



Marching bifurcations

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ABSTRACT

This paper dedicated to my late mum and dad (Ludwika and Karol Wiercigroch), presents a light-hearted account of important events in my academic career, which have influenced my development and contributed to my achievements. It meant to be published on the occasion of my round birthday, which celebration was delayed by COVID-19 pandemic and some other factors. Predominantly, it is based on a booklet I wrote in 2013 on the occasion of bestowing on me a title *a doctor honoris causa* by the Technical University of Lodz (LUT) of my native Poland. The main focus of this piece is the friendship and interactions with my academic colleagues around the world and in particular with Professor Tomasz Kapitaniak of the LUT. In mathematics, a bifurcation is a qualitative change in a solution, wherein a march is not only a synonym of a periodic excitation but also the passing time. In this context, a bifurcation being a qualitative change has a major influence on the global solution. This definition resonates well a much wider context and this paper attempts to provide some examples.

1. Bifurcations in life: A short and biased research autobiography

In the language of mathematics a bifurcation is a qualitative (structural) or topological change of the solution. Bifurcations can be divided as sub and supercritical. The former are more dangerous and can lead to catastrophic effects not only in the language of mathematics. From the stability point of view, we can distinguish among others the following standard types of bifurcations: saddle-node, period doubling, pitchfork and Hopf. A rather unusual type is a grazing bifurcation, which occurs in impacting oscillators, which I and my group have been thoroughly investigating for many years and have managed to get some new insights introducing so-called grazing induced bifurcations (e.g. [23,29–31,37,40,45,48,55]).

Marching Bifurcations is a light-hearted account of important events in my career and life, which influenced my development and contributed to my achievements. I was born on 14 July 1960 in Rajcza in working class family and was the second son of my late parents, Ludwika and Karol Wiercigroch. From the earlier years, I have shown a significant interest and talent in mathematical and physical sciences. I was very interested in chemistry taking parts in the primary school Olympiads and carried out many chemical experiments, often dangerous, but luckily without any lasting consequences. In this period, I was also a keen altar boy being significantly influenced by the charismatic cardinal of Krakow, the late pope, John Paul II (Karol Wojtyła) and my local priest, Reverend Stanislaw Bajer.

As a high school I chose the Technical High School in Żywiec, the best high school in mathematical and physical sciences in terms of spatiotemporal location. This choice allowed me to deepen the knowledge in hard sciences, specifically in mathematics and mechanics, having at the same time a good practical grounding. Time spent in Żywiec had also a beneficial effect on the development of my shy personality at that time. A vastly positive influence in these formative years had my Head Teacher and an acknowledged expert in design, late Mr Eugeniusz Wrzeszcz. I graduated from the high school not only with flying colours, but as the best graduate I was given a free entry to any Polish university. The second free entry came from being a laureate of the National Competition for the Best Technical Projects, which was held in 1980 in the capital Warsaw.

The choice of my degree programme and university can be described as the first important bifurcation of the subcritical type. In that time two people had made a very strong influence on my future activities, namely, the Reverend Franciszek Pieczka and Mr Piotr Wiercigroch. The Reverend Pieczka led a seminary workshop aimed to deepen the Christian faith and to recruit new adepts to the Krakow Seminary. Mr Piotr Wiercigroch, my God father, a distinguished inventor and engineer with some 30 patents, was a strong supporter of the Warsaw Military Academy of Technology.

First, I considered the Theological Seminary of Krakow Archdiocese and the Warsaw Military Academy of Technology, but after the visits to both institutions, I quickly decided to subcritically bifurcate to the Applied Mathematics and Theoretical Physics Faculty of the Silesian

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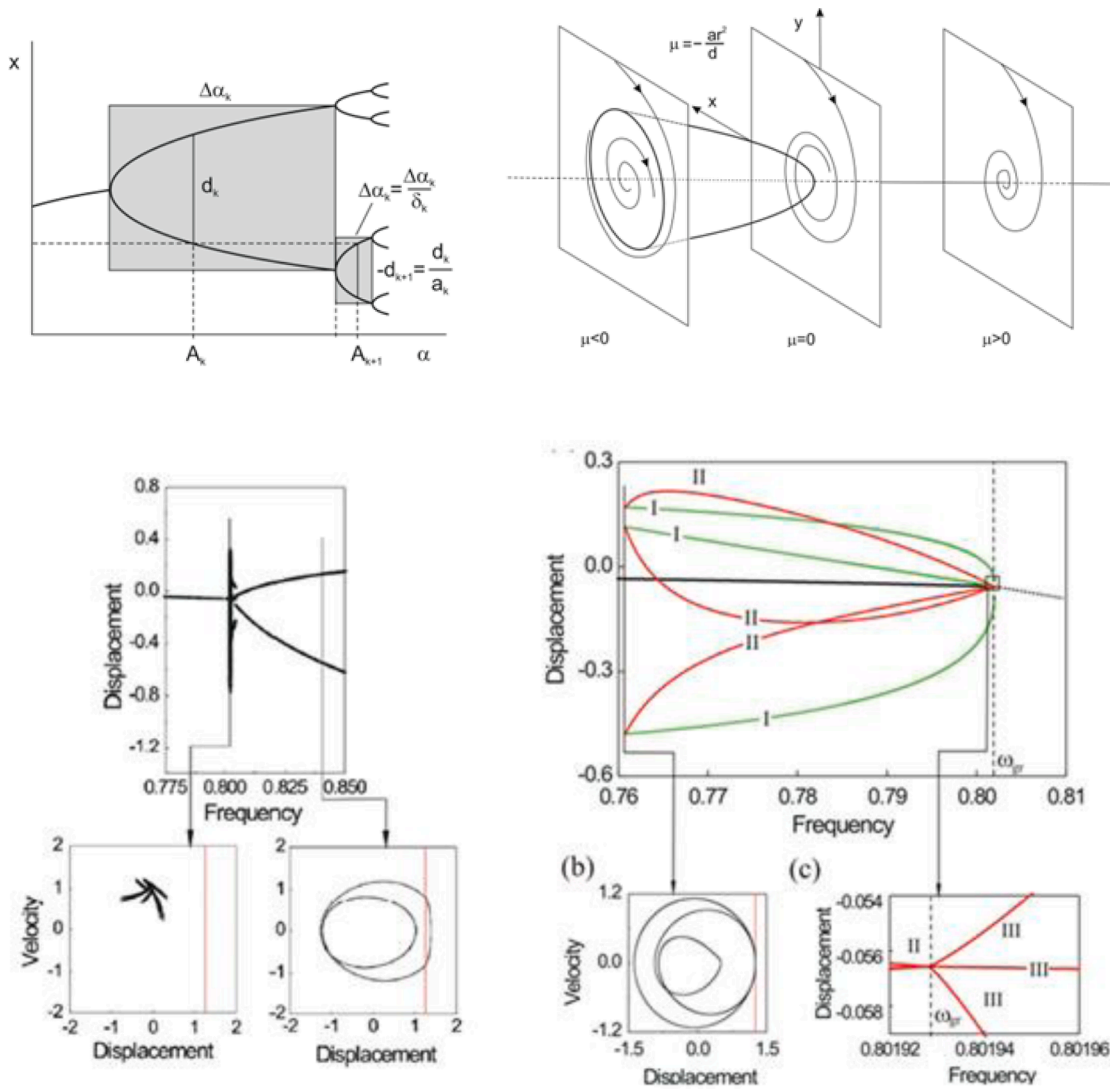


Fig. 1. The upper panel shows examples of typical bifurcations of period doubling (left) and Hopf type (right). The lower panels depict grazing induced bifurcations investigated thoroughly by my research group, where on the left and right hand sides the modelling and experimental results are shown (e.g. [29–31]).



Fig. 2. The first two from the left photographs were taken in 1972 when I was in the primary school, when my church in Rajcza was celebrating a millennium of Cracovian diocese. On the very left is my school ID photograph; on the right is a photograph of the millennium celebration mass during which I was serving. The ID photograph on the right was taken during the final year in the high school.

University of Technology. The Warsaw Military Academy of Technology was very persistent and keen to get me enrolled, which I managed to escape. The next bifurcation was saddle-node type to a stable solution, the Mechanical-Technological Faculty of the same University, from

which I graduated in 1985 with the first class (see the right panel of Fig. 3). My specialization was machine tools and other technological machinery. Just after my graduation I was offered an assistantship in the Machine Tools Department led by a late Professor Tadeusz Tyrlik.

