ intervals. To include the 184

effects of different ND-carbohydrate composition we run the model for an resis-185 tant starch (RS) fraction of either 0.2 or 0.78 (the default value), with non-starch 186 polysaccharides (NSP) making up the remaining ND-carbohydrate in each case. 187 Although subject to large uncertainties, we estimate the RS fractions for the 188 Duncan et al. (2007) experiments of 0-0.6 (M diet), 0-0.68 (HPMC) and 0-0.12 189 (HPLC) (based on RS is 0–20% of ingested starch (Capuano et al., 2018) and 190 bio-available NSP is 75% of ingested NSP (Slavin et al., 1981)). Due to the 191 low fibre nature of many of these simulations we run the model with a slightly 192 longer transit time of 1.5 d and for both continuous inflow and meals. 193

Fig. 6 shows the SCFA results from our model experiment and Fig. 5 shows 194 the results from the in vivo experiment. It is clear, from both the model and 195 in vivo results that the proportion of butyrate increases as the amount of ND-196 carbohydrate in the diet increases. Furthermore, both model and in vivo results 197 show an increase in TSCFA with ND-carbohydrate intake rate. Since Duncan 198 et al. (2007) also look at the relationship between butyrate concentration and 199 grams of carbohydrate eaten per day, we plot butyrate against carbohydrate en-200 tering the colon (Fig. 7) to compare with their Fig. 1. In both cases, butyrate 201 concentration increases with incoming carbohydrate. Furthermore, as seen in 202 both the model and the data, the percentage of butyrate increases with carbo-203 hydrate intake (Fig. 7). Analysis of 10 human studies involving 163 subjects 204 has shown a highly significant increase in percentage butyrate with increasing 205 total SCFA concentration in faecal samples (LaBouyer et al., 2022). 206

In terms of microbial composition, Fig. 6 shows the results from our simulations are reasonably consistent across inflow type (meals or continuous), with B dominating at low carbohydrate intake. When the RS fraction is low (i.e. when ND-carbohydrate is made up of 80% NSP) then NBFD increase with increased C intake. Whereas when C is mostly RS then NBSD and BP1 increase with C. In both cases BP2 increase with increasing C intake.



Figure 5: Table on left shows the dietary intake for two human studies (Duncan et al. (2007) and Walker et al. (2011). PI, CI, SI and NSPI refer to ingested dietary protein, carbohydrate, starch and NSP. Note, starch value for the high RS diet in the Walker et al. (2011) study included 26 g commercial RS. Bar plots show SCFA data from these studies. The bars in the plots have been ordered to show increasing RS fraction (estimated by SI/CI) for the Walker study (for comparison with Fig. 8) and increasing carbohydrate for the Duncan study (for comparison with Fig. 6).



Figure 6: Simulated Biomass and SCFA results for increasing carbohydrate inflow. Simulations are run with continuous substrate inflow (cts) and with 'meals' for a transit time of 1.5 days. The results are the average over the last 3 weeks of a 28 day simulation and 'meals' is the average over 4 stochastically-generated simulations.



Figure 7: Plot of modelled butyrate, % butyrate and TSCFA against grams of carbohydrate entering the colon each day. Data from Duncan et al. (2007) is shown in magenta - due to uncertainties in converting ingested starch to RS entering the colon there are large error bars on the amount of C (g/d). Error bars show C estimated by the sum of 75% of ingested NSP plus 0-20% of ingested starch.

213 Effects of carbohydrate composition

Here we use the model to simulate the effects of changing carbohydrate compo-214 sition on the microbial community composition by changing the ratio of RS to 215 NSP whilst keeping the same amount of total incoming carbohydrate. Fig. 8 216 show a summary of the model results. Although there are differences between 217 the continuous inflow/meals, and also for the different transit times (1 d and 3 218 d), the modelled trends are generally similar, showing a significant shift in com-219 munity as the fraction of RS increases, an increase in TSCFA and changes in 220 the SCFA ratios. We compare our results with a human dietary study (Walker 221 et al. (2011), Salonen et al. (2014) and references therein) examining the im-222 pact of switching the major type of ND-carbohydrate from wheat bran (NSP) 223 to resistant starch. Volunteers were provided successively with a maintenance 224 diet, diets high in RS or NSPs and a reduced carbohydrate weight loss (WL) 225 diet, over 10 weeks (Fig. 5). 226

There are large discrepancies between the SCFA predicted by our model (Fig. 8) and the measured SCFA data (Fig. 5). Our model predicts an increase in TSCFA as proportion of RS increases whereas total fecal SCFA were significantly

lower for the RS and WL diets compared to the other two diets (in which NSP 230 is higher). One possible explanation is that fermentation of RS occurs in more 231 proximal regions of the colon compared with NSP fibre fermentation, such that 232 there is greater absorption of the SCFA products. A second possibility, also 233 likely, is that transit times were longer for the RS diet than for the NSP diet, 234 which we predict would result in decreased SCFA concentrations. In our model 235 the effect of the RS fraction on TSCFA is greater than the effect of transit time 236 so we do not see this in Fig. 8. 237

The human study also included detailed compositional analysis of the fecal 238 microbiota (Walker et al. (2011), Salonen et al. (2014)) that revealed specific 239 responses mainly by different groups of Firmicutes bacteria to the RS and NSP 240 diets. This information was particularly important for the phylogenetic assign-241 ments to the functional groups used here and previously in the model of Kettle 242 et al. (2015). Our modelling predicts striking shifts in the microbial commu-243 nity, especially involving the NBSD, NBFD and butyrate-producing groups, 244 with changing proportions of RS and NSP fibre (Fig. 8). We should also note 245 that in the volunteer experiments many bacterial species were not significantly 246 altered by the RS-NSP switch in vivo (Walker et al., 2011) indicating that many 247 may be generalists, able to switch quickly between energy sources. 248

249 Discussion

The development of a complex model of the microbial community in the human colon, whose simulations compare well with data, represents a significant step forward. Previous models have been based on simpler microbial models (e.g. Cremer et al. (2017), Munoz-Tamayo et al. (2010), Moorthy et al. (2015)), or have not shown such a good agreement with data (e.g. Smith et al. (2021)). Our previous complex model community consisted of 10 functional groups, but the model was designed only to simulate continuous culture conditions in a chemostat (Kettle et al., 2015). Translating this 10-group model into an in vivo setting



Figure 8: Biomass and SCFA results for changing the RS fraction of inflowing carbohydrate with continuous substrate inflow ('cts inflow') and with 'meals'. Protein and carbohydrate inflow are 10 and 50 g d^{-1} respectively. The results are the average over the last 3 weeks of a 28 day simulation and 'meals' is the average over 4 stochastically-generated simulations.

has required introducing multiple gut compartments, and the absorption of wa-258 ter and SCFA, followed by comparison with generally observed characteristics 259 of the system. We were then able to use this model to examine the predicted 260 impact of changes in the amount and type of non-digestible carbohydrate (fibre) 261 present in human diets upon concentrations of fermentation products (SCFA) 262 in different gut compartments and in stool. At the same time, we predict the 263 likely impact of dietary changes and variations in gut transit upon microbiota 264 composition and fermentation products. The model must be regarded as work 265 in progress particularly with respect to microbiota composition. Predictions can 266 however become improved and refined as more information becomes available 267 in time. 268

Assignments of microbial taxa to our ten functional groups were based ini-269 tially on evidence from cultured isolates. These assignments have since been 270 supported and greatly extended by analysis of genes diagnostic for different fer-271 mentation pathways within genomes and metagenomes (Reichardt et al., 2014) 272 and by molecular detection of species enriched within the community by defined 273 growth substrates in chemostat experiments (Duncan et al., 2016) and dietary 274 intervention studies (Salonen et al., 2014). Nevertheless, these assignments in-275 evitably remain provisional and incomplete and we do not claim that the model 276 predictions can be made precise at a phylogenetic level. More emphasis is placed 277 in our model on the prediction of metabolic outputs based on microbial transfor-278 mations and interactions. While there is relatively little phylogenetic overlap for 279 example between producers of propionate and butyrate (Reichardt et al. (2014), 280 Louis and Flint(2017) there are many cases where individual species are known 281 to use multiple alternative substrates as energy sources, which complicates as-282 signments. For this reason, more weight was given to fermentation pathways 283 than to substrate preferences in defining the functional groups. However, it 284 would also be possible to define completely different groupings that relate to 285 other outputs (e.g. bile acid metabolism, or vitamin/micronutrient supply) in 286 order to address specific questions. Furthermore, it may well be worthwhile to 287

increase the number of functional groups in the future. The large B group for 288 example currently includes members of the Bacteroidetes phylum, but its char-289 acteristics are mainly based on well-studied members of the Bacteroides genus. 290 We know that *Prevotella* is another highly abundant genus of *Bacteroidetes* in 291 the human colon, but the two genera tend not to co-occur at high levels in the 292 same individuals (Wu et al. (2011), Chung et al. (2020)). Less is known about 293 human colonic *Prevotella*, for which there are relatively few cultured representa-294 tives, making it premature to create a separate grouping, but this would clearly 205 be desirable in the future as their prevalence is reported to affect health and 296 responses to dietary intervention. In future it should become possible to define 297 the relative abundance of functional groups (MFGs) and their relationship to 298 phylogeny directly from genomic and metagenome analysis, by examining genes 299 diagnostic for particular pathways and functions (e.g. Reichardt et al, 2014). 300

The parameter values for the microbial groups used in our model are from 301 the intrinsic data frames in the microPop package (the only changes are to 302 LactateProducers). Although the work presented here did not attempt to fit 303 particular parameters to data, as we focussed on expanding the scope of the 304 model (i.e. changing the environment from fermentor to colon), these values 305 are easy to alter, e.g. Wang et al. (2020) changed many of these parameters to 306 achieve a better model fit to their data. As well as adjusting the parameters 307 for each group to represent inter-individual variation, groups can also be easily 308 added or removed from the model through the input argument 'microbeNames'. 309 Furthermore, it is also possible to include any number of strains (with varying 310 parameter values) within each functional group in order to add more variation 311 in outcome (see Kettle et al. (2015)) but we did not do this here in the interests 312 of computational time. It should also be noted that the parameter values are 313 highly uncertain in many cases and within each of our functional groups there 314 will be large variability due to adaptation and evolution. Given this, we do 315 not claim that the model response is necessarily representative of what may 316 happen in an individual's gut, rather it can be used as an aid to gain insight 317

into the relative importance of the different processes we are currently aware ofand potentially to highlight, those we are not.

In addition to this, it must be noted that the default diet chosen here with 10 g of protein and 50 g of carbohydrate fibre reaching the colon each day could be revised for any given population. However, converting from quantities of ingested food to substrate inflow to the colon is highly uncertain with large variations between studies, as well as technical issues with measuring this accurately. With more time, it would be interesting to investigate a larger range of typical diets but this was beyond the scope of the current work.

In summary, although performing reasonably well, the model has the potential to be considerably improved simply by altering the parameter values and existing settings, however, more fundamental changes such as those listed below could also be investigated in future work:

- Adding more functional groups or pathway switches in the existing functional groups. For example at present only the Bacteroides group can utilise protein but it is now known that some butyrate producers can also utilise amino acids (Louis and Flint, 2017)
- Our pH relation with TSCFA is very simplistic and could potentially be improved, although host secretions mean this is not necessarily straightforward.
- Currently we set the transit time for the colon and then this is split between the 3 model compartments based on their relative sizes. An interesting addition would be to alter transit time based on the composition of the various substrates entering the colon. For example, increasing residence time for high protein and/or low fibre diets. Due to variation in individual response this may need to include significant uncertainty ranges.
- Related to this is changing the absorption rate of water through the gut
 wall based on the diet, for example more water could remain in the gut
 on a high fibre diet.

• A longer term goal would be to model the processes in the gastrointestinal tract preceding the colon in order to simulate how substrates entering the colon relate to dietary intake. This would allow more accurate prediction of microbial metabolite production based on diet.

To conclude, our model helps to explain some important, but poorly under-351 stood, relationships that have been reported in human studies, including the 352 increase in butyrate proportion with increasing total faecal SCFA (LaBouyer 353 et al., 2022). This phenomenon has important implications in view of the 354 claimed benefits of butyrate supply for colorectal cancer prevention and the 355 health of the colonic mucosa (Louis et al. (2014), Hamer et al. (2008)). The 356 model also predicts increasing total faecal SCFA with greater fibre intake and 357 more rapid gut transit. Gut transit is also shown to have potentially important 358 consequences for microbiota composition and gut metabolism. In addition, the 359 model confirms that the amount and type of non-digestible carbohydrate in the 360 diet has the potential to cause major changes in microbiota composition. The 361 nature of such changes is, however, predicted to be influenced by patterns of 362 meal feeding and by any effects of dietary components (e.g. dietary fibre) upon 363 gut transit. Human studies suggest that they will also depend on the initial 364 microbiota composition. There is potential to use the model to explore how the 365 presence of particular functional groups (such as lactate-utilizers (Wang et al 366 2020)) within an individual's microbiota can influence their gut metabolism and 367 response to dietary intervention. This may indeed be one of the most intriguing 368 and fruitful applications of such modelling approaches in the future. 369

370 Materials and methods

371 Software

- 372 To facilitate continued research and future model development by other re-
- ³⁷³ searchers we provide all model code on github (https://github.com/HelenKettle/microPopGutCode).

³⁷⁴ The R package microPopGut is contained in the file microPopGut_1.0.tar.gz.

- ³⁷⁵ This can be downloaded and installed in R using install.packages('microPopGut_1.0.tar.gz').
- ³⁷⁶ Furthermore instructions on how to use the package are given in the supplemen-
- tary file 'gettingStartedWithMicroPopGut.pdf'.

378 Microbial Model

The microbial functional group model is based on the model described by Ket-379 tle et al. (2015) and implemented using the R package microPop (Kettle et al., 380 2018). The microbial groups include producers of the three major SCFA de-381 tected in fecal samples (acetate, butyrate and propionate) together with uti-382 lizers of acetate, lactate, succinate, formate and hydrogen (see Table 1 for a 383 summary, or refer to Kettle et al. (2015) for more detail). The model and its 384 equations are described in detail by Kettle et al. (2015) and Kettle et al. (2018) 385 so only a brief overview is given here The microbial groups are defined as data 386 frames within the R package and these are shown in section 3 of the Supp. Info... 387 Although this application uses the microbial parameters (e.g. maximum growth 388 rates, yields etc) that are in the package's intrinsic data frames, these can be 389 easily changed by either modifying the dataframe in R or by providing a new 390 dataframe - either as an input csv file or by creating one in R. One of the input 391 arguments to the function microPopGut() is microbeNames which allows the 392 user to also enter other microbial groups. 393

The growth substrates available in the large intestine are divided into four 394 categories: protein (P), non starch polysaccharides (NSP), resistant starch (RS) 395 and sugars (and oligosaccharides and sugar alcohols); for simplicity, all carbo-396 hydrate units are regarded as being hexoses. NSP comprise major components 397 of dietary fibre including the structural polysaccharides of the plant cell wall 398 (cellulose, xylan, pectin), whereas RS refers to the fraction of dietary starch 399 that resists digestion in the small intestine. We consider 10 major metabolites 400 that arise from substrate fermentation: acetate, propionate, butyrate, lactate, 401 succinate, formate, hydrogen, carbon dioxide, methane and ethanol. Six of these 402

metabolites (acetate, lactate, succinate, formate, hydrogen and carbon dioxide) 403 are also considered as substrates, because they are known to be consumed by 404 some groups (cross-feeding). It is well known that pH affects growth rate there-405 fore each group is assigned a preferred range of pH within which it can reach its 406 maximum growth rate, but outside of which, its growth is reduced or zero. We 407 model the rate of bacterial growth using Monod kinetics and assume that from 408 1 g of resource, Y g of biomass is produced. We assume that resource that is 409 taken up by microbes, but not used to produce biomass, is converted to metabo-410 lites. If not all of the resource is converted to biomass or to the metabolites 411 represented in our model, it is discarded. This applies, for example, to many 412 diverse fermentation products of proteins (e.g. phenols, amines) that are not 413 among the 10 major products covered by the model. Although the model was 414 initially developed to be run with multiple strains within each functional group, 415 in the current work we do not do this due to the high CPU time associated with 416 multiple compartments. 417