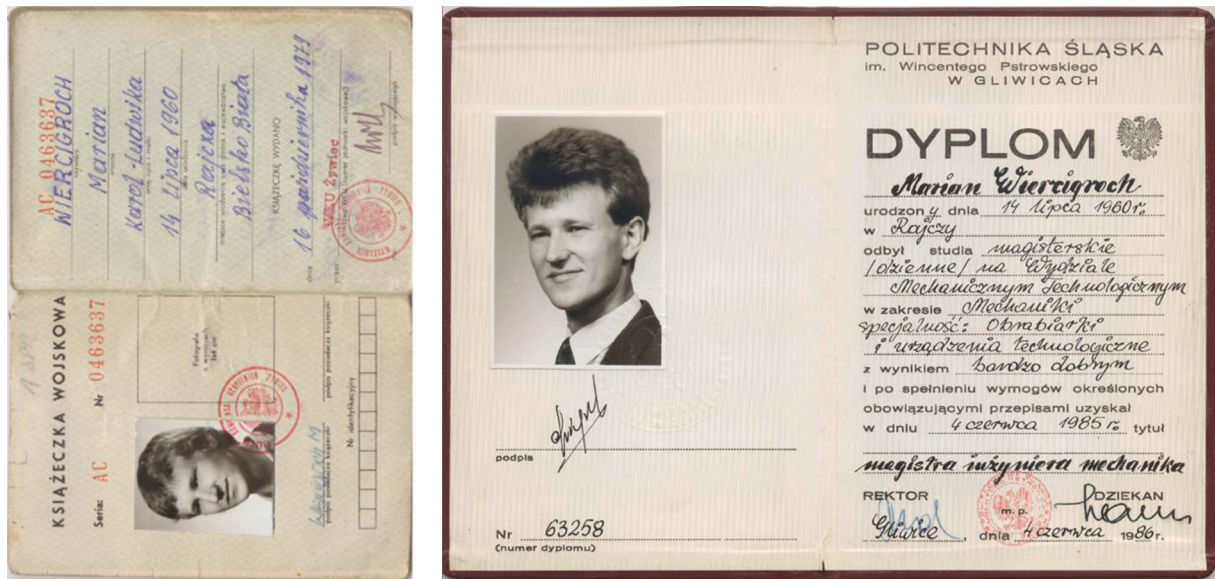


Fig. 3. On the left is my military record book from 16 October 1979, the time when I passed the medical check-ups and was eligible to serve in the Polish Army; on the right is my alma mater graduation certificate specifying the field of mechanical engineering and the first class degree obtained on 4th June 1985 and issued on 4th June 1986.



Fig. 4. Soldiers meeting in Kyoto in November 2011 during the historical conference, IUTAM Symposium on 50 Years of Chaos and Beyond, organised to celebrate the discovery of the Japanese attractor by Professor Yoshisuke Ueda.

In that time, personal computers and computational methods have been under a vast and rapid development. To illustrate this point, I did all computations for my master project on quasi-statics of the cutting process supervised by Professor Jan Kosmol, on a microcomputer ZX-81. Thereafter I had an access to a more graphically advanced ZX Spectrum to finally get my hands on my first IBM PC. From this point on, I had started a long running and passionate *flirt* with computers and scientific computations. In that time I wrote my own code in Pascal to simulate dynamics of discrete dynamical systems. This code proved to be useful in lots of projects in the area of dynamics.

On 4 January 1986 I started one year military training (see the left

panel of Fig. 3 with the photograph page of my military record book) aimed for future officers in the Army Regiment located in Chełmno Pomorskie. At that time I have experienced a global bifurcation, which has changed my attitude to science and approach to life, from somehow linear to dominantly nonlinear, which occasionally goes chaotic.

This bifurcation was caused by Professor Tomasz Kapitaniak, a close friend and colleague, whom I met in Chełmno Pomorskie for the first time and with whom we have been meeting regularly in various locations around the world (see photograph from 2011 meeting in Kyoto shown in Fig. 4). At that time he was a private lieutenant, with a PhD degree, and now he is an internationally renowned scientist and a full member of the

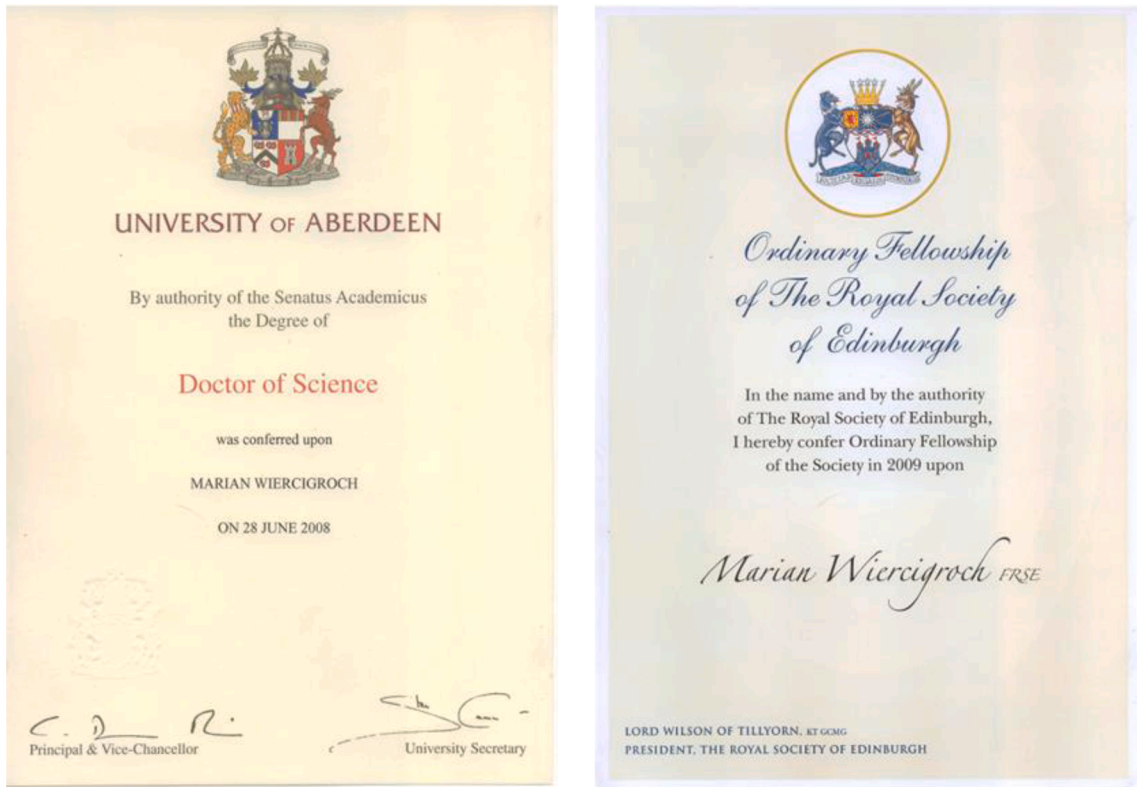


Fig. 5. On the left, a DSc degree certificate conferred in 2008; on the right a certificate of being elected a Fellow of the Royal Society in Edinburgh from 2009.



Fig. 6. Left panel presents a photograph from the annual meeting of the Centre for Applied Dynamics Research held in Linklater Rooms on 25 October 2006. In the front row from the left: Dr Ekaterina Pavlovskaja, Adriane Schelin, Professors Celso Grebogi and Michael Thompson, Elena Sitnikova, Marian Wiercigroch (CADR Director), Dr Dragan Jovicic. In the middle row from the left: Dr Kaliyaperumal Nakkeeran, Marko Keber, Scott Davidson, Drs Andrew Starkey, Alessandro de Moura, Qingjie Cao, Gyorgy Karolyi and Charles Wang, Tamas Bodai, Bryan Horton, Ravindran Manoharan. In the back row from the left: Olusegun Ajibose, Ronny Sternberger, Nick Burns, Christian Rodriguez, Paulo Bonifacio, Dr Jan Sieber and James Ing. Right panel photograph is from the Graduation ceremony held in July 2004 at the University of Aberdeen. From the left the former Rector (Lord Wilson, the former Governor of Hong Kong), honorary graduate (Professor Mike Thompson) and the Promoter (myself).

Polish Academy of Sciences. From that time on I started my *swift military scientific march*. In 1991 I defended with a distinction my PhD thesis entitled ‘Modelling of dynamic interactions in metal cutting based on the turning process on a horizontal boring-milling machine’. The work was supervised by the late Professor Tadeusz Tyrlik. Just after I accepted the invitation extended by late Professor Allan Barr FRSE to join the University of Aberdeen as a postdoctoral research fellow, which was a crucial decision in my career. In 1994 I underwent a pitchfork bifurcation, namely, I was awarded a Senior Fulbright Fellowship, wrote a

habilitation dissertation on ‘Dynamics of Discrete Mechanical Systems with Discontinuities’, and was appointed a lecturer at the University of Aberdeen.