418 Inflow to colon

⁴¹⁹ Incoming substrates and water

The main sources of nutrient for microbiota in the colon are complex dietary 420 carbohydrates that are not absorbed higher up the digestive tract. We use 421 a default value of 50 g d^{-1} of carbohydrate, C, in our model and we vary the 422 proportion of this which is NSP or RS using the RS fraction (i.e. RS/(RS+NSP) 423 where RS+NSP=C). Based on Cremer et al. (2017) and references therein, 424 about 15 g of bio-available NSP and 30-40 g of RS enter the colon per day 425 which gives us an RS fraction of 0.67-0.9 with average value of 0.78 which we 426 use as our default value. According to Yao et al. (2016) less is known regarding 427 dietary proteins, P, that escape digestion to reach the large intestine, although it 428 is estimated that around 6 - 18 g P reaches the large intestine daily, the majority 429 from the diet and a small proportion from endogenous origins. Given this, here 430

Table 4: Summary of default values used in the model. Parameter values for the microbial groups are given in the Supp. Info. (section 3)

Symbol	Description	Default Value
T_t	transit time through colon	1.25 d
\dot{P}_{diet}	protein inflow rate	10 g d^{-1}
\dot{C}_{diet}	carbohydrate inflow rate	50 g d^{-1}
\dot{W}_{diet}	water inflow rate	1100 g d^{-1}
\dot{M}	mucin inflow rate	5 g d^{-1}
K_M	half saturation constant for Mucin breakdown	$0.5 \text{ g } \mathrm{l}^{-1}$
a_W	rate of water absorption by host	$3 d^{-1}$
a_Z	rate of SCFA absorption by host	$9.6 \ d^{-1}$

we assume that 10 g d^{-1} of undigested P reaches the colon from dietary intake 431 along with a small amount from mucin degradation (approx. 1 g d^{-1}). Phillips 432 and Giller (1973) state that water enters at approximately $1.5 \ l \ d^{-1}$ and about 433 90% of this is absorbed by the colon. Stephen and Cummings (1980) states that 434 normal fecal daily output in Britain is 100-200 g d^{-1} of which 25-50 g d^{-1} is 435 solid matter and the rest (50-175 g d^{-1}) is water. Thus if 90% is absorbed then 436 this indicates water inflow in the range $0.5 - 1.75 \mid d^{-1}$. The midpoint of this 437 range is 110 g d^{-1} of water outflow which, if 90% is absorbed, implies that the 438 inflow of water is approximately 1100 g d^{-1} . This will clearly vary depending 439 on the host's oral water intake but we use 1100 g d^{-1} as our default value. The 440 default inflow values are summarised in Table 4. 441

442 Meals

The normal human diet does not consist of continuous fixed inflow of substrate; 443 for a more realistic substrate inflow to the colon we simulate eating 3 meals a 444 day with randomly varying composition. We then approximate the passage of 445 these meals through the stomach and small intestine to obtain a smoothed time 446 series for substrate entering the colon. Note that we are not simulating all the 447 food ingested by the host (most of which will not reach the colon) but rather 448 simply trying to produce a more realistic time series for the substrates that we 449 know reach the colon. 450



We specify three meals per day each with a duration of 30 minutes. This

time-series is then passed through a one-compartment ordinary differential equation model representing the time spent in the stomach and small intestine (estimated to take 7 hours), i.e.

$$\frac{ds(t)}{dt} = s(t)_{in} - vs(t) \tag{1}$$

where $v=3.4 \text{ d}^{-1}$ (inverse of 7 h transit time in days); $s(t)_{in}$ is time series 455 representing 3 meals a day (g d^{-1}) and t is time in days. The inflow to the 456 colon (i.e. the outflow from small instestine) is given by vs(t). The composition 457 (in terms of P, NSP, RS and water (W)) of these meals varies randomly around 458 the mean of each component (Table 4) for each meal. To generate such random 459 fluctuations we draw samples for each meal from a gamma distribution (since 460 this is always above zero) defined by a scale parameter (γ_s) and the daily average 461 inflow of the substrate (g d^{-1}). We assume the magnitude of the substrate 462 fluctations are proportional to the mean value. Preliminary simulations showed 463 that γ_s equal to half the mean value of each substrate gave a good variation for 464 P, RS and NSP, and for water variation we assumed γ_s was one tenth of the 465 incoming daily flow. The distributions and flow patterns are shown in Fig. 9. 466

467 Mucin

There is a further input of protein and carbohydrate from the host via the 468 breakdown of host-released mucin by many strains in the B group (Ravcheev 460 and Thiele, 2017) and in our NBFD group (Crost et al., 2013). It is estimated 470 that 2.7-7.3 g d⁻¹ of mucin, denoted \dot{M} , is secreted into the colon (Florin 471 et al., 1991), therefore we take the midpoint value 5 g/d. We assume our mucin 472 degraders break down 1 g of mucin into 0.05 g sulphate, 0.2 g P and 0.75 g C, 473 based on Sung et al. (2017), but consider their yield on mucin to be negligible 474 compared with growth on other substrates. We split C equally between NSP 475 and RS - this arbitrary choice did not affect model results since C from mucin 476 $(3.75 \text{ g d}^{-1} \text{ maximum})$ is much less than dietary C (50 g d⁻¹), but this should 477



Figure 9: a) Gamma distribution from which random values are drawn to generate the composition of each meal (note water is not shown due to the large difference in magnitude between water and dietary substrates). b) The substrate inflow time series to the proximal colon after passing through the small intestine. Examples shown for 3 stochastic simulations starting with different seeds. c) Barplots showing the composition of 6 meals over 2 days for 3 different stochastic simulations.

⁴⁷⁸ be revised if considering very different dietary drivers. Since the compartments ⁴⁷⁹ of the colon are not equal-sized we assume that the rate of mucin entering the ⁴⁸⁰ colon is divided through the model compartments proportional to their relative ⁴⁸¹ volumes. We assume this enters the colon at a fixed, continuous rate and mucin-⁴⁸² derived P and C are a function of the mass of mucin degraders, D_M (B and ⁴⁸³ NBFD), such that,

$$\dot{C(t)} = 0.75 \frac{D_M(t)}{D_M(t) + K_M W_v(t)} \dot{M}$$
 (2)

$$\dot{P(t)} = 0.2 \frac{D_M(t)}{D_M(t) + K_M W_v(t)} \dot{M}$$
 (3)

where C, P, D_M are in mass units and the over dot indicates a rate (e.g. g d⁻¹), t is time and W_v is the volume of water in the model compartment. K_M (g l⁻¹) is chosen such that if $D_M << K_M W_v$ then there is minimal breakdown of mucin and if $D_M >> K_M W_v$ there is maximal breakdown. The smaller the value of K_M the more breakdown there will be at low concentrations of mucin degraders. We set $K_M=0.5$ g l⁻¹ based on preliminary model simulations.

490 Absorption by host

⁴⁹¹ SCFA and water are both absorbed by the host through the gut wall; over 95% ⁴⁹² of SCFA (Topping and Clifton, 2001) and approximately 90% of incoming water ⁴⁹³ is absorbed (Phillips and Giller, 1973). Experiments by Ruppin et al. (1980) ⁴⁹⁴ found that the absorption rates of SCFA to be approximately 0.4 h⁻¹ (i.e. 9.6 ⁴⁹⁵ d⁻¹) with little difference in rates between the different SCFA (Ruppin et al. ⁴⁹⁶ (1980), Topping and Clifton (2001)).

We can estimate mathematically the specific water absorption rate required to give 90% absorption of inflowing water for a given number of compartments in the colon (N) and a given transit time, T_t , using

$$a_W = \frac{16.95 - 9.72N + 1.77N^2}{T_t} \tag{4}$$

(see Supp. Info. Section 1.3 for the derivation). As a rough estimation, for a 3 compartment model with a transit time 1-1.5 days, gives $a_W \approx 3 \text{ d}^{-1}$ (Supp. Info. Fig. S1a). Given this will not be significantly affected by the microbial model (microbial uptake/production of water is small) this is a robust estimation.

To estimate the value of the specific absorption rate of SCFA, a_Z , we used 505 a simple model (see Supp. Info. sections 1.1 and 1.4). Estimating the value 506 of the specific absorption rate of SCFA based on the values of SCFA given in 507 the verification criteria and given our estimate for a_W we found that it was 508 necessary for the specific absorption rate to change along the colon (see Supp. 509 Info. section 1.4). The best estimates were given by a_Z values of 25.2, 4.2 and 510 9.2 d^{-1} in the proximal, transverse and distal colon respectively. However, in 511 the interests of a robust model (i.e. the fewer parameter values, the better) 512 we made the decision to use one value for a_Z . Since the experimental value of 513 9.6 d⁻¹ compares well with our estimate in the distal colon we set $a_Z=9.6$ d⁻¹ 514 throughout. It should be noted though that our model results could potentially 515 be improved by varying a_Z between model compartments. 516

517 pH

⁵¹⁸ Calculating pH in our model is not straightforward due to a lack of necessary ⁵¹⁹ state variables as well as pH buffering via secretions from the host. However, ⁵²⁰ observations tell us the pH in the colon goes from 5.7 in the proximal, 6.2 in ⁵²¹ the transverse and 6.6 in the descending colon and TSCFA in these regions is ⁵²² around 123 mM, 117 mM and 80 mM respectively (Cummings et al., 1987). ⁵²³ Therefore an approximate approach is to simply make pH a function of TSCFA.

524 Fitting a line through the above points gives us the following relationship

$$pH = 8.02 - 0.0174 \times TSCFA.$$
 (5)



Figure 10: a) Relating pH to TSCFA using Eq. 5 and data from (Cummings et al., 1987). b) Example of microbial tolerance to pH. A pH tolerance function of this form is specified individually for each microbial group in our model.

which we further limit by setting the minimum and maximum pH values at 5 and 8 respectively i.e. if the TSCFA values give predicted pH outside of this range (Fig. 10).

The impact of pH on microbial growth is modelled via a pH limitation func-528 tion whereby there is a range over which there is no limit on growth but outside 529 of this range the growth rate decreases linearly to reach zero at the specified 530 outer limits. Thus there are 4 parameters used to describe the pH tolerance -2531 for the inner range where there is no limit on growth and 2 for the outer range 532 outside which there is no growth – an example is shown in Fig. 10. The pH 533 tolerance range for each microbial group is specified under the entry 'pHcorners' 534 in the data frame for each group and shown in Supp. Info. section 3. 535

536 Fecal outflow

Fecal outflow (g d⁻¹) at time, t, is given by $m_d(t)V_d$ where $m_d(t)$ is the mass in the distal colon (i.e. microbes, unconsumed substrate, microbial metabolites and water) and V_d is the specific wash out rate from the colon (the inverse of the time spent in the distal colon). For continuous outflow (as is used in most gut models) we compute the specific wash out rate from each compartment by assuming the fraction of time spent in compartment, i, is proportional to its 543 volume fraction, thus

$$T_i = \frac{v_i}{v_{colon}} T_t \tag{6}$$

where v_i is the volume of compartment *i* and v_{colon} is the total volume of the colon. The specific wash out rate is then $V_i = 1/T_i$.

If we introduce bowel movements then, assuming the distal colon is approximately emptied for each bowel movement, the total transit time is given by

$$T_t = \Sigma_{i=1}^2 T_i + \frac{1}{N_{BM}}$$
(7)

where N_{BM} is the number of bowel movements per day. For example, using vol-548 ume measurements (Table 1B) and assuming a total transit time of 1 day would 549 mean about 45% of the transit time is spent in the proximal and transverse 550 colon and about 55% of the day spent in the distal, which would be similar to 2 551 bowel movements per day. In model experiments where we vary the number of 552 bowel movements per day we also change the time spent in the rest of the colon 553 since we assume increased bowel movements are indicative of a general increase 554 in passage rate. We estimate the wash out rate from the colon during a bowel 555 movement, V_{BM} , by 556

$$V_{BM} = -\frac{\ln(f_d)}{\Delta t_{BM}} \tag{8}$$

where f_d is the fraction of mass left in the distal colon after the bowel movement and Δt_{BM} is the time taken for the bowel movement (d). For example, if a bowel movement takes 10 minutes to remove 90% of the contents of the distal colon then V_{BM} is 332 d⁻¹. This is not affected by the number of bowel movements per day.

562 Author Contributions

Kettle wrote the model code and led the writing of the manuscript. Flint contributed to writing the manuscript. Flint and Louis contributed to all aspects
of microbiolgy and all authors contributed critically to the drafts and gave final

566 approval for publication.

567 Acknowledgments

568 We thank the Scottish Government's Rural and Environment Science and Ana-

⁵⁶⁹ lytical Services Division (RESAS) for funding this research.

570 Data Accessibility

- All model code is on github (https://github.com/HelenKettle/microPopGutCode).
- ⁵⁷² The R package microPopGut is contained in the file microPopGut_1.0.tar.gz.
- ⁵⁷³ This can be downloaded and installed in R using install.packages('microPopGut_1.0.tar.gz').
- 574 Furthermore instructions on how to use the package are given in the supplemen-
- 575 tary file 'getStartedWithMicroPopGut.pdf'. The model output for the simula-
- 576 tions described in this manuscript are included on figshare in the file Mod-
- elRuns.tar.gz (https://doi.org/10.6084/m9.figshare.21094558.v1). The plotting
- ⁵⁷⁸ code is provided in the github repository.

579 Funding Statement

The Scottish Government's Rural and Environment Science and Analytical Services Division (RESAS) funded this research.

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microPopGut: R package for simulating microbial populations in the human colon

Helen Kettle

Overview of microPopGut

MicroPopGut is an R package which simulates/predicts the growth of interacting microbial populations in the human colon based on the solution of a system of ordinary differential equations (ODEs). It models the colon as three compartments (proximal, transverse and distal) with a microbial community based on 10 microbial functional groups (MFGs) in each one. Protein and carbohydrates (resistant starch and non-starch polysaccharide (NSP)) enter the proximal compartment. This inflow can be modelled as a constant rate or with fluctuations to simulate meals (which have passed through the stomach and small intestine). The outflow from the distal compartment can be modelled as a constant flow or bowel movements can be simulated.

To simulate microbial growth we use our previous R package, microPop, which is a generic package for modelling microbial communities. The 10 microbial functional groups used in microPopGut are instrinsic data frames in microPop (see Table 1 in the paper Kettle et al. 2018, in the link below for details of the MFGs). The main difference to the usual use of microPop used here is that we include water as a state variable. Water is injested by the host and absorbed through the colon walls and its volume is not constant. When calculating concentrations we use the current volume of water in each compartment.

the microPop package

For background info, the microPop package is described in the paper:

Kettle H, G Holtrop, P Louis, HJ Flint. 2018. microPop: Modelling microbial populations and communities in R. Methods in Ecology and Evolution, 9(2), p399-409. doi: 10.1111/2041-210X.12873

https://besjournals.onlinelibrary.wiley.com/doi/full/10.1111/2041-210X.12873

The user specifies the system via a number of input files (csv files that become dataframes) and the function microPopModel() will construct and solve the necessary equations (ordinary differential equations) and provide an output containing the solution (e.g. the concentrations of microbes, substrates and metabolites at the required time points) as well as all the settings/parameters involved in the simulation, and plots of the microbes and resources over time.