In parallel to the Fulbright Scholarship at the University of Delaware, I was also a lecturer at the University of Aberdeen, supervising undergraduate projects. At that time the main means of communication for large documents exchange was fax. This led to numerous long fax transmissions between Universities of Aberdeen and Delaware, causing a few problems for secretaries. In the middle of 1996 just after

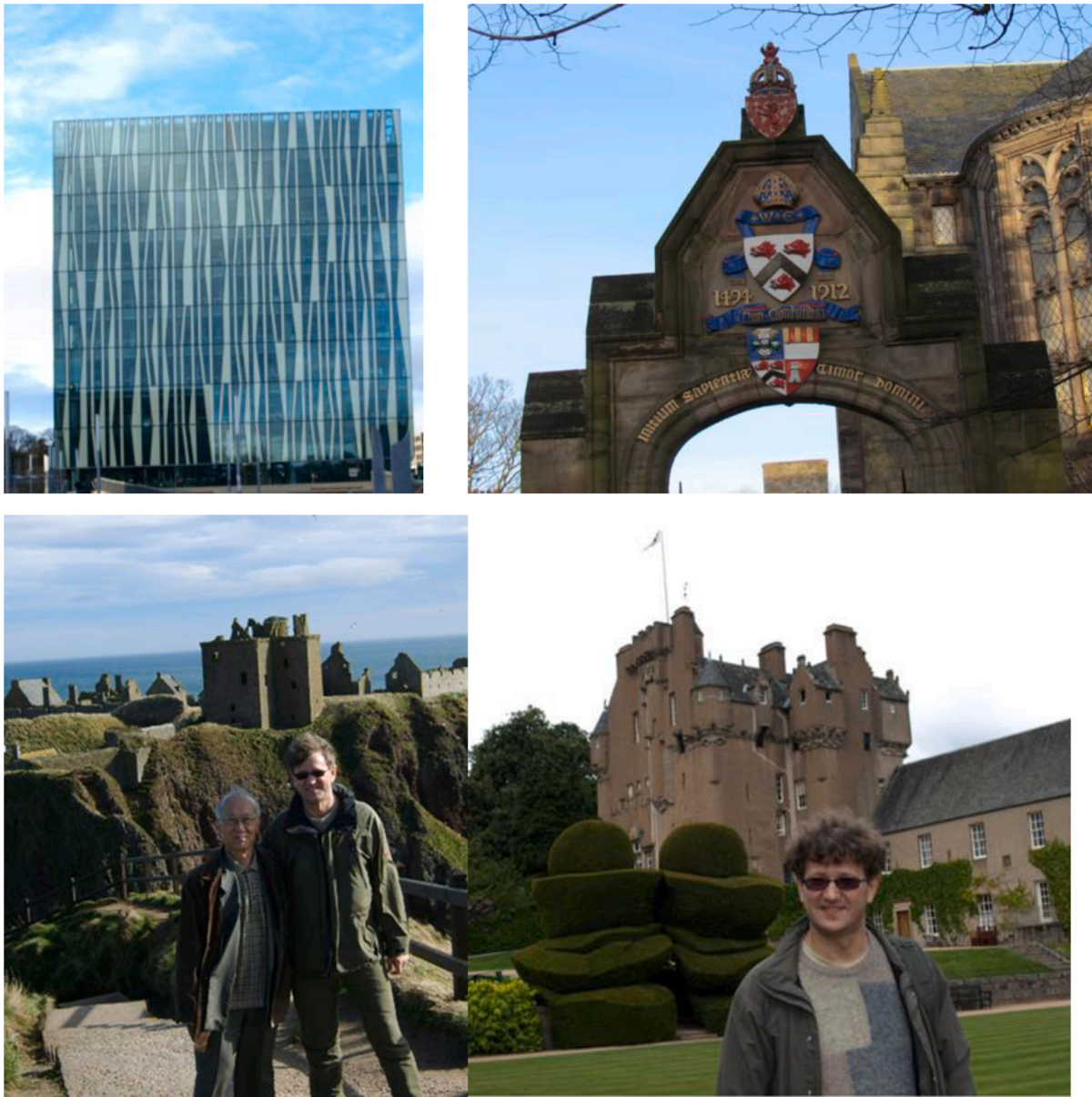


Fig. 7. Upper left panel depicts the Sir Duncan C Rice Library and the upper right the gate to the New Kings buildings at the University of Aberdeen. At the bottom left, with my colleague and friend, Emeritus Professor Yoshi Ueda of Kyoto University, who discovered chaos in 1961, at the front of dramatic ruins of medieval Dunnotar Castle. On the right bottom at the front of the Crathes Castle located in the Royal Deeside.

completing my Fulbright Scholarship and a research project sponsored by the Office of Naval Research, I returned to Scotland and started to build my research group.

Since then I have been promoted through the ranks to a senior lecturer in 1999, reader in 2000 and to a personal chair in 2002. Four years later in 2006, in the frame of the Sixth Century Campaign, I was promoted to a Sixth Century Chair for my scholarly contributions and international reputation in the field of applied dynamics. According to my many colleagues, I have excelled as a talented administrator and organizer. Among others, I served as a Head Engineering at the University of Aberdeen between 2003 and 2007, when Aberdeen Engineering had grown significantly in research strength with appointments of Professors Steve Reid, Michael Thompson and Celso Grebogi.

In 2008 I obtained the highest academic degree in the British system (see the left panel of Fig. 5), a Doctor of Science from the University of Aberdeen for a monograph entitled *Engineering Dynamics of Non-smooth Mechanical Systems: Modelling, Analysis and Experimental Studies*, which was based on a selection of my works published in the best peer review

journals. This monograph presents a systematic approach to modeling, analysis, verification and design of strongly nonlinear dynamical systems. In 2009 for my contribution to nonlinear dynamics and its applications, I was elected a Fellow of the Royal Society of Edinburgh, the Scotland National Academy (see the right panel of Fig. 5).

2. Research interests and place of work

My research interests are focused on advancing understanding of engineering and physical systems undergoing complex dynamical phenomena involving nonlinear resonances. And throughout my career, I have been very fortunate and privileged to tackle a broad spectrum of fundamental and applied problems originating from mechanics and engineering systems. Most of them have had a strong focus on dynamics and vibration of predominantly mechanical systems in form of structures and processes. These investigations can be grouped into four major categories, namely, non-smooth [1–117] and smooth [118–158] dynamical systems, dynamics and control [159–165], and solid



Fig. 8. A group photograph from the first international conference on nonlinear mechanics entitled *Recent Advances in Nonlinear Mechanics* organized at Aberdeen in August 2005. The conference attracted the international authorities in dynamics (e.g. Prof Philip Holmes, Princeton; Prof JMT Thompson, UCL; Prof G Rega, Rome), solid mechanics (Prof John Willis, Cambridge) and fluid mechanics (Prof Paul Manneville, Paris). The picture was taken in the background of the King College Chapel, the oldest building of the University of Aberdeen.

mechanics [166–179]. The studies on non-smooth dynamical systems dynamics, can be further divided into problems with non-smooth stiffness [1–58], non-smooth friction [59–70], and a combination of those two effects [70–117]. The investigations into smooth dynamical systems have been focussed predominantly on complex dynamics of pendula systems [118–133], vortex induced vibration [134–142], underwater acoustics [143–149] and neurodynamics [150–158].

My research group is organized in a form of the Centre for Applied Dynamics Research (CADR), which was officially opened in 2003. On average the Centre would have 25 members comprised of academics and PhD students (see left panel of Fig. 6 with a group photograph from CADR annual meeting held in 2006). The main aim of CADR is to develop robust solutions for the fundamental problems in dynamics and to apply them to engineering practice. CADR has modern and well equipped experimental laboratories, which attract visitors from around the world. It has a rich seminar programme, has hosted many international visitors, has organized half a dozen of international conferences and collaborates with the leading scholars (see right panel of Fig. 6).

The University of Aberdeen (UoA) located in the North East of Scotland, is an ancient institution founded in 1495 by William Elphinstone, the Bishop of Aberdeen and Chancellor of Scotland at that time. The UoA is Scotland's 3rd oldest university and the 5th oldest in the English-speaking world and its motto is *'Initium sapientiae timor domini'* (The fear of the Lord is the beginning of wisdom). It has been consistently ranked among the top 160 universities in the world and within the top 20 universities in the United Kingdom.