Also see the webpage:

https://www.bioss.ac.uk/people/helen/microPop/microPop.html

Getting started with microPopGut

Install the package and add the library:

```
install.packages('microPopGut')
#> Loading required package: usethis
#> i Loading microPopGut
#> Loading required package: microPop
#> Loading required package: deSolve
#> Loading required package: visNetwork
library(microPopGut)
```

Basic model run

Note that simulating a complex microbial community of 10 MFGs in 3 compartments is fairly slow to run, so the code evaluated in this tutorial only simulates very short time periods.

In this first example we only use two microbial groups and have constant inflow and outflow to and from the colon and we run the simulation for 2 hours.

```
sim.time.h=2 #time to simulate in hours
m.out=microPopGut(
   numDays=sim.time.h/24, #number of days to simulate
    time.step=1/24/60, #time step at which you want output
    transitTime=1.25, #time taken to move through colon (days)
   microbeNames=c('Bacteroides', 'ButyrateProducers1'), #vector of MFG names
                  #(these are data frames provided in the microPop package)
   microbeNames.short=c('Bacteroides'='B', 'ButyrateProducers1'='BP1') #abbreviated names used for plot
)
#> [1] "simulating growth in compartment 1 - please wait!"
#> [1] "using microPopGut"
#> [1] "Set up completed, ODE solver called..."
#> [1] "simulating growth in compartment 2 - please wait!"
#> [1] "using microPopGut"
#> [1] "Set up completed, ODE solver called..."
#> [1] "simulating growth in compartment 3 - please wait!"
#> [1] "using microPopGut"
#> [1] "Set up completed, ODE solver called..."
```

Here we can see several messages telling us which compartment the processor is currently simulating - this is helpful if the model is running over several hours.

To look at the results of the model there are two inbuilt functions. The first is **verification()** (see below) which gives a summary of the concentrations of the short chain fatty acids (SCFA) in each compartment, which are released as the microbes grow (averaged over the time period **start.av** to **fin.av**), as well as the fraction of the incoming water that reaches the end of the colon (should be about 0.1, i.e. 10%) and the microbial outflow from the colon (should be around 16 g/d). Note, TSCFA is the total SCFA.

```
#> Propionate (mM) 17.3 22.3 23.9
#> [1] "Fraction of the incoming water that leaves colon is 0.12"
#> [1] "fecal microbe output rate is 17.04 g/d"
```

Next we use **plotMPG()** to see a summary plot of the SCFA concentration, the mass of each microbial group and the pH in each model compartment.

plotMPG(m.out)



Changing host diet

A standard western diet is the default setting in the **microPopGut()** but this can be changed via the input arguments, **init** (i.e. the starting mass in each of the 3 model compartments) and **inflow** which is the mass inflow each day of carbohydrate, protein and water. Here you can also specify the division of carbohydrate into resistant starch and NSP using **RS.frac**. In this example we change from 10 g/d of protein to zero and add an extra 10 g/d to the carbohydrate default of 50 g/d. Results are shown in Fig. 1.

```
m.out=microPopGut(
    numDays=1,
    time.step=1/24/60,
    transitTime=1.25,
    microbeNames=c('Bacteroides', 'ButyrateProducers1'),
    microbeNames.short=c('Bacteroides'='B', 'ButyrateProducers1'='BP1'),
    #initial mass in each compartment
    init=list(
        C=2, #carbohydrate (g)
        P=0, #protein (q)
        B=10, #biomass (q)
        Acetate=0.3606, #g
        Propionate=0.1482, #q
        Butyrate=0.1762, #q
        W=100), #water (g)
    #inflow from diet
    inflow=list(
        C=60, #carbohydrate (g/d)
        P=0, #protein (q/d)
        W=1100, #water (q/d)
        RS.frac=0.78) #fraction of C that is resistant starch (rest is NSP)
)
time=m.out$solution[[1]][,'time']
verification(m.out,start.av=0.8*max(time),fin.av=max(time))
dev.new()
plotMPG(m.out)
```

Meal composition/fluctuations

The default setting in **microPopGut()** is constant inflow but there is also the option to include a more realistic inflow which aims to represent intermittent host eating. This is specified in the **meals** input list.

The **gamma.mag** option in the **meals** list controls the magnitude of the fluctuations in meal composition and size by controlling the spread of the gamma distribution that the values are drawn from for each substrate.

```
m.out=microPopGut(
    numDays=1,
    time.step=1/60/24,
    transitTime=1.25,
    microbeNames='Bacteroides',
    microbeNames.short=c('Bacteroides'='B'),
    meals=list(
        seed=1,
        fluc.inflow=TRUE,
        fluc.subst.comp=TRUE,
        plotInflow=TRUE,
        saveInflowFig=TRUE,
        breakfast.start=7, #time (24 h clock) to start breakfast
```



Figure 1: Summary results for a diet with no protein and 2 MFGs

```
lunch.start=13, #time (24 h clock) to start lunch
dinner.start=19, #time (24 h clock) to start dinner
meal.duration.h=0.5, #length of time eating one meal in hours
time.to.reach.colon.h=7, #time take to pass through stomach and small intestine in hours
gamma.mag=1 #scaling factor to control the fluctuations in meals
)
```

Figs. 2-4 shows meals over 7 days for gamma.mag equal to 0.1, 1 and 1.9 respectively for 3 arbitrary substrates A, B and C, and water. Note that after stochastically generating the composition the output is scaled so that the mean substrate values are maintained over the time period (this information is printed to screen when you run the model). Due to smoothing delays as the meals pass through the small intestine and stomach the final inflow to the colon may have slightly smaller means (this is also printed to screen).



Figure 2: Meal composition for gamma.mag=0.1



Figure 3: Meal composition for gamma.mag=1

The "meals" are then passed through an ODE model representing the stomach and small intestine - the amount of smoothing caused by this is controlled by the time.to.reach.colon.h item in the meals list. The fig. below shows the input to the colon for gamma.mag=1.9 and time.to.reach.colon.h=7 hours.

Full gut model (10 MFGs with meals for 7 days)

In this example we show the settings for simulating the full model. In this example we also change the pH tolerance and the maximum growth rate on resistant starch of the LactateProducers group. The code below



Figure 4: Meal composition for gamma.mag=1.9



Figure 5: Substrate inflows to colon (after passing through stomach and small intestine model) for gamma.mag=1.9 $\,$

takes over an hour to run so if you want to try it out it is better to change **num.days** from 5, to 1 or less, or to try fewer groups e.g. microbeNames=microbeNames[1:2].

```
microbeNames = c('Bacteroides', 'ButyrateProducers1',
                 'ButyrateProducers2', 'ButyrateProducers3',
                 'LactateProducers', 'PropionateProducers',
                 'Methanogens', 'NoButyFibreDeg',
                 'NoButyStarchDeg', 'Acetogens')
microbeNames.short = c('Bacteroides'='B', 'ButyrateProducers1'='BP1',
                    'ButyrateProducers2'='BP2', 'ButyrateProducers3'='BP3',
                    'LactateProducers'='LP', 'PropionateProducers'='PP',
                    'Methanogens'='M', 'NoButyFibreDeg'='NBFD',
                    'NoButyStarchDeg'='NBSD', 'Acetogens'='A')
#Change pH tolerance & Gmax(RS) for lactate producers
#read LPc from batch file
LactateProducers['pHcorners',2:5]=c(4.5,5.25,7.2,7.95)
LactateProducers['maxGrowthRate', 'RS']=7
m.out=microPopGut(
    numDays=5,
    time.step=1/24/60,
    transitTime=1.25,
    microbeNames=microbeNames,
    microbeNames.short=microbeNames.short,
    meals=list(
        seed=1,
        fluc.inflow=TRUE;
        fluc.subst.comp=TRUE,
        plotInflow=TRUE,
        saveInflowFig=TRUE,
        breakfast.start=7,
        lunch.start=13.
        dinner.start=19,
        meal.duration.h=0.5,
        time.to.reach.colon.h=7,
        gamma.mag=1
    )
)
```

See Fig. 6 for the results of **plotMPG(m.out)**

Bowel Movements

By default the model is set up for zero bowel movements per day (BMpd) i.e there is constant outlow. To turn on bowel movements, set **BMpd** in the **bowel.movements** input to either 1, 2 or 3 (see code below). The **start.BM.time** list gives the start times for 1, 2 or 3 bowel movements per day and the bowel movement duration is set using **BM.duration.h**. In our model we assume that bowel movements only affect the distal part of the colon.

```
microbeNames = c('Bacteroides', 'ButyrateProducers1', 'ButyrateProducers2', 'ButyrateProducers3', 'Lactat
microbeNames.short = c('Bacteroides'='B', 'ButyrateProducers1'='BP1', 'ButyrateProducers2'='BP2', 'ButyrateProducers1'='BP1', 'ButyrateProducers2'='BP2', 'ButyrateProducers1'='BP1', 'ButyrateProducers2'='BP2', 'ButyrateProducers1'='BP1', 'ButyrateProducers2'='BP2', 'ButyrateProducers1'='BP1', 'ButyrateProducers2'='BP2', 'ButyrateProducers1'='BP1', 'ButyrateProducers2'='BP2', 'ButyrateProducers2'='BP2', 'ButyrateProducers1'='BP1', 'ButyrateProducers2'='BP2', 'ButyrateProducers2'='BT4', 'ButyrateProducers2'='BT4', 'ButyrateProducers2'='BT4', 'ButyrateProducers2'='BT4', 'ButyrateProducers2'='BT4', 'BT4', 'BT
```



Figure 6: Summary results for 10 MFGs over 5 days

```
sim.time.h=48 #time to simulate in hours
m.out=microPopGut(
   numDays=sim.time.h/24,
   time.step=1/24/60,
   transitTime=1.25,
   microbeNames=microbeNames[1:2],
   microbeNames.short=microbeNames.short[1:2],
    bowel.movements = list(
        BM.duration.h = 15/60,
        frac.distal.emptied = 0.9,
        BMpd = 3,
        start.BM.time = list(7, c(7, 19), c(7, 15, 21)))
)
time=m.out$solution[[1]][,'time']
verification(m.out,start.av=0.8*max(time),fin.av=max(time))
dev.new()
plotMPG(m.out)
```

Multiple strains per group

By default there is only one strain in each MFG but using the functionality of microPop (on which microPopGut is based) we can add multiple strains in each group. In versions of microPop from 1.6 onwards we can have different numbers of strains in each group. The parameters for each strain in a group are drawn randomly from a given range for that particular group. The particulars of this are controlled by the **strainOptions** input argument.

```
m.out=microPopGut(
   numDays=2,
   time.step=1/24/60,
   transitTime=1.25,
   microbeNames=c('Bacteroides', 'ButyrateProducers1'),
   microbeNames.short=('Bacteroides'='B', 'ButyrateProducers1'='BP1'),
   numStrains=c('Bacteroides'=3,'ButyrateProducers1'=2),
    strainOptions = list(
        randomParams = c("halfSat", "yield", "maxGrowthRate",
        "pHtrait"),
        seed = 3,
        distribution = "uniform",
        percentTraitRange = 10,
        maxPHshift = 0.1,
        applyTradeOffs = FALSE,
        tradeOffParams = NULL,
        paramsSpecified = FALSE,
        paramDataName = NULL)
)
time=m.out$solution[[1]][,'time']
```



Figure 7: Summary results for 2 MFGs over 2 days with 3 bowel movements per day



verification(m.out,start.av=0.8*max(time),fin.av=max(time))
plotMPG(m.out)

Figure 8: Summary results for 2 MFGs: Bacteroides with 3 strains and ButyrateProducers1 with 2 strains

Troubleshooting

Failure of ODE solver

If you get warnings about time steps then this mean the ODE solver is failing - generally because the problem is too stiff i.e. there are rapid changes in time. Ways to deal with this are to make your time step

(microPopGut input argument) smaller, to make gamma.mag smaller (nearer to zero) which will decrease the size of the meal fluctuations, or to alter the tolerances in the ODE solver (see ode.options list of microPopGut input arguments). If you are running the system with only one group, adding more groups often makes the system more stable as this slows down the growth of each individual group due to resource competition.

Supp. Info. for "Process-based modelling of microbial community dynamics in the human colon"

Helen Kettle, Petra Louis and Harry J. FLint

July 1, 2022

1 1 Mathematical Model

² 1.1 Simple Model

In this section we present a very simple model with one microbial group and
one colon compartment that we then use to derive bounds on parameters (e.g.
absorption of SCFA and water) and to look at the bulk properties of the system,
e.g. the relationship between transit time and SCFA concentration.

This simple model consists of, bacteria (X), substrate (S), SCFA mass (Z)and water (W) all with units of mass. We set f_s as the fraction of the waste products of X that are SCFA, and Y is the amount of microbial growth for 1 g of S and a_Z and a_W are the absorption rates of Z and W. The rates of change are given by

$$\frac{dX(t)}{dt} = G(t)X(t) - X(t)V$$
(1)

$$\frac{dS(t)}{dt} = \dot{S_{in}} - \frac{G(t)X(t)}{Y} - S(t)V$$
(2)

$$\frac{dZ(t)}{dt} = f_s \left(\frac{1}{Y} - 1\right) G(t) X(t) - (V + a_Z) Z(t)$$
(3)

$$\frac{dW(t)}{dt} = \dot{W}_{in} - (V + a_W)W(t) \tag{4}$$

where microbial growth, G, is given by

$$G(t) = G^m \frac{S(t)}{S(t) + K} \tag{5}$$

where K is the half-saturation constant and G^m is the maximum growth rate of X on S. Transit time is incorporated via the washout rate, V such that $V = 1/T_t$.

Steady state analysis (i.e. when the system is not changing with time) of the one group model can be used to give us some bounds or checks on the bulk properties of the system. The steady state solution (at time, t_s), assuming X > 0, is given by

$$X(t_s) = (\dot{S_{in}}/V - S(t_s))Y \tag{6}$$

$$S(t_s) = \frac{VK}{G^{\max} - V} \tag{7}$$

$$Z(t_s) \approx VX(t_s) \frac{1-Y}{Y(a_Z+V)}$$
(8)

$$W(t_s) = \frac{\dot{W}_{in}}{a_W + V} \tag{9}$$

where $\dot{X_{in}}$ is the inflow rate of X. 20

1.2Microbial yield and substrate inflow 21

Assuming the microbes consume all available substrate, then the steady state 22 mass of microbes can be approximated by 23

$$X(t_s) \approx \frac{\dot{S}_{in}Y}{V} \tag{10}$$

where S_{in} is the dietary inflow of all substrates (i.e. dietary P, C and mucin); V 24 is the wash out rate from the system and Y, the microbial yield. Assuming the 25 output of microbes (given by $X_{t_s}V$) is 14-28 g d⁻¹ (Stephen and Cummings, 26 1980) (with midpoint of 21) and the substrate inflow is about 65 g d^{-1} ; Eq. 10 27 suggests that Y is 21/65 i.e. about 0.3 which matches very well with the yield 28 values for our functional groups which have yield values around 0.28 or 0.33 (see 29 other Supp. Info. file). 30