It is an institution with a great heritage and achievements including 5 Nobel Prize winners. James Clerk Maxwell, the founder of modern physics, was the University professor before joining the University of Cambridge. It has over 15000 students and around 2500 of academic and administrative staff. UoA researches and educates in the whole spectrum of academic disciplines ranging from art, through medicine and mathematics to engineering. Late University Principal, Professor Sir Duncan Rice had run a unique in the UK and very successful fund raising campaign allowing to upgrade many university facilities including the library, which was named after him (see Sir Duncan Rice Library on the top left panel of Fig. 7).

Aberdeen is the third largest city in Scotland and the Europe capital of the energy industry. At the same time Aberdeen is the doorstep of a picturesque and historic North-East coast. This part of Scotland is Aberdeenshire, having one of the highest densities of castles (see the bottom photographs of Fig. 7) and distilleries in the United Kingdom.

3. International collaborations, conferences and editorial work

Undertaking high quality research especially in science and engineering must involve interactions with the leading researchers and I have realized this fact very early in my career. As my academic and research identity has been shaped by Polish, American and British higher education systems, I have naturally developed many collaborative links and projects within UK and internationally. These includes EPSRC funded projects undertaken in collaboration with the University of Glasgow, Polish Academy of Sciences and Rolls Royce. I have had over two dozens international exchange projects with Brazil, China, Check Republic, India, Italy, Israel, Netherlands, Poland and Russia, funded by the British Council, London Mathematical Society, Royal Society of Edinburgh, Royal Society of London, Royal Academy of Engineering and others.

I have participated in numerous international conferences and visited many collaborators and colleagues delivering in total over 50 keynote and plenary addresses and around 150 talks around the world. I have organized and co-organized around 100 sessions at various international conferences and have helped to shape long running conference series such as *Advanced Problems in Mechanics* organized by the Russian Academy of Sciences in St Petersburg.

I have established two conference series, *Recent Advances in Nonlinear Mechanics (RANM)* and *International Conference on Engineering Vibration (ICoEV)* in 2013. The first series, RANM, started in Aberdeen in 2005 (see Fig. 8) with some 150 delegates including leading international figures in dynamics, fluid and solid mechanics. The following RANM conferences were held in Kuala Lumpur (2009), Harbin (2014), Lodz (2019) and Hangzhou (2021). The last one was organized in a hybrid mode with some 30,000 attending online.

The ICoEV series of conference originates from long running

conferences organized by two Indian colleagues, Profs M Baneerjee and P Biswas, named as *International Conferences on Vibration Problems (ICoVP)*, which started in India and then became more international. My involvement in the ICoVP conferences was in 2011 and 2013, when these conferences were held in Prague and Lisbon. The first ICoEV conference was held in Ljubljana in 2015, the second was in Sofia (2015), the third was hosted by the University of Aberdeen in 2020 and it was online due to the COVID-19 pandemic.

Throughout my career I have been involved in development and stimulating research in my area of engineering dynamics also by organizing special issues of various journals [180–193]. These include *Philosophical Transactions of the Royal Society*, *Proceedings of the Institution of Mechanical Engineers*, *Meccanica*, *Chaos Solitons and Fractals*, *IMA Journal of Applied Mathematics*, *International Journal of Bifurcation and Chaos*, *International Journal of Nonlinear Mechanics* and *International Journal of Mechanical Sciences*. In total, together with my guest co-editors, I have published 14 special issues.

4. Closure

In summary, my academic career has been formed and developed in the UK, after having been educated in Poland and undertaking research spells in the US in mid-nineties. Since 2006, I am holding a prestigious Sixth Century Chair in Applied Dynamics and I am the founding director of the Centre for Applied Dynamics Research at the University of Aberdeen. My area of research is theoretical and experimental nonlinear dynamics, which I apply to various engineering problems.

I am also the inventor of new patented drilling technology called Resonance Enhanced Drilling and the Founder and Chief Technology Officer of a spinoff company iVDynamics Ltd. In Aberdeen I have established unique experimental laboratories allowing to investigate complex nonlinear dynamic interactions in mechanical systems with the focus on energy generation.

I have received many awards and distinctions including a Senior Fulbright Scholarship (1994), Fellowship of the Royal Society of Edinburgh (2009), DSc *honoris causa* by the Lodz University of Technology (2013), Distinguished Professorships at the Perm National Research Polytechnic University (2017), Balseiro Institute (2018) and Yanshan University (2021), a Scottish Champion of Knowledge Exchange (2020). In 2014 and 2021 I was a panelist of the Research Excellence Framework assessing the quality of research in the UK.

I have published over 500 journal and conference papers and I have been a frequent keynote and plenary speaker at major international conferences. I sit on a dozen editorial boards of peer review journals and since 2013 I have been the Editor-In-Chief of *International Journal of Mechanical Sciences*, a leading journal in mechanics and mechanical engineering [194].(Fig. 1, Fig. 2)

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

No data was used for the research described in the article.

References

- [1] Wiercigroch M. Bifurcation analysis of harmonically excited linear oscillator with clearance. *Chaos Solitons Fractals* 1994;4(2):297–303.
- [2] Wiercigroch M, Sin VWT. Experimental study of a symmetrical piecewise base-excited oscillator. *Trans ASME - J Appl Mech* 1998;65:657–63.
- [3] Wiercigroch M, Sin VWT, Li K. Measurement of chaotic vibration in symmetrically piecewise linear oscillator. *Chaos Solitons Fractals* 1998;9(1-2): 209–20.
- [4] Sin VWT, Wiercigroch M. The design of a symmetrically piecewise oscillator for measurement of chaotic vibration. *Proc Inst Mech Eng Part C* 1999;213:241–9.
- [5] Wiercigroch M, Neilson RD, Player MA. Material removal rate prediction for ultrasonic drilling of hard materials using impact oscillators approach. *Phys Lett A* 1999;259(2):91–6.
- [6] Wiercigroch M. Modelling of dynamical systems with motion dependent discontinuities. *Chaos Solitons Fractals* 2000;11(15):2429–42.
- [7] Woo K-C, Rodger AA, Neilson RD, Wiercigroch M. Application of HB method to periodic responses of a vibro-impact milling system. *Chaos Solitons Fractals* 2000; 11(15):2515–2425.
- [8] Loong K-SV, Wojewoda J, Wiercigroch M. Design of load cell for measurement ultrasonic percussive drilling forces. *Proc Inst Mech Eng – Part C* 2001;215: 965–72.
- [9] Karpenko E, Wiercigroch M, Cartmell MP. Regular and chaotic dynamics of a discontinuously nonlinear rotor system. *Chaos Solitons Fractals* 2002;13(6): 1231–42.
- [10] Karpenko E, Wiercigroch M, Pavlovskaja EE, Cartmell MP. Piecewise approximate analytical solutions for a Jeffcott rotor with a snubber ring. *Int J Mech Sci* 2002; 44(3):475–88.
- [11] Karpenko EV, Wiercigroch M, Pavlovskaja EE. Bifurcation analysis of the preloaded Jeffcott rotor. *Chaos Solitons Fractals* 2003;15:407–16.
- [12] Foong C-H, Wiercigroch M, Deans WF, Pavlovskaja EE. Chaos caused by fatigue crack growth. *Chaos Solitons Fractals* 2003;16:651–9.
- [13] Pavlovskaja EE, Karpenko EV, Wiercigroch M. Nonlinear dynamic interactions of a Jeffcott rotor with a preloaded snubber ring. *J Sound Vib* 2004;276(1-2): 361–79.
- [14] Emans J, Wiercigroch M, Krivtsov AM. Cumulative effect of structural nonlinearities: dynamics of a cantilever beam system with impacts. *Chaos Solitons Fractals* 2005;23(5):1661–70.
- [15] Wiercigroch M, Wojewoda J, Krivtsov AM. Dynamics of ultrasonic percussive drilling of hard rocks. *J Sound Vib* 2005;280(3-5):739–57.
- [16] Wiercigroch M. Applied nonlinear dynamics of non-smooth dynamical systems. *J Braz Soc Mech Sci Eng* 2006;28(4):521–8.
- [17] Ing J, Pavlovskaja E, Wiercigroch M. Dynamics of a nearly symmetrical piecewise oscillator close to grazing incidence: modelling and experimental verification. *Nonlinear Dyn* 2006;46:225–38.
- [18] Woo K-C, Rodger AA, Neilson RD, Wiercigroch M. Phase shift adjustment for Harmonic Balance Method applied to vibro-impact systems. *Meccanica* 2006;41: 269–82.
- [19] Cao Q, Wiercigroch M, Pavlovskaja EE, Grebogi C, Thompson JMT. Archetypal oscillator for smooth and discontinuous dynamics. *Phys Rev E* 2006;74:046218. 5 pages.
- [20] Karpenko EV, Wiercigroch M, Pavlovskaja EE, Neilson RD. Experimental verification of Jeffcott rotor model with preloaded snubber ring. *J Sound Vib* 2006;298(4-5):907–17.
- [21] Foong CH, Wiercigroch M, Pavlovskaja E, Deans WF. Nonlinear vibration caused by fatigue. *J Sound Vib* 2007;303(1-2):58–77.
- [22] Cao Q, Wiercigroch M, Pavlovskaja EE, Thompson JMT, Grebogi C. Piecewise linear approach to an archetypal oscillator for smooth and discontinuous dynamics. *Philos Trans R Soc – Part A* 2008;366:635–52.
- [23] Ing J, Pavlovskaja EE, Wiercigroch M, Banerjee S. Experimental study of impact oscillator with one sided elastic constraint. *Philos Trans R Soc – Part A* 2008;366: 679–704.
- [24] Cao Q, Wiercigroch M, Pavlovskaja EE, Grebogi C, Thompson JMT. The limit case response of the archetypal oscillator for smooth and discontinuous dynamics. *Int J Non Linear Mech* 2008;43(6):462–73.
- [25] de Souza SLF, Wiercigroch M, Caldas LL, Balthazar JM. Suppressing grazing chaos in impacting system by structural nonlinearity. *Chaos, Solitons Fractals* 2008;38: 864–9.
- [26] Ma Y, Ing J, Banerjee S, Wiercigroch M, Pavlovskaja E. The nature of the normal form map for soft impacting systems. *Int J Non Linear Mech* 2008;43(6):504–13.
- [27] Wiercigroch M, Krivtsov AM, Wojewoda J. Vibrational energy transfer via modulated impacts for percussive drilling. *J Theoret Appl Mech* 2008;46(3): 715–26.
- [28] Sitnikova E, Pavlovskaja EE, Wiercigroch M. Dynamics of impact oscillator with SMA constraint. *Eur Phys J – Spec Top* 2008;165(229):238.
- [29] Banerjee S, Ing J, Pavlovskaja E, Wiercigroch M, Reddy R. Invisible grazing and dangerous bifurcations in impacting systems. *Phys Rev E* 2009;79:037201.
- [30] Ing J, Pavlovskaja E, Wiercigroch M, Banerjee S. Bifurcation analysis of an impact oscillator with one sided elastic constraint near grazing. *Physica D* 2010;239: 312–21.
- [31] Ing J, Pavlovskaja E, Wiercigroch M, Banerjee S. Complex dynamics of bilinear oscillator close to grazing. *Int J Bifurcation Chaos* 2010;20(11):3801–17.
- [32] Sitnikova E, Pavlovskaja EE, Wiercigroch M, Savi MA. Vibration control of impact oscillator with SMA constraint. *Int J Non Linear Mech* 2010;45:837–49.
- [33] Kundu S, Banerjee S, Ing J, Pavlovskaja E, Wiercigroch M. Singularities in soft impacting systems. *Physica D* 2012;241:553–65.
- [34] Sitnikova E, Pavlovskaja E, Ing J, Wiercigroch M. Experimental bifurcations of an impact oscillator with SMA constraint. *Int J Bifurcation Chaos* 2012;22(5): 1230017.
- [35] Divenyi S, Savi MA, Wiercigroch M, Pavlovskaja E. Drill-string vibration analysis using non-smooth dynamics approach. *Nonlinear Dyn* 2012;70:1017–35.