Specific water absorption, a_W 1.331

Extending Eq. 9 to N compartments with downstream flow from 1 to N, and 32 assuming the specific absorption rate is the same in all, then at steady state the 33 water in each compartment is given by, 34

$$W_1 = \frac{\dot{W}_{in}}{a_W + V_1},$$
 (11)

$$W_2 = \frac{W_1 V_1}{a_W + V_2}, \dots$$
(12)

...,
$$W_N = \frac{W_{N-1}V_{N-1}}{a_W + V_N}$$
 (13)

Successively substituting for the unknowns gives 35

$$W_N = \frac{W_{in}V_1V2...V_{N-1}}{(a_W + V_1)(a_W + V_2)...(a_W + V_N)}$$
(14)

If 90% of water is absorbed over the transit time then in the last compartment, $N, W_N V_N = 0.1 \dot{W}_{in}$. Substituting this into Eq. 14 gives 37

$$\prod_{k=1}^{N} (a_W + V_k) = 10 \prod_{j=1}^{N} V_j.$$
(15)

- This can be solved numerically where V_j is computed by dividing the colon into N compartments which each take fraction, f_j^T , of the total transit time to pass 38
- 39



Figure S1: a) Achieving 90% water absorption for different transit times (1, 1.5 and 2 days represented by solid, dashed and dotted line respectively) and different number of compartments (1, 2, and 3 by colour, as shown in legend). The dotted horizontal line shows the required value for 90% incoming water absorption in the colon and the vertical blue lines show the a_W value which gives the correct total absorption for the 3 different transit times (which are as before, 1, 1.5 and 2 days represented by solid, dashed and dotted line respectively). b) Investigating SCFA absorption. TSCFA (mM) for different a_Z for transit time of 1.25 days, for the one group, three compartment model. a_Z is from 1,2,...30 /d with values constant throughout the colon. The dashed horizontal lines show the expected TSCFA in each compartment. The simulation is for 5 days and the results are the mean over the last day. Constant inflow and outflow (no meals or bowel movements) with a_W changing with transit time according to Eq. 16.

through. Using fractional times based on compartment volume (Fig. 1 in main manuscript) and assuming that a_W is the same in each compartment we find that for a one compartment model, $a_W = \frac{9}{T_t}$; for a two compartment model, $a_W = \frac{4.59}{T_t}$; and for a three compartment model, $a_W = \frac{3.72}{T_t}$ (see Fig. S1). This can be expressed exactly by

$$a_W = \frac{16.95 - 9.72N + 1.77N^2}{T_t} \tag{16}$$

where N is the number of compartments in the model. Note that this does 45 not mean that specific water absorption changes with transit time, rather that 46 to fulfill the 90% absorption criteria we can set a_W based on N and T_t . Once 47 a typical transit time is chosen, the value of a_W can be fixed. As a rough 48 estimation, $a_W \approx 3$ /d for a 3 compartment model with a transit time between 49 one to one and a half days (Fig. S1). Given this will not be significantly 50 affected by the microbial model (microbial uptake/production of water is small) 51 this result will apply to all of the models in this work. 52

⁵³ 1.4 Specific SCFA absorption, a_Z

Using our one group microbial group model but adapted for 3 compartments, and our estimation for a_W based on transit time and the number of compartments (Eq. 16), we run the model for a transit times of 1.25 d with continuous inflow and outflow, over a range of a_Z from 1-30 d⁻¹. We compute TSCFA from our model by converting Z from g to mM using

$$Z_{mM} = 10^6 \frac{Z_g}{W_g m_Z} \tag{17}$$

where m_Z is computed by assuming TSCFA is in the ratio 3:1:1 (Ac:Bu:Pr) 59 to give a weighted mean molar mass of TSCFA, m_Z of 68.4 g mol⁻¹. Fig. S1, 60 shows the TSCFA in each model compartment versus a_Z . The horizontal dashed 61 lines show the TSCFA value matching the model criteria, indicating the best 62 estimates were a_Z equal to 25.2, 4.2 and 9.2 d⁻¹ in the proximal, transverse 63 and distal colon respectively. However, this was determined using a_Z constant 64 through the colon so if a_Z varies between compartments this will change the 65 results. In the interests of a robust model (i.e. the fewer parameter values, the 66 better) we made the decision to use one value for a_Z . Given the experimental 67 value of 9.6 d^{-1} compares well with our best estimate for the distal colon (9.2) 68 d^{-1}) we decided to set aZ =9.6 d⁻¹ throughout. It should be noted however 69 that decreasing a_Z along the colon has been implemented in other models e.g. 70 Labarthe et al. (2019). 71

72 2 Effect of Transit Time

⁷³ Experimental evidence (e.g. (Lewis and Heaton, 1997)) shows that TSCFA ⁷⁴ (mM) decreases as transit time increases. We can explain why this is, mathe-⁷⁵ matically, using a very simple one group model with monod growth, which we ⁷⁶ can solve analytically at steady state. To compute TSCFA in mM we need to ⁷⁷ use the fraction of P that is SCFA and then divide by the mean molor mass ⁷⁸ (m_m) and multiply by 1000 to find mmol. We then need to divide by W in litres, ⁷⁹ thus,

$$TSCFA = 10^6 \frac{Pf_s}{Wm_m}$$
(18)

Substituting for P and W, ignoring scaling constants and assuming remaining substrate at steady state is negligible, shows that TSCFA is linearly related to the expression

$$\frac{\dot{S}_{in}}{\dot{W}_{in}}\frac{a_W + V}{a_P + V} \tag{19}$$

To see the effect of simply changing the transit time through the colon on TSCFA we assume \dot{S}_{in} and \dot{W}_{in} are fixed and replace V by 1/Tt to get

$$TSCFA \propto \frac{a_W T_t + 1}{a_P T_t + 1} \tag{20}$$

- Since we have $a_W=3$ and $a_P=9.6$, the denominator will increase much faster
- $_{\tt 86}$ $\,$ than the numerator as T_t increases thus, theoretically, TSCFA will decrease as
- ⁸⁷ transit time increases as SCFA are absorbed faster than water. Using realistic



Figure S2: TSCFA as a function of transit time obtained from the solution of Eqs. 2-4. We convert from product mass, P, to moles using the average molar mass (weighted according to A:B:P = 3:1:1) of 68.5 g/mol and compute f_s as an average of the microPop microbial group stoichiometries to be approximately 0.5. We set inflowing substrate at 65 g/d (dietary substrate plus mucin) and inflowing water at 1100 g/d, with parameter values Y=0.3, $G^{\text{max}}=20$ /d and K=0.001. [transitTimeModel.R]

parameter values in the above model (Eq. 2-4) allows us to plot TSCFA against
transit time – see Fig S2 which compares very well with the experimental data
shown in Fig. 1 by Lewis and Heaton (1997).

⁹¹ 3 Microbial group parameter values

The parameters describing the different microbial groups are the same as the 92 intrinsic functional groups given in the microPop R package (version 1.6), with 93 one exception. We increased the maximum growth rate of Lactate Producers 94 on RS from 6 d^{-1} to 7 d^{-1} and their pH tolerance were cordinates changed 95 to tolerate lower pH (first two pH coordinates now 4.5 and 5.25, rather than 96 4.95 and 5.7) to ensure a better chance of their survival in the model. This 97 section shows the data frames used for each microbial group in microPopGut. 98 The following list explains the different entries in these data frames. 99

- 'Rtype' refers to the substrate type on the pathway:
- ¹⁰¹ 'X': not involved in pathway
- 'S': substitutable substrate (this can be interchanged with other sub stitutable substrates)
- 'Se': essential substrate (the microbes can not grow without this)
- 'Sb': boosting substrate (if this is present the microbe can grow faster)

107 – 'Sw': water

108

- 'P': metabolic product

• 'halfsat' is the half saturation constant for monod growth

- 'yield' is the microbial mass produced from one gram of substrate
- 'maxGrowthRate' is the specific maximum growth rate of the microbes
- 'stoichiom' refers to the number of moles of each molecules involved in growth
- 'keyResource' is the substrate whose uptake rate is used to compute the uptake of the other substrates on the pathway according to the stoichiom etry
- 'numPathways' defines how many metabolic pathways the microbial group has. When there is more than one pathway, numbered parameter names for the subsequent pathways are used.