- [36] Cao Q, Wang, Wang D, Chen Y, Wiercigroch M. Irrational elliptic functions and the analytical solutions of SD oscillator. *J Theoret Appl Mech* 2012;50(3):701–15.
- [37] Kryzhevich SE, Wiercigroch M. Topology of vibro-impact systems in the neighbourhood of grazing. *Physica D* 2012;241:1919–31.
- [38] Han Y, Cao Q, Chen Y, Wiercigroch M. Novel smooth and discontinuous oscillator with strong irrational nonlinearities. *Sci China* 2012;55:1832–43.
- [39] Sitnikova E, Pavlovskaja EE, Ing J, Wiercigroch M. Suppressing nonlinear resonances in impact oscillator using SMAs. *Smart Mater Struct* 2012;21:075028.
- [40] Paez-Chavez J, Wiercigroch M. Bifurcation analysis of periodic orbits of a non-smooth Jeffcott rotor model. *Commun Nonlinear Sci Numer Simul* 2013;18:2571–80.
- [41] Cao QJ, Han YW, Liang TW, Wiercigroch M, Piskarev S. Multiple buckling and codimension-three bifurcation phenomena of a nonlinear oscillator. *Int J Bifurcation Chaos* 2014;24(1):1430005.
- [42] Han YW, Cao QJ, Wiercigroch M. Chaotic thresholds for the piecewise linear discontinuous system with multiple well potentials. *Int J Non Linear Mech* 2015;70:145–52.
- [43] Páez Chávez J, Vaziri V, Wiercigroch M. Modelling and experimental verification of an asymmetric Jeffcott rotor with radial clearance. *J Sound Vib* 2015;334:86–97.
- [44] Sayah M, Da Silva Baptista M, Ing J, Wiercigroch M. Attractor reconstruction of an impact oscillator for parameter identification. *Int J Mech Sci* 2015;102:212–23.
- [45] Jiang HB, Wiercigroch M. Geometrical insight into non-smooth bifurcations of a soft impact oscillator. *IMA J Appl Math* 2016;81:662–78.
- [46] Liao M, Ing J, Páez Chávez J, Wiercigroch M. Bifurcation techniques for stiffness identification of an impact oscillator. *Commun Nonlinear Sci Numer Simul* 2016;41:19–31.
- [47] Hao Z, Cao Q, Wiercigroch M. Two-sided damping constraint control strategy for high-performance vibration isolation and end-stop impact protection. *Nonlinear Dyn* 2016;86:2129–44.
- [48] Jiang H, Chong ASE, Ueda Y, Wiercigroch M. Grazing-induced bifurcations in impact oscillators with elastic and rigid constraints. *Int J Mech Sci* 2017;127:204–14.
- [49] Chong ASE, Yue Y, Pavlovskaja E, Wiercigroch M. Global dynamics of a harmonically excited oscillator with a play: Numerical studies. *Int J Non Linear Mech* 2017;94:98–108.
- [50] Hao Z, Cao Q, Wiercigroch M. Nonlinear dynamics of the quasi-zero-stiffness SD oscillator based upon the local and global bifurcation analyses. *Nonlinear Dyn* 2017;87:987–1014.
- [51] Chong ASE, Brzeski P, Wiercigroch M, Perlikowski P. Path-following bifurcation analysis of church bell dynamics. *J Comput Nonlinear Dyn* 2017;12(6):061017.
- [52] Liao M, Ing J, Sayah M, Wiercigroch M. Dynamic method of stiffness identification in impacting systems for percussive drilling applications. *Mech Syst Sig Process* 2017.
- [53] Brzeski P, Chong ASE, Wiercigroch M, Perlikowski P. Impact adding bifurcation in an autonomous hybrid dynamical model of church bell. *Mech Syst Sig Process* 2018;104:716–24.
- [54] Li S, Vaziri V, Kapitaniak M, Millett JM, Wiercigroch M. Application of resonance enhanced drilling to coring. *J Pet Sci Eng* 2020;188:106866.
- [55] Wiercigroch M, Kovacs S, Zhong S, Costa D, Vaziri V, Kapitaniak M, Pavlovskaja E. Versatile mass excited impact oscillator. *Nonlinear Dyn* 2020;99(1):323–39.
- [56] Costa D, Vaziri V, Kapitaniak M, Kovacs S, Pavlovskaja E, Wiercigroch M. Chaos in impact oscillators not in vain: dynamics of new mass excited oscillator. *Nonlinear Dyn* 2020;102:835–61.
- [57] Liao M, Wiercigroch M, Sayah M, Ing J. Experimental verification of the percussive drilling model. *Mech Syst Sig Process* 2021;146:107067.
- [58] Pei L, Chong A, Pavlovskaja E, Wiercigroch M. Computation of periodic orbits for piecewise linear oscillator by Harmonic Balance Methods. *Commun Nonlinear Sci Numer Simul* 2022;108:106220.
- [59] Wiercigroch M. Comments on the study of a harmonically excited linear oscillator with a Coulomb damper. *J Sound Vib* 1993;167(3):560–3.
- [60] Wiercigroch M. A note on the switch function for the stick-slip phenomenon. *J Sound Vib* 1994;175(5):700–4.
- [61] Wiercigroch M, Sin VWT, Liew ZFK. Non-reversible dry friction oscillator: design and measurements. *Proc Inst Mech Eng, Part C* 1999;213:527–34.
- [62] Krivtsov AM, Wiercigroch M. Dry friction model of percussive drilling. *Meccanica* 1999;34(6):425–34.
- [63] Krivtsov AM, Wiercigroch M. Penetration rate prediction for percussive drilling via dry friction model. *Chaos Solitons Fractals* 2000;11(15):2479–85.
- [64] Stefanski A, Wojewoda J, Wiercigroch M, Kapitaniak T. Chaos caused by non-reversible dry friction. *Chaos Solitons Fractals* 2003;16:661–4.
- [65] Stefanski A, Wojewoda J, Wiercigroch M, Kapitaniak T. Regular and chaotic oscillations of friction force. *Proc Inst Mech Eng – Part C* 2006;220(3):273–84.
- [66] Wojewoda J, Stefanski A, Wiercigroch M, Kapitaniak T. Hysteretic effects of dry friction: modelling and experimental studies. *Philos Trans R Soc – Part A* 2008;366:747–65.
- [67] Wojewoda J, Stefanski A, Wiercigroch M, Kapitaniak T. Estimation of Lyapunov exponents for a system with sensitive friction model. *Arch Appl Mech* 2009;79:667–77.
- [68] Saha A, Wiercigroch M, Jankowski K, Wahi P, Stefanski A. Investigation of two different friction models from the perspective of friction-induced vibrations. *Tribol Int* 2015;90:185–92.
- [69] Saha A, Stefanski, Wahi P, Wiercigroch M. Modified LuGre friction model for an accurate prediction of friction force in the pure sliding regime. *Int J Non Linear Mech* 2016;80:122–31.
- [70] Dehkordi MK, Osguei AT, Khamoushi I, Pavlovskaja E, Wiercigroch M. Internal mechanics of anti stick-slip tool. *Int J Mech Sci* 2022;221:107188.
- [71] Dai W, Yang J, Wiercigroch M. Vibration energy flow transmission in systems with Coulomb friction. *Int J Mech Sci* 2022;214:106932.
- [72] Pavlovskaja EE, Wiercigroch M, Grebogi C. Modelling of an impact system with a drift. *Phys Rev E* 2001;64:056224 (9 pages).
- [73] Pavlovskaja EE, Wiercigroch M, Woo K-C, Rodger AA. Modelling of a vibro-impact ground moling system by an impact oscillator with a frictional slider. *Meccanica* 2003;38(1):85–97.
- [74] Pavlovskaja EE, Wiercigroch M. Modelling of vibro-impact system driven by beat frequency. *Int J Mech Sci* 2003;45(4):623–41.
- [75] Pavlovskaja EE, Wiercigroch M. Periodic solutions finder for an impact system with a drift. *J Sound Vib* 2003;267(4):893–911.
- [76] Pavlovskaja EE, Wiercigroch M, Grebogi C. (10 pages). Two dimensional map for impact oscillator with drift. *Phys Rev E* 2004;70:036201.
- [77] Pavlovskaja EE, Wiercigroch M. Analytical drift reconstruction for an impact system operating in periodic and chaotic regimes. *Chaos Solitons Fractals* 2004;19(1):151–61.
- [78] Pavlovskaja EE, Wiercigroch M. Low dimensional maps for piecewise smooth oscillators. *J Sound Vib* 2007;305:750–71.
- [79] Litak G, Syta A, Wiercigroch M. Identification of chaos in a cutting process by the 0-1 test. *Chaos, Solitons Fractals* 2009;40:2095–101.
- [80] Ajibose O, Wiercigroch M, Pavlovskaja E, Akisanya AR. Influence of contact force models on the global and local dynamics of drifting impact oscillator. *Int J Non Linear Mech* 2010;45:850–8.
- [81] Ajibose O, Wiercigroch M, Pavlovskaja E, Akisanya AR, Karolyi G. Dynamics of a drifting impact oscillator with a new model of the progression phase. *J Appl Mech* 2012;79:061007.
- [82] Liu Y, Wiercigroch M, Pavlovskaja E. Modelling of a vibro-impact capsule system. *Int J Mech Sci* 2013;66:2–11.
- [83] Liu Y, Pavlovskaja E, Hendry DC, Wiercigroch M. Vibro-impact responses of capsule system with various friction models. *Int J Mech Sci* 2013;72:39–54.
- [84] Páez Chávez J, Wiercigroch M, Pavlovskaja E. Bifurcation analysis of a piecewise-linear impact oscillator with drift. *Nonlinear Dyn* 2014;77:213–27.
- [85] Pavlovskaja E, Hendry DC, Wiercigroch M. Low dimensional models for modelling of the resonance enhanced drilling. *Int J Mech Sci* 2015;91:110–9.
- [86] Liu Y, Pavlovskaja E, Wiercigroch M, Peng Z. Forward and backward motion control of a vibro-impact capsule system. *Int J Non Linear Mech* 2015;70:30–46.
- [87] Kapitaniak M, Vaziri V, Páez Chávez J, Nandakumar K, Wiercigroch M. Unveiling complexity of drill-string vibrations: experiments and modelling. *Int J Mech Sci* 2015;101-102:324–37.
- [88] Wang J, Liu C, Wiercigroch M, Wang C, Shui Y. Stability of periodic modes and bifurcation behaviors in a bouncing-dimer system. *Nonlinear Dyn* 2016;86:1477–92.
- [89] Liu Y, Pavlovskaja and Wiercigroch M. Experimental verification of the vibro-impact capsule model. *Nonlinear Dyn* 2016;83:1029–41.
- [90] Páez Chávez J, Liu L, Pavlovskaja P, Wiercigroch M. Path-following analysis of the dynamical response of a piecewise-linear capsule system. *Commun Nonlinear Sci Numer Simul* 2016;37:103–14.
- [91] Kapitaniak M, Vaziri V, Páez Chávez J, Wiercigroch M. Numerical study of forward and backward whirling of drill-string. *J Comput Nonlinear Dyn* 2017;12(6):061009.
- [92] Liao M, Liu Y, Páez Chávez J, Chong ASE, Wiercigroch M. Dynamics of vibro-impact drilling with linear and nonlinear rock models. *Int J Mech Sci* 2018;146-147:200–10.
- [93] Kapitaniak M, Vaziri V, Páez Chávez J, Wiercigroch M. Experimental studies of forward and backward whirls of drill-string. *Mech Syst Sig Process* 2018;100:454–65.
- [94] Liu Y, Chávez JP, Pavlovskaja E, Wiercigroch M. Analysis and control of the dynamical response of a higher order drifting oscillator. *Proc R Soc A* 2018;474:20170500.
- [95] Wiercigroch M. Chaotic vibrations of a simple model of the machine tool-cutting process system. *Trans ASME - J Vib Acoust* 1997;119(3):468–75.
- [96] Wiercigroch M, Cheng AD-H. Chaotic and stochastic dynamics of metal cutting process. *Chaos Solitons Fractals* 1997;8(4):715–26.
- [97] Wiercigroch M, Krivtsov AM. Frictional chatter in orthogonal metal cutting. *Philos Trans R Soc Lond* 2001;359:713–38.
- [98] Wiercigroch M, Budak E. Nonlinearities, chatter generation and suppression in metal cutting. *Philos Trans R Soc Lond* 2001;359:663–93.
- [99] Warminski J, Litak G, Cartmell MP, Khanin R, Wiercigroch M. Approximate analytical solutions for primary chatter in nonlinear metal cutting model. *J Sound Vib* 2003;259(4):917–33.
- [100] Cao Q, Wiercigroch M, Pavlovskaja E, Yang S. Bifurcations and the penetrating rate analysis of a model for percussive drilling. *Acta Mech Sin* 2010;26(3):467–75.
- [101] Nandakumar K, Wiercigroch M. Stability analysis of a state dependent delayed model for drill-string vibrations. *J Sound Vib* 2013;332(10):2575–92.
- [102] Yan Y, Xu J, Wiercigroch M. Chatter in transverse grinding process. *J Sound Vib* 2014;333:937–53.
- [103] Rusinek R, Wiercigroch M, Wahi P. Modelling of frictional chatter in metal cutting. *Int J Mech Sci* 2014;89:167–76.
- [104] Rusinek R, Wiercigroch M, Wahi. Influence of tool flank forces on complex dynamics of cutting system process. *Int J Bifurcation Chaos* 2014;24(9):1450115.

- [105] Yan Y, Xu J, Wiercigroch M. Non-linear analysis and quench control of chatter in plunge grinding. *Int J Non Linear Mech* 2015;70:134–44.
- [106] Yan Y, Xu J, Wiercigroch M. Regenerative and frictional chatter in plunge grinding. *Nonlinear Dyn* 2016;86:283–307.
- [107] Yan Y, Xu J, Wiercigroch M. Regenerative and frictional chatter in self-interrupted plunge grinding. *Meccanica* 2016;51:3185–202.
- [108] Yan Y, Xu J, Wiercigroch M. Basins of attraction of the bistable region of time-delayed cutting dynamics. *Phys Rev E* 2017;96(3):032205.
- [109] Yan Y, Xu J, Wiercigroch M. Regenerative chatter in a plunge grinding process with workpiece imbalance. *Int J Adv Manuf Technol* 2017;89(9-12):2845–62.
- [110] Yan Y, Xu J, Wiercigroch M. Stability and dynamics of parallel plunge grinding. *Int J Adv Manuf Technol* 2018;99(1-4):881–95.
- [111] Yan Y, Xu J, Wiercigroch M. Estimation and improvement of cutting safety. *Nonlinear Dyn* 2019;98(4):2975–88.
- [112] Yan Y, Xu J, Wiercigroch M. Modelling of regenerative and frictional cutting dynamics. *Int J Mech Sci* 2019;156:86–93.
- [113] Yan Y, Wiercigroch M. Dynamics of rotary drilling with non-uniformly distributed blades. *Int J Mech Sci* 2019;160:270–81.
- [114] Xie D, Huang Z, Ma Y, Vaziri V, Kapitaniak M, Wiercigroch M. Nonlinear dynamics of lump mass model of drill-string in horizontal well. *Int J Mech Sci* 2020;174:105450.
- [115] Yan Y, Liu G, Wiercigroch M, Xu J. Safety estimation for a new model of regenerative and frictional cutting dynamics. *Int J Mech Sci* 2021;201:106468.
- [116] Yan Y, Xu J, Wiercigroch M, Guo Q. Statistical basin of attraction in time-delayed cutting dynamics: modelling and computation. *Physica D* 2021;416:132779.
- [117] Hao Z, Wang D, Wiercigroch M. Nonlinear dynamics of new magneto-mechanical oscillator. *Commun Nonlinear Sci Numer Simul* 2022;105:106092.
- [118] Xu X, Wiercigroch M, Cartmell MP. Rotating solutions for a parametrically driven pendulum. *Chaos Solitons Fractals* 2005;23(5):1537–48.
- [119] Xu X, Wiercigroch M. Approximate analytical solutions for oscillatory and rotational motion of a parametric pendulum. *Nonlinear Dyn* 2007;47(1-3):311–20.
- [120] Xu X, Pavlovskaja EE, Wiercigroch M, Romeo F, Lenci S. Dynamic interactions between parametric pendulum and electrodynamic shaker: effect of non-ideal excitation source. *Z Angew Math Mech* 2007;87(2):172–87.
- [121] Lenci S, Pavlovskaja EE, Rega G, Wiercigroch M. Rotating solutions and stability of parametric pendulum by perturbation method. *J Sound Vib* 2008;310(1-2):243–59.
- [122] Litak G, Borowiec M, Wiercigroch M. Phase locking and rotational motion of a kinematically forced pendulum in noisy and chaotic conditions. *Dyn Syst* 2008;23(3):259–65.
- [123] Horton B, Wiercigroch M, Xu X. Transient tumbling chaos and damping identification for parametric pendulum. *Philos Trans R Soc – Part A* 2008;366:767–84.
- [124] Litak G, Wiercigroch M, Horton B, Xu X. Transient chaotic behaviour versus periodic motion of a parametric pendulum by recurrence plots. *Z Angew Math Mech* 2010;90(1):33–41.
- [125] Horton BH, Sieber J, Thompson JMT, Wiercigroch M. Dynamics of the nearly parametric pendulum. *Int J Non Linear Mech* 2011;46:436–42.
- [126] Pavlovskaja E, Horton B, Wiercigroch M, Lenci S, Rega G. Approximate rotational solutions of pendulum under combined vertical and horizontal excitation. *Int J Bifurcation Chaos* 2012;22(5):1250100.
- [127] Nandakumar K, Wiercigroch M, Chatterjee A. Optimum energy extraction from rotational motion of a parametrically excited pendulum. *Mech Res Commun* 2012;43:7–14.
- [128] Strzalko J, Grabski J, Wojewoda J, Wiercigroch M, Kapitaniak T. Synchronous rotation of the set of double pendula: experimental observations. *Chaos* 2012;22:047503.
- [129] Nandakumar K, Wiercigroch M. Galerkin projections for state-dependent delay differential equations with applications to drilling. *Appl Math Model* 2013;37:1705–22.
- [130] Vaziri V, Najdecka A, Wiercigroch M. Experimental control for initiating and maintaining rotation of parametric pendulum. *Eur Phys J Spec Top* 2014;223:795–812.
- [131] Najdecka A, Kapitaniak T, Wiercigroch M. Rotational motion synchronization of parametric pendulums. *Int J Non Linear Mech* 2015;70:84–94.
- [132] Najdecka A, Narayanan S, Wiercigroch M. Rotary motion of the parametric and planar pendulum under stochastic wave excitation. *Int J Non Linear Mech* 2015;70:30–8.
- [133] Terrero González A, Dunning P, Howard I, McKee K, Wiercigroch M. Is wave energy untapped potential? *Int J Mech Sci* 2021;205:106544.
- [134] Keber M, Wiercigroch M. Dynamics of vertical riser with weak structural nonlinearity excited by wakes. *J Sound Vib* 2008;315:685–99.
- [135] Srinil N, Wiercigroch M, O'Brien P. Reduced order modelling of vortex-induced vibration of catenary riser. *Ocean Eng* 2009;36:1404–14014.
- [136] Wang D, Chen YS, Wiercigroch M, Cao Q. Bifurcation and dynamic response analysis of a rotating blade excited by upstream vortices. *Appl Math Mech* 2016;37:1251–74.
- [137] Wang D, Chen Y, Wiercigroch M, Cao Q. A three-degree-of-freedom model for vortex-induced vibrations of turbine blades. *Meccanica* 2016;51:2607–28.
- [138] Pavlovskaja E, Keber M, Postnikov A, Reddington K, Wiercigroch M. Multi-modes approach to modelling of vortex-induced vibration. *Int J Non Linear Mech* 2016;80:40–51.
- [139] Postnikov A, Pavlovskaja E, Wiercigroch M. 2DOF CFD calibrated wake oscillator model to investigate vortex-induced vibrations. *Int J Mech Sci* 2017;127:176–90.
- [140] Kurushina V, Pavlovskaja E, Postnikov A, Wiercigroch M. Calibration and comparison of VIV wake oscillator models for low mass ratio structures. *Int J Mech Sci* 2018;142-143:547–60.