For more details please refer to Kettle et al. (2015) and Kettle et al. (2018) or use the help function within the microPopGut package.

Table 1: Bacteroides										
	units	Protein	NSP	RS	Acetate	Propionate	Succinate	H2	CO2	other
Rtype	none	Х	S	S	Р	Р	Р	Р	Р	Х
halfSat	g/l		0.001	0.001						
yield	g/g		0.286	0.333						
maxGrowthRate	/d		12	24						
stoichiom	mol		2	2	2	1	1	2	1	
keyResource	none									
numPathways	none	2								
Rtype.2	none	S	Х	Х	Р	Р	Р	Р	Р	Р
halfSat.2	g/l	0.001								
yield.2	g/g	0.2								
maxGrowthRate.2	/d	24								
stoichiom.2	mol	6			2	1	1	2	1	7
keyResource.2	none									
pHcorners	pН	5.6	6.35	7.85	8.6					

Table 2: NoButyStarchDeg

	units	NSP	RS	Acetate	H2	CO2	H2O
Rtype	none	\mathbf{S}	S	Р	Р	Р	Sw
halfSat	g/l	0.001	0.001				
yield	g/g	0.286	0.333				
\max GrowthRate	/d	3.6	14.4				
stoichiom	mol	1	1	2	4	2	2
keyResource	none						
numPathways	none	1					
pHcorners	pН	5.35	6.1	7.6	8.35		

Table 3: NoButyFibreDeg								
	units	NSP	\mathbf{RS}	Acetate	Succinate	H2		
Rtype	none	S	S	Р	Р	Р		
halfSat	g/l	0.001	0.001					
yield	g/g	0.286	0.333					
maxGrowthRate	/d	16.8	3.6					
stoichiom	mol	1	1	1	1	1		
keyResource	none							
numPathways	none	1						
pHcorners	pН	5	5.75	7.25	8			

 Table 4: LactateProducers

Table 4: LactateProducers									
	units NSP RS Sugars Acetate Lactate Formate Ethanol H2O								
Rtype	none	S	S	S	Р	Р	Р	Р	Sw
halfSat	g/l	0.001	0.001	0.001					
yield	g/g	0.286	0.333	0.333					
maxGrowthRate	/d	7.2	7	24					
stoichiom	mol	6	6	6	10	4	2	1	1
keyResource	none								
numPathways	none	1							
pHcorners	pН	4.5	5.25	7.2	7.95				

 Table 5: ButyrateProducers1

		1001	с о. р	augrater	roudcon) 1			
	units	NSP	RS	Sugars	Acetate	Butyrate	H2	CO2	H2O
Rtype	none	S	S	S	Sb	Р	Р	Р	Р
halfSat	g/l	0.001	0.001	0.001	0.001				
yield	g/g	0.286	0.333	0.333					
maxGrowthRate	/d	8.4	8.4	24					
stoichiom	mol	2	2	2	2	3	2	4	2
keyResource	none	Hex							
numPathways	none	1							
nonBoostFrac	none	0.75							
pHcorners	pН	4.95	5.7	7.2	7.95				

 Table 6: ButyrateProducers2

	units	NSP	RS	Sugars	Acetate	Butyrate	Lactate	Formate	CO2	H2O
Rtype	none	S	S	S	Sb	Р	Р	Р	Р	Р
halfSat	g/l	0.001	0.001	0.001	0.001					
yield	g/g	0.286	0.333	0.333						
maxGrowthRate	/d	14.4	7.2	24						
stoichiom	mol	6	6	6	4	7	2	6	4	4
nonBoostFrac	none	0.1								
keyResource	none	Hex								
numPathways	none	1								
pHcorners	$_{\rm pH}$	4.85	5.6	7.1	7.85					

Table <i>i</i> : PropionateProducers											
	units	NSP	RS	Sugars	Acetate	Propionate	CO2	Lactate	H2O		
Rtype	none	S	S	S	Р	Р	Р	Х	Р		
halfSat	g/l	0.001	0.001	0.001							
yield	g/g	0.286	0.333	0.333							
maxGrowthRate	/d	7.2	7.2	24							
stoichiom	moles	3	3	3	2	4	2		2		
keyResource	none										
numPathways	none	2									
Rtype.2	none	Х	Х	Х	Р	Р	Р	Se	Р		
halfSat.2	g/l							0.001			
yield.2	g/g							0.111			
maxGrowthRate.2	/d							4.8			
stoichiom.2	moles				1	2	1	3	1		
keyResource.2	none	Lactate									
pHcorners	pH	4.75	5.5	7	7.75						

Table 7. PropionateProdu

 Table 8: ButyrateProducers3

	units	NSP	RS	Sugars	Acetate	Butyrate	Formate	H2	CO2	Lactate	H2O
Rtype	none	S	S	S	Р	Р	Р	Р	Р	Х	Sw
halfSat	g/l	0.001	0.001	0.001							
yield	g/g	0.286	0.333	0.333							
maxGrowthRate	/d	7.2	7.2	24							
stoichiom	mol	10	10	10	2	9	12	10	8		2
keyResource	none										
numPathways	none	2									
Rtype.2	none	Х	Х	Х	Se	Р	Х	Р	Р	Se	Р
halfSat.2	g/l				0.001					0.001	
yield.2	g/g									0.111	
maxGrowthRate.2	/d									4.8	
stoichiom.2	mol				2	3		2	4	4	2
keyResource.2	none	Lactate									
pHcorners	pН	4.85	5.6	7.1	7.85						

Table 9: Acetogens

Table 9: Acetogens										
	units	NSP	RS	Sugars	Acetate	H2	CO2	Formate	H2O	
Rtype	none	\mathbf{S}	S	S	Р	Х	Х	Х	Х	
halfSat	g/l	0.001	0.001	0.001						
yield	g/g	0.286	0.333	0.333						
maxGrowthRate	/d	7.2	7.2	24						
stoichiom	moles	1	1	1	3					
keyResource	none									
numPathways	none	3								
Rtype.2	none	Х	Х	Х	Р	Se	Se	Х	Р	
halfSat.2	g/l					0.001	0.001			
yield.2	g/g						0.03			
maxGrowthRate.2	/d						2.4			
stoichiom.2	moles				1	4	2		2	
keyResource.2	none	CO2								
Rtype.3	none	S	S	S	Р	Р	Р	Se	Х	
halfSat.3	g/l	0.001	0.001	0.001				0.001		
yield.3	g/g	0.286	0.333	0.333						
maxGrowthRate.3	/d	7.2	7.2	24						
stoichiom.3	moles	1	1	1	3	2	2	2		
keyResource.3	none	Hex								
pHcorners	pН	5.25	6	7.5	8.25					

	units	H2	CO2	CH4	H2O	Formate
Rtype	none	Se	Se	Р	Р	Х
halfSat	g/l	0.001	0.001			
yield	g/g		0.03			
maxGrowthRate	/d		2.4			
stoichiom	mol	4	1	1	2	
keyResource	none	CO2				
$\operatorname{numPathways}$	none	2				
Rtype.2	none	Х	Р	Р	Р	Se
halfSat.2	g/l					0.001
yield.2	g/g					0.00724
maxGrowthRate.2	/d					2.4
stoichiom.2	mol		3	1	2	4
keyResource.2	none	Formate				
pHcorners	pН	5.25	6	7.5	8.25	

Table 10: Methanogens

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