- [141] Kurushina V, Pavlovskaja E, Wiercigroch M. VIV of flexible structures in 2D uniform flow. *Int J Eng Sci* 2020;150:103211.
- [142] Wang D, Hao Z, Pavlovskaja E, Wiercigroch M. Bifurcation analysis of vortex-induced vibration of low-dimensional models of marine risers. *Nonlinear Dyn* 2021;106:147–67.
- [143] Wiercigroch M, Cheng AH-D, Simmens J, Badiéy M. Nonlinear behavior of acoustic rays in underwater sound channel. *Chaos Solitons Fractals* 1998;9(1-2):193–207.
- [144] Wiercigroch M, Badiéy M, Simmens J, Cheng AH-D. Nonlinear dynamics of underwater acoustics. *J Sound Vib* 1999;220(5):771–86.
- [145] Bodai T, Fenwick AJ, Wiercigroch M. Ray chaos in underwater acoustics and its application applications. *Int J Bifurcation Chaos* 2008;18(5):1579–87.
- [146] Bodai T, Fenwick AJ, Wiercigroch M. New graphical tools for studying acoustic ray propagation. *J Sound Vib* 2009;324:350–60.
- [147] Bodai T, Fenwick AJ, Wiercigroch M. Ray stability for background sound speed profiles with transition. *Int J Bifurcation Chaos* 2009;19:2953–64.
- [148] Bodai T, Wiercigroch M. Acoustic ray stability for long-range sound speed profile transition scenarios. *Int J Bifurcation Chaos* 2011;21:177–94.
- [149] Wang Z, Zhou W, Shu T, Xue Q, Zhang R, Wiercigroch M. Modelling of low-frequency acoustic wave propagation in dilute gas-bubbly liquids. *Int J Mech Sci* 2022;216:106979.
- [150] Du Y, Lu Q, Wang S, Wiercigroch M. A new method for characterizing patterns of neural spike trains and its application. *Int J Non Linear Mech* 2009;44:432–40.
- [151] Han F, Lu Q, Wiercigroch M, Li Q. Chaotic burst synchronization in heterogeneous small-world neuronal network with noise. *Int J Non Linear Mech* 2009;44:298–303.
- [152] Han F, Lu Q, Wiercigroch M, Ji Q. Complete and phase synchronization in heterogeneous small-world networks. *Chin Phys B* 2009;18(2):482–8.
- [153] Han F, Zhen B, Du Y, Zheng Y, Wiercigroch M. Global Hopf bifurcation analysis of a six-dimensional Fitzhugh-Nagumo neural network with delay by a synchronized scheme. *Discr Continuous Dyn Syst - B* 2011;16(2):457–74.
- [154] Han F, Wiercigroch M, Fang JA, Wang Z. Degree of excitement and synchronization of small-world neuronal networks with synapse plasticity. *Int J Neural Syst* 2011;21(5):415–25.
- [155] Han F, Lu QS, Wiercigroch M, Fang JA, Wang ZJ. Firing synchronization of learning neuronal networks with small-world connectivity. *Int J Non Linear Mech* 2012;47:1161–6.
- [156] Han YW, Cao QJ, Wiercigroch M. Estimation of chaotic thresholds for the recently proposed rotating pendulum. *Int J Bifurcation Chaos* 2013;23(4):1350074.
- [157] Sun X, Han F, Wiercigroch M, Shi X. Effects of time-periodic inter coupling strength on burst synchronization of a clustered neuronal network. *Int J Non Linear Mech* 2015;70:119–25.
- [158] Pei L, Wang S, Wiercigroch M. Analysis of Hopf bifurcations in differential equations with state-dependent delays via multiple scales method. *ZAMM* 2018;98:789–801.
- [159] De Paula AS, Savi M, Wiercigroch M, Pavlovskaja E. Bifurcation control of a parametric pendulum. *Int J Bifurcation Chaos* 2012;22(5):1250111.
- [160] Liu Y, Wiercigroch M, Ing J, Pavlovskaja E. Intermittent control of co-existing attractors. *Philos Trans R Soc – Part A* 2013;371:20120428.
- [161] De Paula AS, Savi MA, Vaziri V, Pavlovskaja E, Wiercigroch M. Experimental bifurcation control of a parametric pendulum. *J Vib Control* 2017;23(14):2256–226.
- [162] Vaziri V, Kapitaniak M, Wiercigroch M. Suppression of drill-string stick-slip vibration by sliding mode control: numerical and experimental studies. *Eur J Appl Math* 2018;29(5):805–25.
- [163] Li W, Vaziri V, Aphale S, Dong S, Wiercigroch M. Dynamics and frequency and voltage control of downhole oil pumping system. *Mech Syst Sig Process* 2020;139:106562.
- [164] Vaziri V, Oladunjoye I, Kapitaniak M, Aphale SS, Wiercigroch M. Parametric analysis of a sliding-mode controller to suppress drill-string stick-slip vibration. *Meccanica* 2021;55(12):2475–92.
- [165] Li WC, Vaziri V, Aphale SS, Dong S, Wiercigroch M. Energy saving by reducing motor rating of sucker-rod pump systems. *Energy* 2021;228:120618.
- [166] Wiercigroch M, Neilson RD, Player MA. Load cell for dynamic measurement of cutting forces generated during ultrasonic drilling and milling of hard materials. *Proc Inst Mech Eng. Part E* 1998;212(E4):263–70.
- [167] Zak A, Cartmell MP, Ostachowicz W, Wiercigroch M. One-dimensional SMA models for use with reinforced composite structures. *Smart Mater Struct* 2003;12:338–46.
- [168] Foong C-H, Wiercigroch M, Deans WF. An experimental rig to investigate fatigue crack growth under dynamic loading. *Meccanica* 2003;38(1):19–31.
- [169] Foong CH, Wiercigroch M, Deans WF. Novel dynamic fatigue-testing device: Design and measurements. *Meas Sci Technol* 2006;17:2218–26.
- [170] Mazzilli CEN, Sanches CT, Baracho Neto OGP, Wiercigroch M, Keber M. Non-linear modal analysis for beams subjected to axial loads: Analytical and Finite Element solutions. *Int J Non Linear Mech* 2008;43(6):551–61.
- [171] Jaksic N, Foong C-H, Wiercigroch M, Boltezar M. Parameter identification and modelling of the fatigue testing rig. *Int J Mech Sci* 2008;50:1142–52.
- [172] Ma L, Korsunsky AM, Wiercigroch M. Dislocation model of localized plastic deformation initiated with a flat punch. *Int J Solids Struct* 2010;47(7-8):1082–9.
- [173] Thompson JMT, Silveira M, van der Heijden GHM, Wiercigroch M. Helical post-buckling of a rod in a cylinder with applications to drill-strings. *Proc R Soc Lond - Part A* 2012;468:1591–614.

- [174] Ajibose OK, Wiercigroch M, Akisanya AR. Experimental studies of the resultant contact forces in drill bit–rock interaction. *Int J Mech Sci* 2015;91:3–11.
- [175] Ma L, Yari N, Wiercigroch M. Shear stress triggering brittle shear fracturing of rock-like materials. *Int J Mech Sci* 2018;146–147:295–302.
- [176] Gasiorek D, Baranowski P, Malachowski J, Mazurkiewicz L, Wiercigroch M. Modelling of guillotine cutting of multi-layered *aluminium* sheets. *J Manuf Processes* 2018;34:374–88.
- [177] Kapitaniak M, Vaziri V, Wiercigroch M. Bifurcation scenarios in helical buckling of slender rods using new FE. *Int J Eng Sci* 2020;147:103197.
- [178] Riabokon E, Poplygin V, Turbakov M, Kozhevnikov E, Kobiakov D, Guzev M, Wiercigroch M. Nonlinear Young's modulus of New Red Sandstone: experimental studies. *Acta Mech Solida Sin* 2021;34:989–99.
- [179] Ma L, Tang Z, Bian Z, Zhu J, Wiercigroch M. Analytical solution for circular inhomogeneous inclusion problems with non-uniform axisymmetric eigenstrain distribution. *Int J Mech Sci* 2021;194:106213.
- [180] Kapitaniak T, Wiercigroch M. Dynamics of impact oscillators: An introduction. *Chaos Solitons Fractals* 2000;11(15):2411–2.
- [181] Wiercigroch M. Nonlinear dynamics in metal cutting: Preface. *Philos Trans R Soc Lond* 2001;359:661–2.
- [182] Wiercigroch M, Kreuzer E, Kapitaniak T. Nonlinear dynamics of mechanical systems. *Meccanica* 2003;38(1):1–3.
- [183] Wiercigroch M, Rodger AA. Control and condition monitoring of engineering systems. *Meccanica* 2003;38(2):181–3.
- [184] Fenwick AJ, Wiercigroch M, Champneys AR. *IMA J Appl Math* 2005;70:603–4.
- [185] Collins M, Wiercigroch M. Guest Editorial - Special Issue on Chaos in Science and Engineering. *Proc Inst Mech Eng Part C J Mech Eng Sci* 2006;220(4):571.
- [186] Wiercigroch M, Pavlovskaja E. Nonlinear dynamics of engineering systems. *Int J Non Linear Mech* 2008;43(6):459–61.
- [187] Wiercigroch M. Introduction. Experimental nonlinear dynamics of fluids. *Philos Trans R Soc – Part A* 2008;366:1227–9.
- [188] Wiercigroch M. Introduction. Experimental nonlinear dynamics of solids. *Philos Trans R Soc – Part A* 2008;366:675–8.
- [189] Lu Q, Wiercigroch M. Special issue on "Nonlinear dynamics in biological systems". *Int J Non Linear Mech* 2010;45(6):601–2.
- [190] Warminski J, Wiercigroch M. Special issue on "Dynamics, control and design of non-linear systems with smart structures". *Int J Non Linear Mech* 2010;45(6): 601–2.
- [191] Lu Q, Chen L, Wiercigroch M. *Int J Bifurcation Chaos* 2012;22(5):1202004. Editorial.
- [192] Wiercigroch M, Pavlovskaja E. Preface. *Int J Non Linear Mech* 2015;70(1).
- [193] Wang B, Wiercigroch M. Forward: Special issue in honour of Professor Steve R. Reid. *Int J Mech Sci* 2015;91:1–2.
- [194] Wiercigroch M. Editorial: *IJMS* cannot stop growing. *Int J Mech Sci* 2021;204: 106557.